### The International Linear Collider A Global Project

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The International Linear Collider (ILC) is now under consideration as the next global project in particle physics. In this report, we review of all aspects of the ILC program: the physics motivation, the accelerator design, the run plan, the proposed detectors, the experimental measurements on the Higgs boson, the top quark, the couplings of the W and Z bosons, and searches for new particles. We review the important role that polarized beams play in the ILC program. The first stage of the ILC is planned to be a Higgs factory at 250 GeV in the centre of mass. Energy upgrades can naturally be implemented based on the concept of a linear collider. We discuss in detail the ILC program of Higgs boson measurements and the expected precision in the determination of Higgs couplings. We compare the ILC capabilities to those of the HL-LHC and to those of other proposed  $e^+e^-$  Higgs factories. We emphasize throughout that the readiness of the accelerator and the estimates of ILC performance are based on detailed simulations backed by extensive R&D and, for the accelerator technology, operational experience.

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### 1. INTRODUCTION

While the Standard Model (SM) is a highly successful theory of the fundamental interactions, it has serious shortcomings. New fundamental interactions are required to address them. A central focus of particle physics now involves searching for these new interactions and associated new particles. The SM is theoretically self-consistent, but it does not answer many obvious questions about particle physics. It has no explanation for the dark matter or dark energy that is observed in the cosmos, or for the cosmic excess of matter over antimatter. It does not address the mass scale of quarks, leptons, and gauge bosons, which is significantly lower than the Planck scale. It does not explain the large mass ratios among the SM particles or the values of the quark and neutrino mixing angles. These and other considerations provide a compelling motivation for new interactions beyond the SM. On the other hand, the current success of the SM indicates that further search will be very challenging and, most likely, requires new approaches and new methods.

The discovery of the Higgs boson in 2012 revealed the final particle predicted in the SM. Within that theory, the Higgs boson is the agent for electroweak symmetry breaking and the generation of the masses of all elementary particles. Thus, it occupies a central role in the SM and, specifically, in many of the unresolved issues that we have listed above. The properties of the Higgs boson are precisely specified in the SM, while models of new interactions that address these issues lead to significant corrections to those predictions. Thus, high-precision measurement of the Higgs boson offers a new and promising avenue for searches for new physics beyond the Standard Model. The discovery of deviations of the Higgs boson properties from the SM predictions could well provide the first evidence for new physics beyond the SM.

This study of the Higgs boson properties is the most prominent goal of the International Linear Collider (ILC). The ILC has been designed with this goal in mind. to provide a complete, high-precision picture of the Higgs boson and its interactions. Though the properties of the Higgs boson are already being studied at the LHC, the ILC offers significant advantages. It will bring the measurements to a new, qualitatively superior, level of precision, and it will remove the many model-dependent assumptions required for the analysis of the Higgs boson measurements at hadron colliders. The ILC will be highly sensitive to Higgs boson decays that yield invisible or other exotic final states, giving unique tests of models of new weakly interacting particles and dark matter. The ILC can also probe for direct pair-production of particles with very weak interactions. Since direct searches at high-energy hadron colliders have not discovered new particles, it is urgent and compelling to open this new

path to the search for physics beyond the SM.

As an  $e^+e^-$  linear collider, the ILC brings a number of very powerful experimental tools to bear on the challenge of producing a precise, model-independent accounting of the Higgs boson properties. The ILC has a well-defined, adjustable centre-of-mass energy. It produces conventional SM events at a level that is comparable to, rather than overwhelmingly larger than, Higgs signal processes, allowing easy selection of Higgs boson events. At its initial stage of 250 GeV, Higgs boson events are explicitly tagged by a recoil Z boson. At a linear collider, both the electron and positron beams can be polarized, introducing additional observables. Because all electroweak reactions at energies above the Z resonance have order-1 parity violation, beam polarization effects are large and provide access to critical physics information.

After operation of a linear collider at the starting energy, it is straightforward to upgrade the centre-of-mass energy. This is the natural path of evolution for a new high-energy physics laboratory. An upgrade in energy systematically expands the list of physics processes that can be studied with high precision and polarized beams. An upgrade to 500 GeV accesses the Higgs boson coupling to the top quark and the Higgs boson self-coupling. Together with the 250 GeV results, this will give a complete accounting of the Higgs boson profile. An energy upgrade to 350 GeV begins the use of the ILC as a top quark factory, offering precision measurements of the top quark mass and electroweak couplings. At the same time, the ILC will study the reactions  $e^+e^- \to f\bar{f}$  and  $e^+e^- \rightarrow W^+W^-$  with high precision. Here also, deviations from the SM predictions can indicate new physics. Finally, the ILC will search directly for pair production of weakly coupled particles with masses up to half the centre-of-mass energy, without the requirement of special signatures needed for searches at hadron colliders. Because of its upgrade capability and the unique access that  $e^+e^-$  beams give to many important reactions, the ILC will continue to be a leading discovery machine in the world of particle physics for decades.

The ILC is mature in its design and ready for construction. The technology of the ILC has been advanced through a global program coordinated by the International Committee for Future Accelerators (ICFA). In the mid-1990's, various technology options to realise a highenergy linear collider were emerging. ICFA asked the Linear Collider Technical Review Committee to develop a standardised way to compare these technologies based on their parameters, such as power consumption and luminosity. A second review panel was organised by ICFA in 2002; it concluded that both warm and cold technologies had developed to the point where either could be the basis for a high energy linear collider. In 2004, the International Technology Review Panel (ITRP) was charged by ICFA to recommend an option that could focus the worldwide R&D effort. This panel chose the superconducting radiofrequency technology (SCRF), in a large part due to its energy efficiency and potential for broader

applications.

Today's design of the ILC accelerator is the result of nearly twenty years of R&D that has involved a broad, global community. The heart of the ILC, the SCRF cavities, is based on pioneering work of the TESLA Technology Collaboration. Other aspects of the technology emerged from the R&D carried out for the competing linear collider projects JLC/GLC and NLC, which were based on room-temperature accelerating structures. The ILC proposal is supported by extensive R&D and prototyping. The successful construction and operation of the European XFEL (E-XFEL) at DESY provides confidence both in the high reliability of the basic technology and in the reliability of its performance and cost in industrial realisation. Other communities acknowledge this; the SCRF technology has also been chosen for new free electron laser projects now under construction in the US and China. Some specific optimisations and technological choices remain. But the ILC is now ready to move forward to construction.

The effort to design and establish the technology for the linear collider culminated in the publication of the Technical Design Report (TDR) for the International Linear Collider (ILC) in 2013 [1]. Twenty-four hundred (2400) scientists, from 48 countries and 392 institutes and university groups, signed the TDR. This document presented optimised collider and detector designs, and associated physics analyses based on their expected performance. From 2005 to the publication of the TDR, the design of the ILC accelerator was conducted under the mandate of ICFA as a worldwide international collaboration, the Global Design Effort (GDE). Since 2013, ICFA has placed the international activities for both the ILC and CLIC projects under a single organisation, the Linear Collider Collaboration (LCC).

With knowledge of the mass of the Higgs boson, it became clear that the linear collider could start its ambitious physics program with an initial centre-of-mass energy of 250 GeV at a cost reduced from the TDR. A revised design of the ILC, the ILC250, was thus presented [2]. This design retains the final-focus and beamdump capability to extend the centre-of-mass energy to energies as high as 1 TeV. Advances in the theoretical understanding of the impact of precision measurements at the ILC250 have justified that the 250 GeV operating point already gives substantial sensitivity to physics beyond the SM [3, 4]. The cost estimate for ILC250 is similar in scale to that of the LHC.

