Cooperativity and Metal–Linker Dynamics in Spin Crossover Framework Fe(1,2,3-triazolate)$_2$

Anastasia B. Andreeva, Khoa N. Le, Kentaro Kadota, Satoshi Horike, Christopher H. Hendon,* and Carl K. Brozek*

ABSTRACT: Cooperative interactions are responsible for the useful properties of spin crossover (SCO) materials—large hysteresis windows, critical temperatures near room temperature, and abrupt transitions—with hybrid framework materials exhibiting the greatest cooperativity and hysteresis of all SCO systems. However, little is known about the chemical origin of cooperativity in frameworks. Here, we present a combined experimental–computational approach for identifying the origin of cooperativity in the metal–organic framework (MOF) Fe(1,2,3-triazolate)$_2$ (Fe(TA)$_2$), which exhibits the largest known hysteresis window of all SCO materials and unusually high transition temperatures, as a roadmap for understanding the manipulation of SCO behavior in general. Variable-temperature vibrational spectroscopy provides evidence that “soft modes” associated with dynamic metal–linker bonding trigger the cooperative SCO transition. Thermodynamic analysis also confirms a cooperativity magnitude much larger than those of other SCO systems, while electron density calculations of Fe(TA)$_2$ support previous theoretical predictions that large cooperativity arises in materials where SCO produces considerable differences in metal–ligand bond polarities between different spin states. Taken together, this combined experimental–computational study provides a microscopic basis for understanding cooperative magnetism and highlights the important role of dynamic bonding in the functional behavior of framework materials.

INTRODUCTION

Switchable behavior in materials is often designed to be abrupt and reversible, have large “memory” (hysteresis), and are triggerable by stimuli near ambient conditions. Spin crossover (SCO) is a leading example of switchable magnetism that arises from paramagnetic systems in equilibrium between high-spin (HS) and low-spin (LS) electronic configurations.1–4 With stimuli such as thermal energy, light, guest adsorption, or pressure, the equilibria can be reversibly shifted to the magnetic state by influencing the bonding environment of the magnetic center. Relatively low-energy input is required to convert between the spin states in SCO systems because the spin-pairing destabilization energy of the LS state equals the crystal-field destabilization energy of the HS state. As octahedral Fe$^{2+}$ comprises the great majority of SCO systems, it serves as the standard model for explicating key concepts, as follows. Low temperature favors the LS state because $t_2g$ $e_g$ electronic configurations have less metal–ligand antibonding character and hence greater enthalpic stability compared to the $e_g^4$ HS states, while moderate temperatures, often below 300 K, favor the HS state due to its greater vibrational entropy.5,6 Due to the impact of SCO on the electronic properties of the magnetic ions, spectroscopy can be used in addition to magnetic measurements to monitor the SCO process, including electronic absorption and $^{57}$Fe Mössbauer spectroscopy.7 Although molecular SCO complexes typically exhibit gradual spin transitions at temperatures below 300 K without magnetic hysteresis, solid-state SCO systems display abrupt transitions with magnetic hysteresis near room temperature, rendering them more useful for readable “on-off” technology.5 Nearly all solid-state examples are porous frameworks such as the Prussian Blue analogues or the Hofmann-type networks (Fe(L)M(CN)$_4$, L = pyrazine or pyridine, M = Co, Ni, Pd, Pt)$_3$, with Fe(py)$_2$Ni(CN)$_4$ as the seminal example,12 while the largest SCO hysteresis has been observed in the metal–organic framework (MOF) Fe(1,2,3-triazolate)$_2$ (Fe(TA)$_2$), as shown in Figure 1.19 Despite the importance of abrupt and hysteretic spin transitions, the specific chemistry responsible for these long-range phenomena is just beginning to emerge.

Several models20–23 describe “cooperative interactions” as the origin of solid-state SCO behavior and successfully reproduce SCO phenomena, but they generally lack insight into the chemical meaning of such interactions. Despite its ambiguity, cooperativity is a measurable thermodynamic quantity. For example, fitting spin transition equilibrium data of solid systems to a noninteracting model24 meant for

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molecular SCO systems grossly overestimates $\Delta H$ and $\Delta S$ of the spin transition compared to values measured from differential scanning calorimetry. A cooperative interaction parameter $\Gamma$ is thus employed to account for the apparent thermodynamic stabilization of solid-state systems.\cite{28,29,30} Theoretical descriptions of SCO associate $\Gamma$ with vibronic interactions and coupled anharmonic oscillations between neighboring magnetic centers.\cite{21,22,23} Although the dominant effect of $\Gamma$ is to lower $\Delta H$, the large vibrational $\Delta S$ of spin transitions has also been identified as a possible contributor to cooperativity.\cite{21}

