# SM HIGGS BRANCHING RATIO MEASUREMENTS AT A LINEAR COLLIDER 



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\left(e^{+} e^{-} \rightarrow Z H \rightarrow b \bar{b}, \sqrt{s}=500 \mathrm{GeV}\right)
$$

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## PARAMETERS

We assume for this study:

- $\sqrt{s}=500 \mathrm{GeV}$ Linear Collider
- Luminosity $\int d t L=500 \mathrm{fb}^{-1}$
- $250 \mathrm{fb}^{-1}$ running with $80 \%$ right polarized electrons
- $250 \mathrm{fb}^{-1}$ running with $80 \%$ left polarized electrons
- 115, 120, 140 and 160 GeV Standard Model Higgs boson masses


## DATA SIMULATION

Pandora v2.1 Monte Carlo (M. Peskin) includes:

- Polarized beams
- Beamstrahlung
- Initial state radiation

Interface to Tauola and Pythia (M. Iwasaki):

- $\tau$ decay
- Parton shower
- Hadronization


## DETECTOR SIMULATION

NLD Large Detector Configuration:

- Vertex Detector: $5 \mu \mathrm{~m}$ res., $r_{i n}=1.2 \mathrm{~cm}$
- Central Tracker: 25-200 cm
- Electromagnetic Calorimeter: 200-250 cm
- Hadronic Calorimeter: $250-374 \mathrm{~cm}$
- 3 T Magnetic Coil
- Muon Detector: $450-650 \mathrm{~cm}$

NLD detector simulation implemented on Root C++ libraries (M. Iwasaki)

## EVENT SELECTION

We select for $e^{+} e^{-} \rightarrow H Z \rightarrow l^{+} l^{-}(l=e, \mu)$

- Reconstruct all lepton pair masses in an event
- Select pair with mass closest to $m_{Z}$
- Calculate recoil mass
- Apply cuts on masses:

$$
\begin{gathered}
\left|m_{Z}-m_{l^{+} l^{-}}\right|<10 \mathrm{GeV} \\
m_{H}-10 \mathrm{GeV}<m_{r e c o i l}<m_{H}+20 \mathrm{GeV}
\end{gathered}
$$

- Include hadronic $Z$ decays by scaling signal up by a factor of 4 (D. Strom, LEP II experience)


Signal event reconstructed $Z$ and recoil mass distributions.

## SIGNAL



Cross sections for $e^{+} e^{-} \rightarrow Z H$ with $Z \rightarrow l^{+} l^{-}(l=e, \mu)$ are in fb with $80 \%$ left polarized electrons.

| $\bullet$ - Mode | 115 | 120 | 140 | 160 |
| :--- | :--- | :--- | :--- | :--- |
| $-H \rightarrow b \bar{b}$ | 5.9 | 3.5 | 1.5 | 0.24 |

- $H \rightarrow W W^{\star}$
0.68
0.74
2.4
5.8
- $H \rightarrow c \bar{c}$
0.24
0.14
0.064
0.0099
- $H \rightarrow \tau^{+} \tau^{-}$
0.62
0.38
0.17
0.027
- $H \rightarrow g g$
0.41
0.27
0.16
0.033
- $H \rightarrow Z Z^{\star}$
0.050
0.08
0.34
0.19


## BACKGROUND

Approximately 29\%/31\%/36\%/39\% (115/120/140/160) of signal events pass the mass selection cuts and are then subjected to decay mode cuts.

A small fraction of backgrounds also pass the cuts. Primary backgrounds, with cross sections for left,right polarizations are:

- $e^{+} e^{-} \rightarrow W^{+} W^{-}$
( $\sigma \approx 14300,1700 \mathrm{fb}$ )
- $e^{+} e^{-} \rightarrow q \bar{q}$
$(\sigma \approx 16000,11000 \mathrm{fb})$
- $e^{+} e^{-} \rightarrow Z Z$
( $\sigma \approx 560,340 \mathrm{fb}$ )
- $e^{+} e^{-} \rightarrow t \bar{t}$
( $\sigma \approx 740,400 \mathrm{fb}$ )

The most pernicious of these is $e^{+} e^{-} \rightarrow Z Z$, especially for the lighter Higgs cases.

Therefore the Higgs mass is reconstructed using tracks and unassociated clusters and cuts are made at the Higgs decay mode level.