In its current form, the ILC250 is a 250 GeV centreof-mass energy (extendable up to a 1 TeV) linear  $e^+e^$ collider, based on 1.3 GHz SCRF cavities. It is designed to achieve a luminosity of  $1.35 \cdot 10^{34}$  cm<sup>-2</sup>s<sup>-1</sup> and provide an integrated luminosity of 400 fb<sup>-1</sup> in the first four years of running. The scenario described in Section III gives a complete program of  $2 \text{ ab}^{-1}$  of data at 250 GeV over 12 years. The electron beam will be polarised to 80%, and the baseline plan includes an undulator-based positron source which will deliver 30% positron polarisation.

The experimental community has developed designs for two complementary detectors, ILD and SiD. These detectors are described in [5]. They are designed to optimally address the ILC physics goals, with complementary approaches. One detector is based on TPC tracking (ILD) and one on silicon tracking (SiD). Both employ particle flow calorimetry based on calorimeters with unprecedented fine segmentation. Extensive R&D and prototyping gives confidence that the unprecedented levels of performance in calorimetry, tracking, and particle identification required to achieve the physics programme can be realised. The extensive course of prototyping justifies our estimates of full-detector performance and cost. The detector R&D program leading to these designs has contributed a number of advances in detector capabilities with applications well beyond the linear collider program. Similarly to the situation for the collider, some final optimizations and technology choices will need to be completed in the next few years.

There is broad interest in Japan to host the international effort to realise the ILC project. This interest has been growing over many years. Political entities promoting the plan to host the ILC in Japan include the Federation of Diet Members for ILC and the Advanced Accelerator Association, a consortium of industrial representatives that includes most of the large high-tech companies in Japan. The ILC has been endorsed by the community of Japanese particle physicists (JAHEP) [6]. Detailed review in Japan of the many aspects of the project is nearing a conclusion. Since 2013 the MEXT ministry has been examining the ILC project in great detail, including the aspect of risk minimisation. This review concluded when MEXT's ILC Advisory Panel released its report [7] on July 4, 2018, summarising the studies of the several working groups (WG) that reviewed a broad range of aspects of the ILC. The most recent studies include a specific review of the scientific merit and the technical design for the ILC250. The Physics WG scrutinised the scientific merit of the ILC250, leading to their strong and positive statement on the importance of the ILC250 to measure precisely the couplings of the Higgs boson [7]. The TDR WG reviewed issues addressed in the Technical Design Report and the ILC250 design, including the cost estimate and technical feasibility. Other working groups of the MEXT review commented on manpower needs, organisational aspects, and the experience of previous large projects. The report of the ILC Advisory Panel was followed by the beginning of deliberations in a committee and technical working group established by the Science Council of Japan (SCJ), the second stage of the review process. The SCJ released its review on December 19, 2018 [8]. The review concluded that "the research topic of precise measurement of Higgs couplings is extremely important" but expressed doubts about the cost of the project, which is well beyond the costs of proposals brought forward by chemists and biologists. The financing of the project will depend on negotiations with international partners, led by the Japanese government

after a clear statement of interest. The Japanese government is now preparing for this step, which can be followed by a move to the next phase of international negotiations. A new independent committee (LDP Coordination Council for the Realization of ILC), led by high-ranking members of the Liberal Democratic Party, the majority party in the Diet, has now convened to encourage the national government along this path.

Given a positive signal by the Japanese government, the ILC could move forward rapidly. The potential timeline would have an initial period of about 4 years to obtain international agreements, prepare for the construction, and form the international laboratory and its governance structure. The construction phase would then need 9 years.

It is an important aspect of the discussions of the ILC in Japan that the ILC has been organized from the beginning as a global project that will foster exchange between Japan and other nations. Thus, the scientific interest and political engagement of partner countries is of major importance for the Japanese authorities.

The purpose of this report is to set out in detail the current status of the ILC project, expanding on a recent paper prepared as input to the Update of the European Strategy for Particle Physics [9]. We discuss the physics reach of the ILC, the technological maturity of the accelerator, detector, and software/computing designs, and the further steps needed to concretely realise the project. Section 2 describes the accelerator design and technology, reviewing both current status of SCRF development and the general layout of the machine. This section also presents luminosity and energy upgrade options, as well as civil engineering plans, including site specific details, and cost and schedule estimates. Section 3 presents the current thinking about the operations of the ILC, with estimates of the plan and schedule for the collection of integrated luminosity. Section 4 gives an overview of the physics case for the ILC as a 250 GeV collider. This includes a more detailed discussion of the significance of the Higgs boson as a tool for searching for physics beyond the SM, the qualitative comparison of the ILC to the LHC as a facility for precision Higgs studies, and the theoretical approach for extracting Higgs boson couplings from  $e^+e^-$  data. This section also discusses the physics opportunities of searches for exotic Higgs decays and studies of other processes of interest including SM fermion pairproduction and searches for new particle pair production. Section 5 described the additional opportunities that the energy extension to 500 GeV will make available.

Section 6 provides detailed descriptions of the ILC detector designs that have been developed by the community, through detector R&D and prototyping, and used as detector models to show the simulated performance on the various physics channels. Section 7 summarises the computing needs of the ILC program, including software. These two sections provide the basis for a discussion of the experimental measurements of reactions crucial to the ILC program. All of the projections of experimental uncertainties given in this paper are based on fullsimulation studies using the model detectors described in Sec. 6, with capabilities justified by extensive R&D programs.

Building on this discussion, Sec. 8 gives a description of physics simulations involving Higgs boson reactions. Section 9 describes physics simulations carried out for the reactions  $e^+e^- \to W^+W^-$  and  $e^+e^- \to f\bar{f}$ . Section 10 discusses simulations of measurements of top quark properties at the energy-upgraded ILC. These studies lead to concrete quantitative estimates for the expected uncertainties in Higgs boson coupling determinations. Based on the results of these studies, we present in Sec. 11 what we feel are conservative estimates for the precision that the ILC will attain in a highly model-independent analyss for the determination of the Higgs boson width and absolutely normalized couplings. We compare these estimates to those presented in the CDRs for other  $e^+e^-$  Higgs factories and those expected from the high-luminosity phase of the LHC.

Section 12 describes the capability of the ILC for direct searches for pair-production of new particles, covering a number of scenarios that are difficult for the LHC but which can be investigated in detail at  $e^+e^-$  colliders. Section 13 gives our conclusions.

### 2. ILC MACHINE DESIGN

The International Linear Collider (ILC) is a 250 GeV (extendable up to 1 TeV) linear  $e^+e^-$  collider, based on 1.3 GHz superconducting radio-frequency (SCRF) cavities. It is designed to achieve a luminosity of  $1.35 \cdot 10^{34}$  cm<sup>-1</sup>s<sup>-1</sup> and provide an integrated luminosity of  $400 \text{ fb}^{-1}$  in the first four years of running. The electron beam will be polarised to 80 %, and positrons with 30 % polarization will be provided if the undulator based positron source concept is employed.

Its parameters have been set by physics requirements first outlined in 2003, updated in 2006, and thoroughly discussed over many years with the physics user community. After the discovery of the Higgs boson it was decided that an initial energy of 250 GeV provides the opportunity for a precision Standard Model and Higgs physics programme at a reduced initial cost [2]. Some relevant parameters are given in Tab. I. This design evolved from two decades of R&D, described in Sec. 1, an international effort coordinated first by the GDE under ICFA mandate and since 2013 by the LCC.