Based on our previous work on dynamic metal–linker bonding in MOFs,\cite{28} we hypothesized that vibrational "soft modes" drive the large cooperativity of SCO frameworks, just as they trigger other types of phase changes through coupled lattice dynamics. Specifically, we propose that certain vibrations act as "soft modes" by driving metal–ligand bonds to convert between strong and weak interactions, thereby enabling the huge volumetric expansion from the condensed LS state into the HS form, as shown in Scheme 1a. Recently, we reported that the strong temperature dependence of MOF optical absorption arises in part from this thermally activated dynamic bonding.\cite{29} Furthermore, we propose that this dynamic bonding also serves as the mechanism of both large hysteresis and abrupt transitions of SCO frameworks: the large hysteresis arises from the "expansion pressure" of neighboring HS centers forcing minority LS centers back into the HS state and the vice versa scenario for "compression pressure", causing SCO to occur at lower and higher temperatures, respectively, compared to the expected $T_{1/2}$ for a system without cooperative interactions (Scheme 1b). Dynamic bonding would therefore assist in the reversible bond configurations and coupled motion of neighboring atoms in this mechanism, while also causing the abrupt transitions because as lattice phonons, they drive the collective motion of the entire lattice simultaneously.

Here, we report a combined experimental–computational investigation into the origin of the exceptional SCO cooperativity of Fe(TA)$_2$. Variable-temperature diffuse reflectance infrared vibrational spectroscopy (VT-DRIFTS) provides evidence for dynamic metal–linker bonding in the family of isostructural M(TA)$_2$ materials ($M = Mn, Fe, Co, Cu, Zn$) reminiscent of the "loose–tight" equilibrium phase change observed for conventional carboxylate MOFs.\cite{28} In addition to dynamic bonding, the vibrational spectra of Fe(TA)$_2$ depict hallmark signatures of soft modes at the SCO critical temperature, suggesting a microscopic origin of cooperativity. Thermodynamic analysis of the SCO equilibrium also allows cooperativity to be quantified, revealing an unusually large magnitude that explains the wide magnetic hysteresis. Finally, computational analysis suggests that this large cooperativity arises from the ionic and polarizable bonding inherent to MOF materials and other systems with metal ions bridged by azolates and similar ligands. Compared to other classes of SCO molecules and materials, these results explain why ionically bound networks of metal–organic bridges are uniquely well-suited building blocks for switchable magnetism, while raising fundamental questions concerning the general importance of dynamic bonding in the phase-change behavior of porous materials.

**METHODS**

**Materials.** All commercial chemicals were used as received unless stated otherwise. Copper(II) hydroxide (technical grade, Aldrich), 1H,1,2,3-triazole (>98%, TCI), N,N-dimethylformamide (DMF, ACS grade, Fisher Scientific), ammonium hydroxide (30% NH$_4$OH, ACS grade, Baker), ethanol (EtOH, 100%, Decon), iron(II) chloride (98%, anhydrous, Strem), manganese(II) nitrate tetrahydrate solution (98%, anhydrous, Aesar), zinc(II) chloride (>98%, reagent grade, Sigma-Aldrich), anhydrous cobalt(II) chloride (97%, anhydrous, Afa Aesar), and methanol (MeOH, HPLC grade, Oakwood Chemical). Solvothermal syntheses were conducted in 20 mL scintillation vials charged with stir bars heated in an aluminum dry bath or in a Yamato Convection oven unless stated otherwise.

**Characterization.** Variable-temperature diffuse reflectance infrared Fourier transform (VT-DRIFT) spectra were recorded on a Nicolet 6700 FT-IR spectrometer equipped with a Transmission E.S.P. attachment and a MCT-A detector paired with a Harrick Scientific Praying Mantis Diffuse Reflection (DRP) accessory. Introduction of vacuum and temperature variation was possible with a Harrick Scientific low-temperature reaction chamber (CHC) equipped with UV quartz and 2 Harrick 15 mm × 2 mm potassium bromide windows. To maximize the intensity, all samples were diluted with potassium bromide. Reflectance FT-IR spectra were obtained in the range of 4000–650 cm$^{-1}$ with 0.9820 cm$^{-1}$ resolution and 32 scans. Variable-temperature powder X-ray diffraction (PXRD)
Table 1. Thermodynamic Properties of Spin Crossover Frameworks and Molecules$^{a,b}$

