

Your Name: \_\_\_\_\_

1. Compute  $\int 6x^{-2} - 12x^{-1} + 8 \, dx$

2. Find the particular solution to the differential equation  $\frac{dy}{dx} = e^{5x} + 3\sqrt{x}$ , where  $y = \frac{6}{5}$  when  $x = 0$ .

3. Find a general solution to the differential equation  $3t \cdot \frac{dx}{dt} = x^{-2}$ .

4. Verify that  $y = e^{-3x} + e^x$  is a solution to the differential equation  $y'' = 3y - 2y'$ .

5. According to Robert Solow's economic theory, when a portion of all output is reinvested in capital, the rate of change in capital stock,  $K$  (in thousands of dollars), can be written in terms of capital stock and time  $t$  years from now by the differential equation

$$\frac{dK}{dt} = Se^{bt}K^{1-a},$$

where  $a$ ,  $b$ , and  $S$  are all positive constants. Given  $K(0) = 1600$ ,  $a = 0.5$ ,  $b = 0.02$ , and  $S = 2$ , find **and interpret including units** the value of  $K(5)$ . [Hint: in your solution choose the less negative option for the constant]