The fundamental goal of the design of the ILC accelerator is a high energy-efficiency. The ILC design limits the overall power consumption of the accelerator complex during operation to 129 MW at 250 GeV and 300 MW at 1 TeV, which is comparable to the power consumption of CERN. This is achieved by the use of SCRF technology for the main accelerator, which offers a high RF-to-beam efficiency through the use of superconducting cavities, operating at 1.3 GHz, where high-efficiency klystrons are

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Quantity	Symbol	Unit	Initial	$\mathcal{L}$ Upgrade	TDR	Upgr	ades
Centre of mass energy	$\sqrt{s}$	$\mathrm{GeV}$	250	250	250	500	1000
Luminosity	$\mathcal{L} = 10^{34}$	${\rm cm}^{-2}{\rm s}^{-1}$	1.35	2.7	0.82	1.8/3.6	4.9
Polarisation for $e^{-}(e^{+})$	$P_{-}(P_{+})$		80%(30%)	80%(30%)	80%(30%)	80%(30%)	80%(20%)
Repetition frequency	$f_{\rm rep}$	Hz	5	5	5	5	4
Bunches per pulse	$n_{\mathrm{bunch}}$	1	1312	2625	1312	1312/2625	2450
Bunch population	$N_{\rm e}$	$10^{10}$	2	2	2	2	1.74
Linac bunch interval	$\Delta t_{ m b}$	ns	554	366	554	554/366	366
Beam current in pulse	$I_{\rm pulse}$	mA	5.8	5.8	8.8	5.8	7.6
Beam pulse duration	$t_{\rm pulse}$	$\mu { m s}$	727	961	727	727/961	897
Average beam power	$P_{\rm ave}$	MW	5.3	10.5	10.5	10.5/21	27.2
Norm. hor. emitt. at IP	$\gamma \epsilon_{\mathrm{x}}$	$\mu { m m}$	5	5	10	10	10
Norm. vert. emitt. at IP	$\gamma \epsilon_{ m y}$	nm	35	35	35	35	30
RMS hor. beam size at IP	$\sigma^*_{ m x}$	nm	516	516	729	474	335
RMS vert. beam size at IP	$\sigma_{ m y}^*$	nm	7.7	7.7	7.7	5.9	2.7
Luminosity in top $1\%$	$\mathcal{L}_{0.01}/\mathcal{L}$		73%	73%	87.1%	58.3%	44.5%
Energy loss from beamstrahlung	$\delta_{ m BS}$		2.6%	2.6%	0.97%	4.5%	10.5%
Site AC power	$P_{\rm site}$	MW	129		122	163	300
Site length	$L_{\rm site}$	$\rm km$	20.5	20.5	31	31	40

TABLE I: Summary table of the ILC accelerator parameters in the initial 250 GeV staged configuration (with TDR parameters at 250 GeV given for comparison) and possible upgrades. A 500 GeV machine could also be operated at 250 GeV with 10 Hz repetition rate, bringing the maximum luminosity to  $5.4 \cdot 10^{34} \text{ cm}^{-2} \text{s}^{-1}$  [10].

commercially available. At accelerating gradients of 31.5 to  $35 \,\mathrm{MV/m}$  this technology offers high overall efficiency and reasonable investment costs, even considering the cryogenic infrastructure needed for the operation at 2 K.

The underlying TESLA technology is mature, with a broad industrial base throughout the world, and is in use at a number of free electron laser facilities that are in operation (E-XFEL at DESY, Hamburg), under construction (LCLS-II at SLAC, Stanford) or in preparation (SCLF in Shanghai) in the three regions Asia, Americas, and Europe that contribute to the ILC project. In preparation for the ILC, Japan and the U.S. have founded a collaboration for further cost optimisation of the TESLA technology. In recent years, new surface treatment technologies utilising nitrogen during the cavity preparation process, such as the so-called nitrogen infusion technique, have been developed at Fermilab, with the prospect of achieving higher gradients and lower loss rates with a less expensive surface preparation scheme than assumed in the TDR (see Sec. 2.2.1).

When the Higgs boson was discovered in 2012, the Japan Association of High Energy Physicists (JAHEP) made a proposal to host the ILC in Japan [11, 12]. Subsequently, the Japanese ILC Strategy Council conducted a survey of possible sites for the ILC in Japan, looking for suitable geological conditions for a tunnel up to 50 km in length (as required for a 1 TeV machine), and the possibility to establish a laboratory where several thousand international scientists can work and live. As a result, the candidate site in the Kitakami region in northern Japan, close to the larger cities of Sendai and Morioka, was found to be the best option. The site offers a large, uniform granite formation with no currently active faults and a geology that is well suited for tunnelling. Even in the great Tohoku earthquake in 2011, underground in-

stallations in this rock formation were essentially unaffected [13], which underlines the suitability of this candidate site.

This section starts with a short overview over the changes of the ILC design between the publication of the TDR in 2013 and today, followed by a description of the SCRF technology, and an description of the overall accelerator design and its subsystems. Thereafter, possible upgrade options are laid out, the Japanese candidate site in the Kitakami region is presented, and costs and schedule of the accelerator construction project are shown.

#### 2.1. Design evolution since the TDR

Soon after the discovery of the Higgs boson, the Technical Design Report (TDR) for the ILC accelerator was published in 2013 [14, 15] after 8 years of work by the Global Design Effort (GDE). The TDR design was based on the requirements set forth by the ICFA mandated parameters committee [16]:

- a centre-of-mass energy of up to 500 GeV,
- tunability of the centre-of-mass energy between  $\sqrt{s} = 200 \,\text{GeV}$  and 500 GeV,
- a luminosity sufficient to collect  $500 \text{ fb}^{-1}$  within four years of operation, taking into account a threeyear a ramp up. This corresponds to a final luminosity of  $250 \text{ fb}^{-1}$  per year and an instantaneous luminosity of  $\mathcal{L} = 2 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ ,
- an electron polarisation of at least 80 %,
- the option for a later upgrade to energies up to 1 TeV.



FIG. 1: Schematic layout of the ILC in the 250 GeV staged configuration.

The accelerator design presented in the TDR met these requirements (see Tab. I), at an estimated construction cost of 7,982 MILCU for a Japanese site, plus 22.9 Mh (million hours) of labour in participating institutes [15, Sec. 15.8.4]. Costs were expressed in ILC Currency Units ILCU, where 1 ILCU corresponds to 1 US\$ at 2012 prices.

In the wake of the Higgs discovery, and the proposal by the Japan Association of High Energy Physicists (JA-HEP) to host the ILC in Japan[11] with its recommendation to start with a 250 GeV machine [12], plans were made for a less expensive machine configuration with a centre–of–mass energy of  $\sqrt{s} = 250$  GeV, around the maximum of the Zh production cross section, half the TDR value. Various options were studied in the TDR [15, Sect. 12.5] and later [17]. This resulted in a revised proposal [2] for an accelerator with an energy of 250 GeV and a luminosity of  $\mathcal{L} = 1.35 \cdot 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ , capable of delivering about 200 fb<sup>-1</sup> per year, or 400 fb<sup>-1</sup> within the first four years of operation, taking into account the ramp-up.