<table>
<thead>
<tr>
<th>name</th>
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<tbody>
<tr>
<td>$\Delta H$ (kJ mol$^{-1}$)</td>
</tr>
<tr>
<td>--------</td>
</tr>
<tr>
<td>Fe(TA)$_2$</td>
</tr>
<tr>
<td>Fe(trz)$_2$(Htrz)$_2$BF$_4$</td>
</tr>
<tr>
<td>Fe(py)$_2$Ni(CN)$_4$</td>
</tr>
<tr>
<td>Fe(py)$_2$Pt(CN)$_4$</td>
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<tr>
<td>Ph(PhMes)$_4$Fe(PPh$_3$)$_2$</td>
</tr>
<tr>
<td>Fe(py)$_2$Ni(CN)$_4$</td>
</tr>
<tr>
<td>Fe(bpac)(Au(CN)$_2$)$_2$</td>
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<tr>
<td>Fe(py)$_2$Ni(CN)$_4$</td>
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<tr>
<td>Fe(pz)Pt(CN)$_4$</td>
</tr>
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</table>

$^a$Calculated average from endothermic and exothermic peaks. $^b$Trz = 1,2,4-triazolato; py = pyridine; pz = pyrazine; bpac = 1,2-bis(4'-pyridyl)acetylene; pbp = 1-propyltetrazole; PhB(MesIm)$_3$Fe = iron(II) phosphoraniminate; phen = 1,10-phenanthroline; PM-Aza = N-2'-pyridymethylen-4-(phenyl)aniline.

patterns were collected under a N$_2$ stream using a BTS 500 high-temperature attachment on a Rigaku MiniFlex with a Cu Kr anode (λ = 1.5418 Å). Air-sensitive [Fe(TA)$_2$] was packed in the attachment inside an Ar-filled glove box. The PXRD patterns were indexed, and the obtained cell parameters were refined by the Le Bail method using EXPo2014.\textsuperscript{30} Linear coefficients of thermal expansion (CTE) were calculated from the cell lengths and temperatures as summarized in Table S1. Differential scanning calorimetry (DSC) was performed on a TA Instruments Differential Scanning Calorimeter (DSC Q2000).

**Equilibrium Model and Fitting Parameters.** The equilibrium model explores whether the metal–nitrogen red shifts arise from temperature-dependent intensities of two overlapping bands. Supposing an equilibrium is present as $A = \nu A + B$ with $K_{eq} = |B|/|A|$, we assume $A$ to be a "tight" M–N state with vibrational energy $\nu_A$ and $B$ to be a "loose" state with variable energy $\nu_B$ where $\nu_A > \nu_B$. Rather than describing two specific metal–nitrogen configurations, the two states represent ensembles of configurations in shallow potential energy surfaces that appear more tight or loose. Therefore, the equilibrium will shift to the "loose" state at higher temperatures. Since $\nu_A > \nu_B$ statistically, a red shift should be observed. Using $\nu_A$ and $\nu_B$ to denote the mole fraction of $A$ and $B$, $x_A = 1/(1 + K_{eq})$ and $x_B = K_{eq}/(1 + K_{eq})$. Similarly, we define the apparent peak position to be $x_A\nu_A + x_B\nu_B$ at $T_H$ and $x_A\nu_A + x_B\nu_B$ at $T_C$. After substituting $K_{eq} = \exp[-AG'/RT]$, we get an expression for the red shift as a function of temperature that is fundamentally equivalent to the Boltzmann expressions in the Morse and cross-anharmonicity models. Using a global fitting procedure, we extract $\nu_A$ and $\nu_B$ from our experimental data and assume that all the peaks at each temperature can be deconvoluted into the sum of two Gaussian peaks $A$ and $B$.

**Computational Methods.** Structural relaxation for all structures was performed with DFT calculations as implemented in the Vienna Ab initio Simulation Package (VASP, version 5.4.4).\textsuperscript{31} All calculations were performed with a plane-wave cut off at 500 eV and the unrestricted GGA-PBEsol exchange–correlation functional.\textsuperscript{32} The band gap was optimized to be 0.005 eV A$^{-1}$ and the electronic convergence criterion was set to $10^{-8}$ eV. The automatic k-grid used for all optimizations was $3 \times 3 \times 3$. Symmetry was not enforced for these calculations. The optimized room temperature (RT) structures of the Zn, Co, and Mn analogues were obtained by spin-polarized calculations. The high-temperature structures were obtained by expanding the cells and then optimized by spin-polarized calculations with restricted changes in the cell volume and shape. The Fe analogues were obtained by similar methods as above, but for the RT structure, the spin moments on all Fe atoms were set to 0, and for the HT structures, the spin moment for each Fe atom was set to 4. Similarly, for the Cu analogue, the spin moment for RT and HT were set to match the experimentally reported data.\textsuperscript{33} Energy profiles for all structures were obtained by a similar technique where the unit cell is compressed and expanded from optimized ground-state structures and then reoptimized with restricted change in the cell shape and volume.