## CUT-BASED DECAY MODE TAGS

For $H \rightarrow \tau^{+} \tau^{-}$:

- reconstructed Higgs mass inconsistent with Z mass
- Iow track multiplicity ( $\leq 6$ )

For $H \rightarrow W W^{\star} \rightarrow 2$ jets :

- high momentum lepton in event ( $>10 \mathrm{GeV}$ )
- high momentum lepton is isolated ( $E_{\text {cone }}<10 \mathrm{GeV}$ )

For $H \rightarrow W W^{\star} \rightarrow 4$ jets :

- force event to 4 jets
- best jet pair must satisfy $\left|m_{W}-m_{j j}\right|<10 \mathrm{GeV}$
- jet algorithm $y_{\text {cut }}$ value $y_{32}>0.04$
- thrust in Higgs frame $<0.88$


## CUT-BASED TAGS (CONT.)

For $H \rightarrow b \bar{b}:$

- force event to 2 jets
- calculate $m_{p_{t}}$ with ZVTop (D. Jackson, impl. T. Abe)
- require $m_{p_{t}}>2 \mathrm{GeV}$ for at least one jet

For $H \rightarrow c \bar{c}:$

- force event to 2 jets
- tag jet charm if $m_{p_{t}}<2 \mathrm{GeV}, N_{s i g}>10, p_{j e t} / p_{k i n}>0.45$
- require no jet tagged as beauty, at least one jet tagged as charm, and neither jet contains tertiary vertices

For $H \rightarrow g g$ :

- require no tags from preceding modes
- neither jet has secondary vertices
- no high momentum leptons ( $<1 \mathrm{GeV}$ )


## NEURAL NETWORK STRUCTURE AND TRAINING

In order to optimize these results, the parameters and their cut values were used as inputs to a neural network.

- The neural network has 14 input units (one for each parameter), 15 hidden units, and 6 outputs (one for each decay mode).
- It is fully connected and uses standard back propagation as its learning algorithm.
- To speed and perhaps improve the training, the parameters were mapped to the interval $[0,1]$ by the map $p \mapsto 1-\exp \left[-\left(p / p_{c u t}\right)^{2} \ln 2\right]$.
- For each set parameters in an event $H \rightarrow X$, training asked the network to ouput a 1 for the $H \rightarrow X$ output unit and a 0 for the other output units.


## NEURAL NETWORK TOPOLOGY



State of the neural network for an event $H \rightarrow c \bar{c}$.

## NEURAL NETWORK OPTIMIZATION

- The space $C$ of all possible neural network output cut values is the unit cube in $R^{6}$.
- Each point in $C$ maps to signal $S$ and background $B$ for a given mode $H \rightarrow X$ and thence to fractional branching ratio $\delta_{B R} / B R=\sqrt{S+B} / S$, purity $p=S /(S+B)$, and efficiency $\epsilon=S /\left(\sigma \int d t L\right)$.
- Minimizing $\sqrt{S+B} / S$ for a particular mode mode $H \rightarrow X$ is equivalent to finding the optimal set of neural network output cut values for $H \rightarrow X$.
- For a given mode $H \rightarrow X$, the boundary of the image of $C$ under the $(p, \epsilon)$ map is the optimal purity/efficiency curve.
- We sampled $S$ and $B$ for each mode in the cube on a lattice with $10^{6}$ points.

MISTAGS AND SIGNAL FOR 120 GEV CASE

The analyzed $500 \mathrm{fb}^{-1}$ data sample is listed vertically. The number of signal event tags is listed horizontally.

| Sample | $W W^{\star}$ | $b \bar{b}$ | $c \bar{c}$ | $\tau^{+} \tau^{-}$ | $g g$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $H \rightarrow W W^{\star}$ | 214 | 12.7 | 3.3 | 0.5 | 98 |
| $H \rightarrow b \bar{b}$ | 27.9 | 1599 | 59.7 | 0 | 13.9 |
| $H \rightarrow c \bar{c}$ | 7.0 | 13.6 | 29.3 | 0.02 | 12.2 |
| $H \rightarrow \tau^{+} \tau^{-}$ | 0.3 | 0 | 0.3 | 189.6 | 0 |
| $H \rightarrow g g$ | 52.7 | 9.8 | 3.0 | 0 | 112.8 |
| $H \rightarrow Z Z^{\star}$ | 1.0 | 0.6 | 0.1 | 0 | 0 |
| $e^{+} e^{-} \rightarrow Z Z$ | 123.2 | 524.7 | 38.6 | 24.8 | 161.1 |
| $e^{+} e^{-} \rightarrow W W$ | 0 | 0 | 0 | 0 | 0 |
| $e^{+} e^{-} \rightarrow q \bar{q}$ | 0 | 0 | 0 | 0 | 0 |
| $e^{+} e^{-} \rightarrow t \bar{t}$ | 0 | 0 | 0 | 0 | 0 |

## PURITY/EFFICIENCY PLOTS



Purity vs. efficiency for the case $m_{H}=120 \mathrm{GeV}$. The maximum possible efficiency is 0.31 due to mass cuts.