Several other changes of the accelerator design have been approved by the ILC Change Management Board since 2013, in particular:

- The free space between the interaction point and the edge of the final focus quadrupoles  $(L^*)$  was unified between the ILD and SiD detectors [18], facilitating a machine layout with the best possible luminosity for both detectors.
- A vertical access shaft to the experimental cavern was foreseen [19], allowing a CMS-style assembly concept for the detectors, where large detector parts are built in an above-ground hall while the underground cavern is still being prepared.
- The shield wall thickness in the Main Linac tunnel

was reduced from 3.5 to 1.5 m [20], leading to a significant cost reduction. This was made possible by dropping the requirement for personnel access during beam operation of the main linac.

- Power ratings for the main beam dumps, and intermediate beam dumps for beam aborts and machine tuning, were reduced to save costs [21].
- A revision of the expected horizontal beam emittance at the interaction point at 125 GeV beam energy, based on improved performance expectations for the damping rings and a more thorough scrutiny of beam transport effects at lower beam energies, lead to an increase of the luminosity expectation from 0.82 to  $1.35 \cdot 10^{34}$  cm<sup>-2</sup> s<sup>-1</sup> [22].
- The active length of the positron source undulator has been increased from 147 to 231 m to provide sufficient intensity at 125 GeV beam energy [23].

These changes contributed to an overall cost reduction, risk mitigation, and improved performance expectation.

Several possibilities were evaluated for the length of the initial tunnel. Options that include building tunnels with the length required for a machine with  $\sqrt{s} = 350 \text{ GeV}$  or 500 GeV, were considered. In these scenarios, an energy upgrade would require the installation of additional cryomodules (with RF and cryogenic supplies), but little or no civil engineering activities. In order to be as cost effective as possible, the final proposal (see Figure 1), endorsed by ICFA [24], does not include these empty tunnel options.

While the length of the main linac tunnel was reduced, the beam delivery system and the main dumps are still designed to allow for an energy upgrade up to  $\sqrt{s} = 1 \text{ TeV}.$ 



FIG. 2: A 1.3 GHz superconducting niobium nine-cell cavity.

#### 2.2. Superconducting RF Technology

The heart of the ILC accelerator consists of the two superconducting Main Linacs that accelerate both beams from 5 to 125 GeV. These linacs are based on the TESLA technology: beams are accelerated in 1.3 GHz nine-cell superconducting cavities made of niobium and operated at 2 K (Fig. 2). These are assembled into cryomodules comprising nine cavities or eight cavities plus a quadrupole/corrector/beam position monitor unit, and all necessary cryogenic supply lines (Fig. 3). Pulsed klystrons supply the necessary radio frequency power (High-Level RF HLRF) to the cavities by means of a waveguide power distribution system and one input coupler per cavity.

This technology was primarily developed at DESY for the TESLA accelerator project that was proposed in 2001. Since then, the TESLA technology collaboration [25] has been improving this technology, which is now being used in several accelerators in operation (FLASH at DESY [26, 27], E-XFEL in Hamburg [28]), under construction (LCLS-II at SLAC, Stanford, CA [29]) or planned (SHINE in Shanghai [30]).



FIG. 3: An ILC type cryomodule. ©Rey.Hori/KEK.

#### 2.2.1. The quest for high gradients

The single most important parameter for the cost and performance of the ILC is the accelerating gradient g. The TDR baseline value is an average gradient g = 31.5 MV/m for beam operation, with a  $\pm 20\%$  gradient spread between individual cavities. Recent progress in R&D for high gradient cavities raises the hope to increase the gradient by 10% to g = 35 MV/m, which would reduce the total cost of the 250 GeV accelerator by about 6%. To achieve the desired gradient in beam operation, the gradient achieved in the low-power vertical test (mass production acceptance test) is specified 10% higher to allow for operational gradient overhead for low-level RF (LLRF) controls, as well as some degradation during cryomodule assembly (few MV/m). Figure 4 shows how the achievable gradients have evolved over the past 50 years [31].

*a*. Gradient impact on costs: To the extent that the cost of cavities, cryomodules and tunnel infrastructure is independent of the achievable gradient, the investment cost per GeV of beam energy is inversely proportional to the average gradient achieved. This is the reason for the enormous cost saving potential from higher gradients. This effect is partially offset by two factors: the energy stored in the electromagnetic field of the cavity, and the dynamic heat load to the cavity from the electromagnetic field. These grow quadratically with the gradient for one cavity, and therefore linearly for a given beam energy. The electromagnetic energy stored in the cavity must be replenished by the RF source during the filling time that precedes the time when the RF is used to accelerate the beam passing through the cavity; this energy is lost after each pulse and thus reduces the overall efficiency and requires more or more powerful modulators and klystrons. The overall cryogenic load is dominated by the dynamic heat load from the cavities, and thus operation at higher gradient requires larger cryogenic capacity. Cost models that parametrise these effects indicate that the minimum of the investment cost per GeV beam energy lies at 50 or more GeV, depending on the relative costs of tunnel, SCRF infrastructure and cryo plants, and depending on the achievable  $Q_0$  [32]. Thus, the optimal gradient is significantly higher than the value of approximately  $35 \,\mathrm{MV/m}$  that is currently realistic; this emphasises the relevance of achieving higher gradients.

It should be noted that in contrast to the initial investment, the operating costs rise when the gradient is increased, and this must be factored into the cost model.

b. Gradient limitations: Fundamentally, the achievable gradient of a SC cavity is limited when the magnetic field at the cavity walls surpasses the critical field  $H_{\rm crit,RF}$  of the superconductor. This gradient depends on the material, operating temperature, and the cavity geometry. For the TESLA type cavities employed at the ILC, this limit is about 48 MV/m at 2 K. The best E-XFEL production cavity reached 44.6 MV/m (Fig. 5). The record for single cell cavities operating at 1.3 GHz is 59 MV/m [33].

Niobium is a type-II superconductor, and so it has two distinct superconducting phases, the Meissner state, with complete magnetic flux expulsion, which exists up to a field strength  $H_{c1} \approx 180 \text{ mT}/\mu_0 \ (\mu_0 = 4\pi 10^{-7} \text{ T m/A}$  being the vacuum permeability), and a mixed state in which



FIG. 4: Development of the gradient of SRF cavities since 1970 [31, updated].

flux vortices penetrate the material, up to a higher field strength  $H_{c1}$ , at which superconductivity breaks down completely. In time-dependent fields, the penetrating vortices move due to the changing fields and thus dissipate energy, causing a thermal breakdown. However, for RF fields, the Meissner state may persist metastably up to the superheating field strength  $H_{\rm sh} \approx 240 \,{\rm mT}/\mu_0$ , which is expected to be the critical RF field critical field  $H_{\text{crit,RF}}$  [34]. Experimentally, niobium RF cavities have been operated at field strengths as high as  $H = 206 \,\mathrm{mT}/\mu_0$  [33], and the best E-XFEL production cavities reach about 190 mT. Recently, even 210 mT has been achieved at FNAL [35]. In recent years, theoretical understanding of the nature of this metastable state and the mechanisms at the surface that prevent flux penetration has significantly improved [36, 37]. It appears that a thin layer of "dirty" niobium, *i.e.*, with interstitial impurities, on top of a clean bulk with good thermal conductivity, is favourable for high field operation.

The gradient at which a SC cavity can be operated in practice is limited by three factors in addition to those just listed [34]:

- the thermal breakdown of superconductivity, when local power dissipation causes a local quench of the superconductor,
- the decrease of the quality factor  $Q_0$  at high gradients that leads to increased power dissipation,
- the onset of field emission that causes the break-

down of the field in the cavity.