Vibrational frequency calculations were obtained via the finite difference method (FDM) as implemented in VASP where zone-center (Γ-point) frequencies were calculated. The calculations were carried out with the unrestricted GGA-PBEsol exchange–correlation functional and with similar convergence criteria as relaxation calculations. Electronic properties for all systems were obtained from single-point calculations at the Γ-point with the HSEsol06 functional.\textsuperscript{34}

**RESULTS AND DISCUSSION**

Table 1 summarizes the key thermodynamic parameters for a representative collection of SCO molecules and frameworks. Entries 1–7 are solid-state networks and 8–11 are molecules. The critical temperature ($T_{1/2}$) at which HS and LS populations become equal (50:50) clearly distinguishes between each class of the SCO system, with molecules exhibiting the lowest temperatures and MOFs the highest. This temperature is governed by $\Delta H/\Delta S$ because $\Delta G = 0$ at this condition, such that the differences between the $T_{1/2}$ values mostly arise from differences in $\Delta H$. Solid-state systems (entries 1–7) also display a hysteresis with two critical temperatures ($T_{\text{h}}$ heating and $T_{\text{c}}$ cooling). Both the hysteresis and higher $T_{1/2}$ values have been attributed to cooperative interactions present in covalent and ionic solids that are largely absent in molecular crystals since they feature only weak intermolecular forces between isolated molecules. Although Prussian Blue and Hofmann-type frameworks resemble MOFs, $T_{\text{heating}}$ and $T_{\text{cooling}}$ of Fe(TA)$_2$ are approximately twice as high with a ten-times wider hysteresis window.

To identify the origin of the unexpected SCO behavior of Fe(TA)$_2$ and its relation to cooperativity, we investigated the...
dynamic bonding of $M(TA)_2$ frameworks. Bulk powder XRD of $Fe(TA)_2$ was obtained by the original Yaghi et al. method. Briefly, $FeCl_2$ was combined with 1,2,3-triazole in DMF under air-free conditions and heated to $120^\circ C$, affording a pink solid, with PXRD analysis confirming the phase purity (Figure S22). The related isostructural frameworks with Mn, Co, and Zn were also prepared according to the original report by Yaghi et al. while the Cu material was prepared by the Volkmer procedure. To explore whether $M(TA)_2$ frameworks engage in the same “loose−tight” dynamic bonding equilibrium as carboxylate MOFs, VT-DRIFT spectra were recorded between 173 and 623 K under dynamic vacuum. In Figure 2a the 173 K (LS) and 623 K (HS) spectra of $Fe(TA)_2$ are plotted with computed vibrational transitions of both HS and LS materials (Figure 2b), showing a good overall agreement. As expected for two different phases, the LS and HS spectra show considerable differences, with several bands disappearing and new bands appearing with decreased temperature (Figure 2a). This effect is also apparent in the different expected bands from the calculated phonon modes. Figure 2a,b highlights vibrations labeled X, Y, and Z that persist with temperature, which, as calculations suggest, involve triazolate-based stretches. Interestingly, vibration X, centered at around 1230 cm$^{-1}$, displays temperature dependence whereas Y and Z do not. Figure 2c plots the baseline-subtracted spectra of vibration X for $Fe(TA)_2$ during a cooling cycle. Although carboxylate MOFs exhibit carboxylate stretches that red-shift linearly at higher temperatures, close inspection indicates that this triazolate mode exhibits both red- and blue-shifts with temperature.

Figure 3 plots the peak maxima of vibration X in $Fe(TA)_2$ during a heating cycle, revealing a red-shift−blue-shift inflection centered at $T_{heating}$. While Figure 3b shows a similar trend centered at $T_{cooling}$ during a cooling cycle. A red-shift−blue-shift inflection is hallmark evidence of the special class of vibrations known as soft modes that trigger phase transitions by pushing the atomic positions from one phase to the positions of another. As the material approaches the $T_c$ of a phase transition, soft modes impart increasing amounts of energy to the surrounding lattice through coupled anharmonic oscillations. As a result, the soft mode red-shifts in the frequency because the vibration loses energy to the lattice.
undergoing a phase change. Beyond \(T_c\), however, the soft mode blue-shifts toward its new frequency in the new phase.\(^{43,44}\) Previously, we demonstrated red-shifting carboxylate stretches in carboxylate MOFs and proposed that they arise from metal–carboxylate bond weakening and equilibrium between “tight” and “loose” conformations. Although a blue shift was not observed in these studies, we hypothesized that just as weaker metal–carboxylate binding would lead to lower-frequency C–O stretches by increasing the antibonding electron density in the C–O bond vector, weaker metal–triazolate bonding at higher temperatures would produce lower-frequency triazolate stretches. These results strongly suggest that Fe(TA)\(_2\) exists in equilibrium between species with strong and weak metal–triazolate bonding, but the microscopic origin remained unclear because both SCO and “loose–tight” transitions could give rise to weaker bonding.