## FRACTIONAL BRANCHING RATIO RESULTS

Listed below are the fractional branching ratio errors $\delta_{B R} / B R$.

| Mode | 115 | 120 | 140 | 160 | 180 | 200 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\bullet H \rightarrow W W^{\star}$ | 0.16 | 0.10 | 0.03 | 0.02 | 0.03 | 0.04 |
| $\bullet H \rightarrow b \bar{b}$ | 0.027 | 0.029 | 0.038 | 0.13 | 0.59 | - |
| $\bullet H \rightarrow \tau^{+} \tau^{-}$ | 0.07 | 0.08 | 0.10 | 0.36 | - | - |
| $\bullet H \rightarrow c \bar{c}$ | 0.31 | 0.39 | 0.44 | - | - | - |
| $\bullet H \rightarrow g g$ | 0.16 | 0.18 | 0.23 | - | - | - |
| $\bullet H \rightarrow c \bar{c}+g g$ | 0.15 | 0.16 | 0.20 | - | - | - |

## OTHER HIGGS BRANCHING RATIO STUDIES

| Study | $\sqrt{s} / \mathrm{GeV}$ | $\int d t L / \mathrm{fb}^{-1}$ | Mode | $P\left(e^{-}\right)$ |
| :--- | :--- | :--- | :--- | :---: |
| - H/B/B | 500 | 50 | $Z H$ | 0 |
| - N/K | 300 | 50 | $Z H$ | -0.95 |
| - B | 350 | 500 | $Z H+H \nu \bar{\nu} 0$ |  |
| - B/R | 350 | 500 | $Z H$ | 0 |
| - B/P/I | 500 | 500 | $Z H$ | $\pm 0.8$ |

$H / B / B=M . D$. Hildreth, T.L. Barklow and D.L. Burke, Phys. Rev. Lett., 49, 34411994

N/K=I. Nakamura and K. Kawagoe, in Proceedings of the Workshop on Physics and Experiments with Linear Colliders, vol. II, World Scientific, Singapore 1996.
$B=M$. Battaglia, in Proceedings of the International Workshop on Linear Colliders LCWS99 1999.
$B / R=G$. Borisov and $F$. Richard, in Proceedings of the International Workshop on Linear Colliders LCWS99 1999.
$\mathrm{B} / \mathrm{P} / \mathrm{I}=\mathrm{J}$. Brau, C. Potter and M. Iwasaki, in Proceedings of the Linear Collider Workshop LCWS2000 2000.

## COMPARISON TO OTHER HIGGS BR STUDIES

The fractional branching ratio errors $\delta_{B R} / B R$ from each study are shown in the table below. Here $m_{H}=120$ GeV .

| Mode | $\mathrm{H} / \mathrm{B} / \mathrm{B}$ | $\mathrm{N} / \mathrm{K}$ | B | $\mathrm{B} / \mathrm{R}$ | $\mathrm{B} / \mathrm{P} / \mathrm{I}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| - $H \rightarrow W W^{\star}$ | 0.48 | - | 0.054 | 0.051 | 0.10 |
| - $H \rightarrow b \bar{b}$ | 0.07 | 0.041 | 0.024 | - | 0.029 |
| - $H \rightarrow c \bar{c}$ | - | 0.80 | 0.083 | - | 0.39 |
| - $H \rightarrow g g$ | - | - | 0.055 | - | 0.18 |
| - $H \rightarrow \tau^{+} \tau^{-}$ | 0.14 | 0.15 | 0.06 | - | 0.08 |
| - $H \rightarrow c \bar{c}+g g$ | 0.39 | 0.17 | - | - | 0.16 |

Given the different parameters assumed in each study, such a direct comparison may be misleading.

## CONSISTENCY CHECK

The fractional branching ratio error $\delta_{B R} / B R$ goes like $\left(\sigma \int d t L\right)^{-1 / 2}$. The former divided by the latter is plotted against the latter for the case $m_{H}=120 \mathrm{GeV}$.


Broadly, the results are consistent though there is some discrepancy in the $H \rightarrow c \bar{c}$ and $H \rightarrow g g$ results.

## IMPROVING THE STUDY

By the end of Snowmass 2001, this study should be extended and improved in the following ways:

- Analyze higher Higgs mass cases.
- Confer with other authors to resolve differences in results ( $H \rightarrow c \bar{c}$ and $H \rightarrow g g$ ).
- Consider how to apply this analysis to the light MSSM $h^{0}$ in the decoupling limit.