The onset of these adverse effects is mostly caused by micro-metre sized surface defects of various kinds. Producing a sufficiently defect-free surface in an economic way is thus the central challenge in cavity production.

More than 20 years of industrial production of TESLA type cavities have resulted in a good understanding which production steps and quality controls are necessary to produce cavities with high-quality, nearly defect-free surfaces that are capable of achieving the desired high field strengths at a reasonable production yield.

c. Results from E-XFEL cavity production: The production and testing of 831 cavities for the E-XFEL [38, 39] provides the biggest sample of cavity production data so far. Cavities were acquired from two different vendors, RI and EZ. Vendor RI employed a production process with a final surface treatment closely following the ILC specifications, including a final electropolishing (EP) step, while the second vendor EZ used buffered chemical polishing (BCP). The E-XFEL specifications asked for a usable gradient of  $23.6\,\mathrm{MV/m}$  with a  $Q_0 \ge 1 \cdot 10^{10}$  for operation in the cryomodule; with a 10 % margin this corresponds to a target value of 26 MV/m for the performance in the vertical test stand for single cavities. Figure 5 shows the  $Q_0$  data versus accelerating gradient of the best cavities received, with several cavities reaching more than  $40 \,\mathrm{MV/m}$ , significantly beyond the ILC goal, already with  $Q_0$  values that approach the target value  $1.6 \cdot 10^{10}$  that is the goal of future high-gradient



FIG. 5: Examples of the  $Q_0 (E_{\rm acc})$  curves of some of the best cavities, either treated at RI using "EP final", or at EZ using "BCP flash." [38, Fig. 19]. Vendor "RI" employs a production process that closely follows the ILC specifications, with a final electropolishing step. The ILC gradient /  $Q_0$  goals are overlaid.

R&D.



FIG. 6: Distribution and yield of the "as received" maximum gradient of cavities produced for the E-XFEL, separated by vendor [39, Fig. 33]. Vendor RI employs a production process that closely follows the ILC specifications, with a final electro polishing step.

E-XFEL production data, in particular from vendor RI, provide excellent statistics for the cavity performance as received from the vendors, as shown in Fig. 6. For vendor RI, the yield for cavities with a maximum gradient above 28 MV/m is 85 %, with an average of 35.2 MV/m for the cavities that pass the cut.

Since the E-XFEL performance goal was substantially lower than the ILC specifications, cavities with gradient below 28 MV/m, which would not meet ILC specifications, were not generally re-treated for higher gradients, limiting our knowledge of the effectiveness of retreatment for large gradients. Still, with some extrapolation it is possible to extract yield numbers applicable to the ILC specifications [40].

The E-XFEL data indicate that after re-treating cavities with gradients outside the ILC specification of  $35 \text{ MV/m} \pm 20 \%$ , *i.e.*, below 28 MV/m, a yield of 94 %for a maximum gradient above 28 MV/m can be achieved, with an average value of 35 MV/m, meeting the ILC specification. Taking into account limitations from  $Q_0$  and the onset of field emission, the usable gradient is lower. This gives a 82 (91) % yield and an average usable gradient of 33.4 MV/m after up to one (two) re-treatments. The re-treatment and testing rate is significantly higher than assumed in the TDR, but the E-XFEL experience shows that re-treatment can mostly be limited to a simple high-pressure rinse (HPR) rather than an expensive electropolishing step.

Overall, the E-XFEL cavity production data prove that it is possible to mass-produce cavities meeting the ILC specifications as laid out in the TDR with the required performance and yield.



FIG. 7: Effect of successive cavity treatments on a single cavity: 800 °C bake for five days (black, lowest curve), followed by 48 hours baking at 120 °C (red, middle curve). A third heat treatment including nitrogen infusion (green, top curve) significantly raises the breakdown gradient and the quality factor of the cavity [41, Fig. 5].

d. High-gradient R & D – nitrogen infusion: In recent years, new techniques have emerged that seem to indicate that higher gradients combined with higher quality factors are attainable in bulk niobium cavities.

In the early 2010s, nitrogen doping was developed as a method to substantially increase  $Q_0$  by adding nitrogen during the 800 °C baking, which leads to interstitial nitrogen close to the niobium surface [42]. This technique has been employed successfully in the production of the cavities for LCLS-II, with an average  $Q_0$  of  $3.0 \cdot 10^{10}$ achieved in a prototype cryomodule [43]. However, nitrogen doping reduces the critical RF field of the material and thus limits the achievable gradients to values below 30 MV/m, rendering doped material useless for high gradient applications.

By contrast, in nitrogen infusion the nitrogen is added during the low temperature baking at 120 °C. Experimental results seem to indicate that nitrogen infusion may offer a combination of three advantages:

- Reaching higher accelerating gradients,
- higher  $Q_0$  values, resulting in a reduced cryogenic load,
- a simplified and less expensive production process that does away with the final electropolishing step.

Figure 7 [41, Fig. 19] shows how the addition of nitrogen during the final 48 h long 120 °C bake of a one-cell cavity drastically improves the cavity quality factor as well as the maximum gradient, which comes close to the best E-XFEL cavity results, but at higher  $Q_0$ .

Up to now, it has been difficult to reproduce these exciting results in other laboratories. Success has been reported by groups at JLAB [44], and Cornell [45], but KEK has reported mixed results [46], and DESY has so far not been able to reproduce these results [47]. These difficulties seem to indicate that the recipe for a successful application of nitrogen infusion is not yet fully understood, and that further research and development will be necessary before this process can be transferred to industry.

Nevertheless, the infusion results have triggered a renewed interest in the research on highest gradients in niobium cavities, with a host of new experimental results, increased activity to achieve a more thorough theoretical understanding [36, 37], and application of state-of-the-art analytical methods such as muon spin rotation (muSR) [48]. Recently, a record gradient for TESLA shape cavities of 49 MV/m was reported [35] with a low temperature treatment at 75 °C after 120 °C baking without nitrogen. All these results provide reason for optimism that an improved understanding of the mechanisms that stabilise superconductivity in the presence of high fields will result in improved performance of industrially produced cavities for the ILC.

e.High-gradient R & D – alternative cavity shapes: Fundamentally, the achievable gradient in a niobium cavity is limited by the maximum magnetic field at the cavity surface, not the electrical field strengths. The ratio between peak surface field  $B_{\rm pk}$  and gradient g depends on the cavity geometry and is  $B_{\rm pk}/g = 4.26 \,\mathrm{mT/(MV/m)}$ for TESLA type cavities. A number of alternative cavity shapes have been investigated with lower ratios [49], resulting in single cells gradients up to  $59 \,\mathrm{MV/m}$  [33]. The reduced magnetic field, however, has to be balanced with other factors that favour the TESLA cavity shape, namely: a reasonable peak electrical field to limit the risk of field emission, sufficient iris width and cell-to-cell RF coupling, and a mechanical shape that can be efficiently fabricated.

Recently, new five-cell cavities with a new "low surface field" (LSF) shape [50] have been produced at JLAB and have achieved gradient of up to 50 MV/m in three of the five cells, which is a new record for multi-cell cavities [51]. The LSF shape aims to achieve a good compromise between the goal of a low magnetic field and the other criteria, and demonstrates that further improvements in gradient may be realised in the future.