For obtaining thermodynamic insight into the origin of the “strong–weak bonding” equilibrium of Fe(TA)\(_2\), van’t Hoff analysis was performed on the equilibrium constants \(K\) determined from the population fitting of vibration X, where \(K = [\text{weak}] / [\text{strong}]\). Figure 4b plots \(K\) versus temperature for Fe(TA)\(_2\) recorded during a cooling cycle just after the HS-to-LS transition. Because [weak] and [strong] are present in equal proportions (\(K = 1\)) at around 350 K, these data suggest that “tight–loose” equilibrium contributes to bond weakening at these temperatures. If SCO is the cause, \(K = 1\) would occur at a \(T_{\text{cooling}}\) of 465 K. The absence of an obvious HS–LS equilibrium at these temperatures is also consistent with the unusually abrupt SCO of Fe(TA)\(_2\), which arises from large changes in equilibrium ratios of LS and HS species in a narrow temperature range around \(T_{1/2}\).

Figure 4. Equilibrium analysis of vibrational mode “X” in Fe(TA)\(_2\). Data collected during a cooling cycle. (a) Baseline-subtracted spectra fitted to two species at fixed positions indicated by vertical dashed lines and (b) van’t Hoff analysis of equilibrium constants \(K = [\text{loose}] / [\text{tight}]\) versus temperature. The values of [tight] and [loose] were determined from the relative integrated intensities of the high-frequency (blue) and low-frequency (red) species.

To determine whether Fe(TA)\(_2\) engages in a “tight–loose” equilibrium in addition to SCO behavior, we investigated the Mn, Co, Cu, and Zn analogues by VT-DRIFTS. Figure 5 shows the spectra of all materials collected between 173 and 623 K. Although Fe(TA)\(_2\) displays a single temperature-dependent vibration, the non-SCO analogues exhibit several temperature-dependent bands, which, as calculations suggest, possess a triazolate character (Figures S26–30). Unlike Fe(TA)\(_2\), these bands only red-shift at higher temperatures. Although all spectra appear qualitatively similar, we focused our investigation on a single phonon mode in all materials indicate fatigue in the crystalline lattice, as has been observed previously in SCO solids.\(^{45,46}\)
around 1180 cm$^{-1}$, which also appears as the only temperature-dependent mode (vibration X) in Fe(TA)$_2$. As shown in Figure 5b,d,f, the peak maxima of this mode in Mn(TA)$_2$, Co(TA)$_2$, and Zn(TA)$_2$ linearly red-shift at higher temperatures with slopes of around $-0.01$ cm$^{-1}$ K$^{-1}$, which are half as steep as those in Fe(TA)$_2$. Shallow slopes could arise from...
systems with either less dynamic bonding or from equilibria between species with similar vibrational frequencies, such as ensembles of metal–ligand conformations with degenerate potential energies. Because these slopes are smaller than the χ measured for carboxylate MOFs, we expect that they arise from stronger and less dynamic metal–nitrogen bonding. Unlike the Mn, Co, and Zn analogues, Cu(TA)2 undergoes a phase transition from tetragonal-to-cubic symmetry.33 Interestingly, the peak maximum of Cu(TA)2 during the warming cycle exhibits a red-shift—blue-shift inflection at the critical temperature (Figure 5h), suggesting that this vibration also serves as a soft mode for Cu(TA)2. Population analysis of this mode in the Mn, Co, Cu, and Zn analogues also supports the presence of two-state equilibria (Figures S6−16), strongly suggesting that M(TA)2 materials undergo a “tight−loose” equilibrium even in the absence of SCO. Interpreting these fits in terms of “tight−loose” ensembles affords conventional 300 K formation constants (Kf = [tight]/[loose]) of all M(TA)2 materials.

Table 2. Thermal Expansion Coefficients (TEC), Red-Shifted Slopes (χ), Stability Constants (ln(Kf)), and Loose−Tight Thermodynamic Parameters of M(TA)2.

<table>
<thead>
<tr>
<th>MOF</th>
<th>TEC (10−6 K−1)</th>
<th>slope (cm−1 K−1)</th>
<th>stability constants</th>
<th>ΔH (kJ mol−1)</th>
<th>ΔS (J K−1 mol−1)</th>
<th>Cp (J K−1 mol−1)</th>
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</thead>
<tbody>
<tr>
<td>Fe(TA)2-LS</td>
<td>51.2[ca]</td>
<td>−0.020(0)[ca]</td>
<td>−0.016(0)</td>
<td>1.74</td>
<td></td>
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<tr>
<td>Fe(TA)2-HS</td>
<td>56.0</td>
<td>−0.035(2)</td>
<td></td>
<td>14.5</td>
<td>39.6</td>
<td>119.7</td>
</tr>
<tr>
<td>Cu(TA)2-LT</td>
<td>32.9[ca]</td>
<td>−0.023(5)[ca]</td>
<td>−0.014(1)</td>
<td></td>
<td></td>
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</tr>
<tr>
<td>Cu(TA)2-HT</td>
<td>1.0[ca]</td>
<td>−0.046(0)[ca]</td>
<td>−0.026(4)</td>
<td>1.97</td>
<td>8.393</td>
<td>17.1</td>
</tr>
<tr>
<td>Co(TA)2</td>
<td>15.2[ca]</td>
<td>−0.017(2)</td>
<td>1.09</td>
<td>7.979</td>
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<td>68</td>
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<tr>
<td>Mn(TA)2</td>
<td>20.2[ca]</td>
<td>−0.013(1)</td>
<td>0.67</td>
<td>6.841</td>
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<td>Zn(TA)2</td>
<td>30.6[ca]</td>
<td>−0.017(7)</td>
<td>0.91</td>
<td>5.605</td>
<td>24.8</td>
<td>196.1</td>
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</table>

“LS = low-spin state. HS = high-spin state. LT = low-temperature phase. HT = high-temperature phase. [a] obtained from a heating cycle.

Figure 6. Total energies of geometry-optimized structures versus metal–triazolate bond lengths of (a) Mn(TA)2, Co(TA)2, Zn(TA)2, and (b) Cu(TA)2. Filled circles correspond to ground-state structures.
Figure 7. Total energies of geometry-optimized Fe(TA)$_2$ structures versus Fe-triazolate bond lengths. Calculations were performed at 0 K.

Figure 8. Cooperativity ($\Gamma$) determined from eq 1 versus temperature for Fe(TA)$_2$. (a) Cooperativity calculated from the heating cycle magnetic susceptibility data. (b) Cooperativity determined from cooling cycle data.

Comparing ln($K_f$) values, as summarized in Table 2, indicates that the non-phase-change materials (Mn, Co, and Zn) possess the most dynamic bonding. van’t Hoff analysis of the Mn, Co, Cu, and Zn analogues (Figures S17–S20) produces $\Delta H$ and $\Delta S$ comparable to carboxylate MOFs, but with considerably larger $\Delta C_p$ (Table 2). Notably, the $\Delta H$ and $K_f$ are the smallest for the Mn and Zn analogues, consistent with the labile bonding expected for these ions lacking crystal-field stabilization energies. Comparatively, the $\Delta H$ and $\Delta S$ values of Fe(TA)$_2$ are approximately twice as large as the other analogues, but they are smaller than the SCO parameters (Table 1), suggesting that they arise from a “tight–loose” rather than SCO equilibrium. Nevertheless, the larger thermodynamic parameters and the presence of only a single soft mode for Fe(TA)$_2$ imply that it proceeds through a markedly different equilibrium process. We propose that vibrations X, Y, and Z red-shift in M(TA)$_2$ materials where only the “tight–loose” equilibrium is relevant, whereas only mode X red-shifts in Fe(TA)$_2$ because it acts as the soft mode driving a separate, competing equilibrium, i.e., the low-spin-to-high-spin phase change. In other words, mode X red-shifts in Fe(TA)$_2$ because it acts as a soft mode to drive SCO, whereas modes X, Y, and Z red-shift in the other materials as a consequence of weakened metal–ligand interactions caused by dynamic bonding.

To further understand the dynamic bonding of M(TA)$_2$ materials, we computed the energies of different metal–ligand conformations. Figure 6 plots the energies of Mn(TA)$_2$, Co(TA)$_2$, Zn(TA)$_2$, and Cu(TA)$_2$ geometries with metal–ligand bond distances that were systematically altered. These “equation of state” diagrams result from uniformly compressing or elongating the entire unit cell volumes and allowing geometries to relax. Energies reflect only enthalpy since the calculations correspond to 0 K. Each data point therefore corresponds to an equilibrium geometry with variable metal–ligand distances. These diagrams are therefore analogous to single-configurational or “reaction” coordinate diagrams. In support of the presence of “tight–loose” equilibria, numerous conformations are accessible through ambient thermal energy, which is indicated by horizontal lines as 1 kcal mol$^{-1}$. These calculations also reproduce the tetragonal-to-cubic phase change of Cu(TA)$_2$ and demonstrate that both phases possess nearly degenerate conformations that would give rise to “tight–loose” equilibria and red-shifted $\chi$.