#### 2.2.2. Further cost reduction R&D

Additional strategies for cost reduction and improved cavity performance are also being investigated.

a. Low RRR material: The niobium raw material and preparation of sheets are a significant cost driver; R&D is underway to re-evaluate the stringent limits on impurities, especially of tantalum, and the demand for a high residual resistivity ratio  $RRR > 300^{-1}$ , to reduce the raw material cost. The electrical conductivity and heat transport by electrons are proportional. This implies that large RRR values, indicative of low impurity content, make the cavities also less susceptible to thermal breakdown from surface defects. However, when defect sizes can be successfully controlled to the extent necessary to achieve gradients above 35 MV/m routinely, the influence of heat conductivity and RRR may be diminished, permitting the use of lower RRR material [52].

b. Ingot and large-grain niobium: Together with direct slicing of discs from large niobium ingots, without rolling, forging and grinding or polishing steps, the cost for niobium sheets has the potential to be reduced by 50% [2, 53]. Without the mechanical deformation during rolling and forging, the grains from the initial crystallisation stay large, which makes later production steps, in particular deep-drawing of half cells, more challenging. Nevertheless, if these challenges are overcome, tests with large-grain and ingot niobium show promising results [54, 55].

#### 2.2.3. Basic parameters

The choice of operating frequency is a balance between the higher cost of larger, lower-frequency cavities and the increased cost at higher frequency associated with the lower sustainable gradient from the increased surface resistivity. The optimum frequency is in the region of 1.5 GHz, but during the early R&D on the technology, 1.3 GHz was chosen due to the commercial availability of high-power klystrons at that frequency.

<sup>&</sup>lt;sup>1</sup> *RRR* is the ratio of the material's room temperature resistivity to the normal conducting resistivity close to 0K; heat conductivity from electrons is proportial to *RRR*. *RRR* is reduced by impurities, in particular interstitial ones from hydrogen, nitrogen and oxygen.

The superconducting accelerating cavities for the ILC are nine-cell structures made out of high-purity niobium (Fig. 2), with an overall length of 1.25 m. Cavity production starts from niobium ingots which are forged and rolled into 2.8 mm thick niobium sheets that are individually checked for defects by an eddy current scan and optical inspection [14]. Cavity cells are produced by deepdrawing the sheets into half cells, 18 of which are joined by electron beam welding with two end groups to form the whole structure. This welding process is one of the most critical and cost-intensive steps of the cavity manufacturing procedure. Utmost care must be taken to avoid irregularities, impurities and inclusions in the weld itself, and deposition of molten material at the inner surface of the cavity that can lead to field emission.

After welding, the inner surface of the cavity must be prepared. The process is designed to remove material damage incurred by chemical procedures during the fabrication process, chemical residues from earlier production steps, hydrogen in the bulk niobium from earlier chemical processing, and contamination from particles. In a last step, the cavity is closed to form a hermetically sealed structure ready for transport. The treatment steps involve a series of rinses with ethanol or high pressure water, annealing in a high purity vacuum furnace at  $800^{\circ}$  C and  $120^{\circ}$  C, and electropolishing or buffered chemical polishing. The recipe for the surface preparation has been developed over a long time. Still, it remains subject to optimisation, since it is a major cost driver for the cavity production and largely determines the overall performance and yield of the cavities. In particular the electropolishing steps are complicated and costly, as they require complex infrastructure and highly toxic chemicals. One advantage of nitrogen infusion (see Sec. 2.2.1) is that the final electropolishing step is omitted.

Careful quality control during the production process is of high importance. At the E-XFEL, several quality controls were conducted by the manufacturer during production, with nonconformities reported to the institute responsible for the procurement, where a decision was made whether to accept or reject a part [38]. With this "build to print" approach, in which the manufacturer guarantees that a precise production process will be followed but does not guarantee a specific performance, procurement costs are reduced, because the manufacturer does not carry, and does not charge for, the performance risk.

Upon reception from the manufacturer, cavities are tested in a vertical cryostat ("vertical test"), where  $Q_0$  is measured as a function of the gradient. Cavities that fall below the specified gradient goal are re-treated by an additional (expensive) electropolishing step or a comparatively simple high-pressure rinse. After retreatment, the vertical test is repeated.

Re-treatment and tests constitute a major cost driver in cavity production. For the ILC TDR, it was assumed that 25% of the cavities would fall below the 28 MV/m gradient threshold and undergo re-treatment and a second vertical test. E-XFEL data from the vendor "RI" that followed the ILC production recipe indicate that 15% to 37% of the cavities fall below 28 MV/m, depending on whether the maximum or the "usable" achieved gradient is considered [40]. However, E-XFEL experience also shows that, in most of the cases, a high-pressure rinse is sufficient as re-treatment to remove surface defects, which is a cost saving compared to the electropolishing assumed in the TDR.

After successful testing, prior to installation in the cryomodule, cavities are equipped with a magnetic shield and the frequency tuner, which exerts mechanical force on the cavity to adjust the resonant frequency to the frequency of the external RF field [15, Sect. 3.3].

#### 2.2.5. Power coupler

The power coupler transfers the radio frequency (RF) power from the waveguide system to the cavity. In the ILC, a coupler with a variable coupling is employed; this is realised using a movable antenna. Another role of the coupler is to separate the cavity vacuum from the atmospheric pressure in the waveguide, and to insulate the cavity at 2 K from the surrounding room temperature. Thus, the coupler has to fulfill a number of demanding requirements: transmission of high RF power with minimal losses and no sparking, vacuum tightness and robustness against window breaking, and minimal heat conductivity. As a consequence, the coupler design is highly complex, with a large number of components and several critical high-tech manufacturing steps.

The baseline coupler design was originally developed in the 1990s for the TESLA Test Facility (TTF, now FLASH) at DESY, and has since been modified by a collaboration of LAL and DESY for use in the E-XFEL. About 840 of these couplers (depicted in Fig. 8) were fabricated by three different companies for the E-XFEL [56], where 800 are now in operation. A lot of experience has been gained from this production [57].



FIG. 8: An E-XFEL type coupler.

#### 2.2.6. Cryomodules

To facilitate transportation, installation and operation, 8 or 9 cavities are integrated into a 12.6 m long cryomodule (Fig. 3), which houses the cavities, thermal insulation, and all necessary supply tubes for liquid and gaseous helium at 2 - 80 K temperature.



FIG. 9: View of installed cryomodules in the tunnel of the E-XFEL [58].

Nine of these cryomodules are connected in the tunnel to form a cryostring with a common liquid helium supply. RF for one such string is provided by two klystrons. No separate helium transfer line is necessary, as all helium transport lines are integrated within the modules. A quadrupole / beam position monitor / corrector magnet unit is mounted instead of the 9th cavity in every third module. Figure 9 shows installed cryomodules in the tunnel of the E-XFEL [58].

Cryomodule assembly requires a dedicated facility with large clean rooms, especially trained, experienced personnel, and thorough quality control [59]. The cryomodules are certified for liquid helium pressure of up to 2 bar. Thus they must conform to the applicable pressure vessel codes, which brings with it very stringent documentation requirements for all pressure bearing parts [60].

For the E-XFEL project, 103 cryomodules were assembled in a facility built and operated by CEA [59, 61] and industrial partners, demonstrating the successful industrialization of the assembly process, with a final throughput of one cryomodule every four working days. This production rate is close to the rate envisaged for a possible European contribution of 300 cryomodules to a 250 GeV ILC in Japan.

While the design gradient for E-XFEL accelerator modules of 23.6 MV/m is significantly lower than the aim of 31.5 - 35 MV/m for the ILC, a number of cryomodules have been built around the world that come close or reach the ILC TDR specification of 31.5 MV/m: An E-XFEL prototype module at DESY reached 30 MV/m [62], Fermilab has demonstrated cryomodule operation at the ILC specification of 31.5 MV/m [63], and KEK has reported





FIG. 10: Average of the operating (blue) and maximum (green) gradient for cavities in each E-XFEL serial-production cryomodule. The specification of 23.6 MV/m is marked by a red line [65]. Modules 98 and 99 were assembled from the lowest-performing cavities.

Figure 10 shows the average cavity gradients per cryomodule for the E-XFEL serial-production cryomodules [65]. In the tests, the gradients were limited administratively to 31 MV/m; the true maxima might be higher. For almost all of the modules, the cavity gradients are significantly above the E-XFEL specification of 23.6 MV/m.

#### 2.2.7. Plug-compatible design

In order to allow various designs of sub-components from different countries and vendors to work together in the same cryomodule, a set of interface definitions has been internationally agreed upon. This "plug-compatible" design ensures that components are interchangeable between modules from different regions and thus reduces the cost risk. Corresponding interface definitions exist for the cavity, the fundamental-mode power coupler, the mechanical tuner and the helium tank. The "S1Global" project [66] has successfully built a single cryomodule from several cavities equipped with different couplers and tuners, demonstrating the viability of this concept.

#### 2.2.8. High-level radio-frequency

The high-level radio-frequency (HLRF) system provides the RF power that drives the accelerating cavities. The system comprises modulators, pulsed klystrons, and a waveguide power distribution system.

a. Modulators: The modulators provide the short, high-power electrical pulses required by the pulsed klystrons from a continuous supply of electricity. The ILC design foresees the use of novel, solid state Marx modulators. These modulators are based on a solidstate switched capacitor network, where capacitors are charged in parallel over the long time between pulses, and discharged in series during the short pulse duration, transforming continuous low-current, low voltage electricity into short high-power pulses of the required high voltage of 120 kV at a current of 140 A, over 1.65 ms. Such Marx modulators have been developed at SLAC [67] and successfully tested at KEK [68]. However, long-term data about the required large mean time between failures (MTFB) are not yet available.

b. Klystrons: The RF power to drive the accelerating cavities is provided by 10 MW L-band multi-beam klystrons. Devices meeting the ILC specifications were initially developed for the TESLA project, and later for the E-XFEL. They are now commercially available from two vendors (Thales and Toshiba), both of which provided klystrons for the E-XFEL. The ILC specifications ask for a 65 % efficiency (drive beam to output RF power), which are met by the existing devices.

Recently, the High Efficiency International Klystron Activity (HEIKA) collaboration [69, 70] has been formed that investigates novel techniques for high–efficiency klystrons. Taking advantage of modern beam dynamic tools, methods such as the Bunching, Alignment and Collecting (BAC) method [71] and the Core Oscillation Method (COM) [72] (Fig. 11) have been developed that promise increased efficiencies up to 90 % [73]. One advantage of these methods is that it is possible to increase the efficiency of existing klystrons by equipping them with a new electron optics, as was demonstrated retrofitting an existing tube from VDBT, Moscow. This increased the output power by almost 50 % and its efficiency from 42 % to 66 % [74].

To operate the ILC at an increased gradient of 35 MV/m would require that the maximum klystron output power is increased from 10 to 11 MW. It is assumed that this will be possible by applying the results from this R&D effort to high-efficiency klystrons.



FIG. 11: Electron phase profile of an 800 MHz klystron employing the Core Oscillation Method (COM) [72].

c. Local Power–Distribution System (LPDS): In the baseline design, a single RF station with one modulator and klystron supplies RF to 39 cavities, which corresponds to 4.5 cryomodules [15, Sec. 3.6.4]. Then 2 klystrons drive a 9 cryomodule cryo-string unit. The power is distributed by the LPDS, a system of waveguides, power dividers and loads. All cavities from a 9-

cavity module and half of a 8–cavity module are connected in one LPDS, and three such LPDS units are connected to one klystron. This arrangement allows an easy refurbishment such that a third klystron can be added to a cryo-string, increasing the available power per cavity by 50 % for a luminosity upgrade (cf. Sec. 2.4).

The LPDS design must provide a cost-effective solution for the distribution of the RF power with minimal losses, and at the same time provide the flexibility to adjust the power delivered to each cavity by at least  $\pm 20\%$  to allow for the specified spread in maximum gradient. The LPDS design therefore contains remotely controlled, motor-driven Variable Power Dividers (VPD), phase shifters, and H-hybrids that can distribute the power with the required flexibility. This design allows one to optimise the power distribution during operation, based on the cavity performance in the installed cryomodule, and thus to get the optimum performance out of the system. It does not require a measurement of the individual cavity gradients after the module assembly, and is thus compatible with the ILC production scheme, where only a fraction of the cryomodules are tested. This is a notable difference from the scheme employed at the E-XFEL, where 100% of the modules were tested, and the power distribution for each module was tailored to the measured cavity gradients, saving investment costs for the LPDS but making the system less flexible.

#### 2.2.9. Cryogenics

The operation of the large number of superconducting cryomodules for the main linacs and the linacs associated with the sources requires a large–scale supply of liquid helium. The cyomodules operate at 2 K and are cooled with superfluid helium, which at 2 K has a vapour pressure of about 32 mbar.

The accelerator is supplied with liquid helium by several cryogenic plants [15, Sec. 3.5] of a size similar to those in operation at CERN for the LHC, at Fermilab, and DESY, with a cooling capacity equivalent to about 19 kW at 4.5 K. The 2 K and 4.5 K helium refrigerators are located in an underground access hall [75] that is connected to the surface, where the helium compressors, gas tanks and further cryogenic infrastructure are located. The total helium inventory is approximately 310000 liquid litres or about 41 metric tonnes, about one third of the LHC's helium inventory. A factor 2 more helium is needed for 500 GeV operation.

## 2.2.10. Series production and industrialisation, worldwide and in Europe

Due to the construction of the E-XFEL, the industrial basis for the key SCRF components is broad and mature, in particular in Europe. Europe has a leading supplier for raw material. In all three regions (Europe, America, Asia), several vendors for cavities have been qualified for ILC type cavities, and provided cost estimates in the past. Two leading cavity vendors are European companies that have profited from large scale production of cavities for E-XFEL; both have won contracts for LCLS-II as a consequence. RF couplers have also been successfully produced by European and American vendors for the E-XFEL and LCLS-II projects.

ILC/TESLA type cryomodules have been built in laboratories around the world (DESY, CEA in Europe, FNAL and JLAB in America, KEK in Asia). Series production has been established in America at Fermilab and JLAB for LCLS-II. The largest series production was conducted by CEA in France, again for the E-XFEL, with the assembly of 103 cryomodules in total by an industrial partner under the supervision of CEA personnel, with a final throughput of one cryomodule produced every four working days.

ILC type, pulsed 10 MW klystrons are commercially available from two vendors in Japan and Europe.

For E-XFEL, China has been a supplier for niobium raw material and cryomodule cold masses (the cryostat with internal insulation and tubing). For the planned SCLF project in Shanghai, China has started to develop cavity and cryomodule production capabilities, which will further broaden the worldwide production capabilities for SCRF components. This reduces the risk that prices are pushed up by a monopoly of manufacturers for a large scale order of components as required for the ILC.