Metal–ligand bond distances could be quantified as a function of temperature by experimentally measuring the thermal expansion coefficients (TECs) of all materials. Analysis of high-resolution powder X-ray diffraction patterns (Figures S21–S24) afforded TECs summarized in Table 2. All TECs resemble values determined for conventional carboxylated MOFs showing values of around 10$^{-6}$ K$^{-1}$, except MOF-5 and HKUST-1, which display negative TECs due to a structural mechanism that likely arises from dynamic bonding. The larger TEC parameters for Fe(TA)$_2$ and Cu(TA)$_2$ are consistent with the large volume changes resulting from their phase changes. With experimental TECs, the corresponding metal–ligand conformations could be identified at each temperature. For example, comparing 173 and 623 K geometries, the metal–triazolate bond distances of Mn(TA)$_2$ shift from 1.94 to 1.95 Å, Co(TA)$_2$ from 1.97 to 1.98 Å, Cu(TA)$_2$ from 1.99 to 2.01 Å, and Zn(TA)$_2$ from 2.15 to 2.16 Å. Taken together, these experimental and computational results support the presence of dynamic metal–ligand bonding in the general family of M(TA)$_2$ frameworks.

To understand the relationship between “tight–loose” and SCO behavior in Fe(TA)$_2$, we investigated the energies of iron–triazolate conformations as a function of temperature. Figure 7 plots the energies of LS (blue) and HS (red) Fe(TA)$_2$ conformations with varying iron–nitrogen bond distances. These calculations reproduce the experimental ground-state geometries (filled circles) and the experimentally determined $\Delta H$ with high accuracy: the energetic difference between the LS and HS energy curves produces a $\Delta H$ of 31.1 kJ mol$^{-1}$, in
excellent agreement with 31.2 kJ mol\(^{-1}\) measured by differential scanning calorimetry (Figure S25). The presence of nearly degenerate iron–nitrogen conformations within ambient thermal energy also corroborates the ability of Fe(TA)\(_2\) to engage in dynamic bonding. As indicated in Figure 7, the TECs imply that metal–ligand bonds in the LS phase could elongate from 1.91 to 1.93 Å at 583 K prior to SCO. Although the relative energies of the LS and HS curves shift with increased temperature due to entropy, these results suggest that SCO may be enabled by the weakening of iron–nitrogen interactions through dynamic bonding in the LS phase. In other words, vibrational soft modes might serve as the microscopic origin of the unusual SCO cooperativity of Fe(TA)\(_2\).

For quantitative analysis of cooperativity (\(\Gamma\)) in Fe(TA)\(_2\), previously reported magnetic susceptibility data\(^{19}\) were interpreted in terms of the Slichter–Drickamer model, as outlined in eq 1.\(^2\) Figure 8 plots \(\Gamma\) versus temperature for both cooling and heating cycles by using experimental values for \(\Delta H\) and \(\Delta S\) and magnetic susceptibility data to determine \(n_{HS}\), the fraction of HS species at each temperature point. In both cycles, \(\Gamma\) becomes infinite at \(T_c\) and levels at large values approximately between 10 and 20 kJ mol\(^{-1}\). A few studies, if any have quantified the value of \(\Gamma\) in SCO frameworks even though they exhibit the largest cooperativity. Most reports on \(\Gamma\) have focused on molecular crystals with weak intermolecular interactions, giving \(\Gamma\) values between 1 and 5 kJ mol\(^{-1}\).\(^{51}\) A \(\Gamma\) value of 20 kJ mol\(^{-1}\) corresponds to a thermal energy of 2400 K, which is consistent with early predictions\(^{21}\) that abrupt SCO transitions arise when \(\Gamma > k_B T_c\). Given the \(T_{heating}\) and \(T_{cooling}\) of 582 K and 465, respectively, \(\Gamma\) would correspond to a \(k_B T_c\) of roughly 4–5. This analysis, therefore, provides quantitative evidence of the unusually large SCO cooperativity of Fe(TA)\(_2\).

With numerical support for large cooperativity and evidence that it relates to vibrational soft modes, we sought deeper microscopic insight into its origin in Fe(TA)\(_2\). Previous theoretical reports contended that cooperativity arises from fluctuations in the Madelung field of a SCO material. According to this model, the greater the difference in the electrostatic interactions between the LS and HS states, the greater the energetic driving force (cooperativity) for magnetic centers to drive each other through the spin transition. Quantitatively, the magnitude of cooperativity depends directly on the difference in the metal–ligand bond polarizations \(\Delta \delta V\) and the electron density distributions \(\Delta q\) of the LS versus HS states,\(^{52}\) i.e., \(\Gamma = \Delta q \times \Delta \delta V\). To explore the ability of this model to account for the large \(\Gamma\) in Fe(TA)\(_2\), we calculated \(\Delta q\) for both Fe(TA)\(_2\) and a related molecular crystal of [Fe(ptz)\(_6\)][BF\(_4\)]\(_2\) (ptz = 1-propyltetrazolate). Figure 9a shows the increased (red) and decreased (blue) \(\Delta q\) of both systems in the HS state relative to the LS states. In both systems, electron density shifts away from the metal–ligand bonding orbitals toward the ligand accepting orbitals. Additionally, inspection of the metal centers indicates rearrangement of electron density within the d-orbitals, as expected for a spin transition. For quantitative comparison of \(\Delta q\), Figure 9b plots \(|\Delta q|\) as a histogram. Although Fe(TA)\(_2\) shows slightly higher changes in the electron density on the Fe centers, it
hysteresis windows at higher temperatures and more abrupt SCO particles, where large domain sizes exhibit larger driving SCO might also explain the strong size dependence of unique SCO behavior. The importance of dynamic bonding in polarizability, cooperativity is especially strong, leading to a linker interactions that engage in dynamic bonding with high electron density along the metal−ligand unit. Compared to other molecular and solid-state SCO materials, we propose that MOFs occupy a perfect middle-ground state between the weak intermolecular interactions of molecular crystals and the strong covalent bonding of conventional semiconductors. Due to ionic metal−linker interactions that engage in dynamic bonding with high polarizability, cooperativity is especially strong, leading to a unique SCO behavior. The importance of dynamic bonding in driving SCO might also explain the strong size dependence of SCO particles, where large domain sizes exhibit larger hysteresis windows at higher temperatures and more abrupt transitions. Specifically, we expect greater bond dynamics in smaller particles due to their more flexible structures, thereby permitting SCO with less thermal energy compared to large domain sizes.

■ CONCLUSIONS
In conclusion, VT-DRIFTS provides evidence for both dynamic metal−linker bonding in the family of M(TA)2 MOFs and hallmark signatures of soft modes at the SCO temperature of Fe(TA)2. These results suggest that the unusual SCO cooperativity of Fe(TA)2 derives from the particularly dynamic vibrations of MOFs, in general. Modeling magnetic susceptibility data allows quantification of cooperativity, affording energetic values several orders of magnitude larger than that reported for nonframework systems. To identify the origin of this large cooperativity, computational analysis of electron density in the HS and LS Fe(TA)2 structures was performed, revealing a much larger difference across metal−linker bonds compared to molecular analogues. As predicted by previous theoretical studies, such considerable changes in bond polarization, as induced by collective vibrations, trigger fluctuations in the Madelung fields thereby electrostatically stabilizing spin transitions. These results, therefore, provide a microscopic mechanism and quantitative analysis of SCO cooperativity for outlining the general design of materials with cooperative magnetism.

■ ASSOCIATED CONTENT

Supporting Information
The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.chemmater.1c03143.

Experimental materials and characterization details; MOF syntheses; VT-DRIFTS of Fe(TA)2 (S1), Cu(TA)2 (S2), Mn(TA)2 (S3), Co(TA)2 (S4), and Zn(TA)2 (S5); equilibrium model and fitting description; population plots of Fe(TA)2 (S6), subtracted reflectance and population plots of Cu(TA)2 (S7–S10), Mn(TA)2 (S11 and S12), Co(TA)2 (S13 and S14), and Zn(TA)2 (S15 and S16); van’t Hoff analysis from the cooling cycle data of Cu(TA)2 (S17), Mn(TA)2 (S18), Co(TA)2 (S19), and Zn(TA)2 (S20); tabulated cell parameters (Table S1) and VT-PXRD data of Mn(TA)2 during the heating cycle (S21), Fe(TA)2 during the heating cycle followed by cooling (S22), Co(TA)2 during the heating cycle (S23), and Cu(TA)2 during the heating cycle (S24); DSC data of Fe(TA)2 (S25); computational methods and simulated vibrational spectra overlayed with VT-DRIFT spectra transformed with the Kubelka−Munk function followed by tabulated frequencies of expected vibrational modes in Fe(TA)2 (S26, Table S2), Cu(TA)2 (S27, Table S3), Mn(TA)2 (S28, Table S4), Co(TA)2 (S29, Table S5), and Zn(TA)2 (S30, Table S6) (PDF)

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Notes
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