Overall, European industry is well prepared to produce the high-tech, high-value SCRF components needed for the ILC, which would likely constitute the largest fraction of any European in-kind contribution (IKC) to the ILC, at very competitive prices. Thus, expenditure for the European IKC will likely stay in Europe, with an excellent chance to stay within the price range assumed in the value estimate. Moreover, European companies are well positioned to win additional contracts from other regions, increasing the economic benefit for Europe from an ILC project.

#### 2.3. Accelerator design

#### 2.3.1. Electron and positron sources

The electron and positron sources are designed to produce 5 GeV beam pulses with a bunch charge that is 50 % higher than the design bunch charge of  $3.2 \text{ nC} (2 \cdot 10^{10} \text{ e})$ , in order to have sufficient reserve to compensate any unforeseen inefficiencies in the beam transport. In the baseline design, both sources produce polarized beams with the same time structure as the main beam, *i.e.*, 1312 bunches in a 727  $\mu$ s long pulse.

The electron source design [15] is based on the SLC polarized electron source, which has demonstarted that the bunch charge, polarisation and cathode lifetime parameters are feasible. The long bunch trains of the ILC do require a newly developed laser system and powerful preaccelerator structures, for which preliminary designs are available. The design calls for a Ti:sapphire

laser impinging on a photocathode based on a strained GaAs/GaAsP superlattice structure, which will produce electron bunches with an expected polarisation of 85%, sufficient for 80% beam polarization at the interaction point, as demonstrated at SLAC [76].

The positron source poses a larger challenge.

In the baseline design, hard gamma rays are produced in a helical undulator driven by the main electron beam, which are converted to positrons in a rotating target. Positrons are captured in a flux concentrator or a quarter wave transformer, accelerated to 400 MeV in two normal conducting preaccelerators followed by a superconducting accelerator very similar to the main linac, before they are injected into the damping rings at 5 GeV. The helical undulators produce photons with circular polarisation, which is transferred to the positrons produced in the target, which are longitudinally polarised as a result. The positron polarisation thus achieved is 30%. The E-166 experiment at SLAC has successfully demonstrated this concept [77], albeit at intensities much lower than foreseen for the ILC. Technological challenges of the undulator source concept are the target heat load, the radiation load in the flux concentrator device, and the dumping of the high intensity photon beam remnant.

As an alternative, an electron-driven positron source concept has been developed. In the electron-driven scheme, a 3 GeV electron beam from a dedicated normal conducting linac produces positrons in a rotating target. The electron drive beam, being independent from the main linac, has a completely different time structure. Positrons are produced in 20 pulses at 300 Hz with 66 bunches each. With this scheme, it takes about 67 ms to produce the positrons needed for a single Main Linac pulse with its 1312 bunches, compared to  $0.8 \,\mathrm{ms}$  for the undulator source. This different time structure spreads the heat load on the target over a longer time, allowing a target rotation speed of only 5 m/s rather than 100 m/s, which reduces the engineering complexity of the target design, in particular the vacuum seals of the rotating parts. Although not free from its own engineering challenges, such as the high beam loading in the normal conducting cavities, the electron driven design is currently considered to be a low risk design that is sure to work.

Aside from the low technical risk, the main advantage of the electron driven design is the independence of positron production and electron main linac operation, which is an advantage for accelerator commissioning and operation in general. In particular, electron beam energies below 120 GeV for operation at the Z resonance or the WW threshold would be no problem. The undulator source, on the other hand, offers the possibility to provide beams at the maximum repetition rate of 10 Hz given by the damping time in the damping rings of 100 ms, whereas the electron driven scheme is limited to 6 Hz due to the additional 66 ms for positron production. The main difference between the concepts is the positron polarisation offered by the undulator source, which adds significantly to the physics capabilities of the machine. The physics implications of positron polarization is discussed later in the report, in Secs. 4.10 and 8.3.

Both concepts have been reviewed recently [23] inside the ILC community, with the result that both source concepts appear viable, with no known show stoppers, but they require some more engineering work. The decision on the choice will be taken once the project has been approved, based on the physics requirements, operational aspects, and technological maturity and risks.

a. Beam polarisation and spin reversal At the ILC, the electron beam and potentially the positron beam are longitudinally polarised at the source, *i.e.*, the polarisation vector is oriented parallel or antiparallel to the beam direction. Whenever a longitudinally polarised beam of energy  $E_{\text{beam}}$  is deflected by an angle  $\theta_{\text{bend}}$ , the polarisation vector undergoes a precession through an angle  $\theta_{\rm pol} = \gamma a \theta_{\rm bend}$  [78], with the Lorentz factor  $\gamma = E_{\rm beam}/m_{\rm e}$  and the electron's anomalous magnetic moment a = (q-2)/2. To preserve the longitudinal beam polarisation during the long transport from the source through the damping rings to the start of the main linac, which involves many horizontal bends, the beam polarisation vector is rotated into the transverse plane, perpendicular to the damping ring plane, before the beam is transferred to the damping rings, and rotated back to a longitudinal direction by a set of spin rotators at the end of the RTML (see Sec. 2.3.3). Through the use of two rotators, it is possible to bring the polarisation vector into any desired direction, and compensate any remaining net precession between these spin rotators and the interaction point, so that any desired longitudinal or transverse polarisation at the IP can be provided.

To control systematic effects, fast helicity reversal is required. This is helicity reversal of each beam independently, on a pulse to pulse basis, which must be achieved without a change of the magnetic fields of the spin rotator magnets. For the electron beam, a fast helicity reversal is possible through a flip of the cathode laser polarisation. For the undulator-based positron source, the photon polarisation is given by the undulator field. Two parallel sets of spin rotators in front of the damping rings are used that rotate the polarisation vector either to the +y or -y direction. With this scheme, fast kickers can select a path through either of the two spin rotators and thus provide a fast spin reversal capability [78, 79].

#### 2.3.2. Damping rings

The ILC includes two oval damping rings of 3.2 km circumference, sharing a common tunnel in the central accelerator complex. The damping rings reduce the horizontal and vertical emittance of the beams by almost six orders of magnitude<sup>2</sup> within a time span of only 100 ms,

to provide the low emittance beams required at the interaction point. Both damping rings operate at an energy of  $5 \,\text{GeV}$ .

The damping rings' main objectives are

- to accept electron and positron beams at large emittance and produce the low-emittance beams required for high-luminosity production.
- to dampen the incoming beam jitter to provide highly stable beams.
- to delay bunches from the source and allow feedforward systems to compensate for pulse-to-pulse variations in parameters such as the bunch charge.

Compared to today's fourth generation light sources, the target value for the normalized beam emittance  $(4 \,\mu\text{m}/20 \,\text{nm}$  for the normalised horizontal / vertical beam emittance) is low, but not a record value, and it is thus considered to be a realistic goal.

The main challenges for the damping ring design are to provide

- a sufficient dynamic aperture to cope with the large injected emittance of the positrons.
- a low equilibrium emittance in the horizontal plane.
- a very low emittance in the vertical plane.
- a small damping time constant.
- damping of instabilities from electron clouds (for the positron DR) and fast ions (for the electron DR).
- a small (3.2 6.4 ns) bunch spacing, requiring very fast kickers for injection and ejection.

Careful optimization has resulted in a TME (Theoretical Minimum Emittance) style lattice for the arcs that balances a low horizontal emittance with the required large dynamic aperture [15, Chap. 6]. Recently, the horizontal emittance has been reduced further by lowering the dispersion in the arcs through the use of longer dipoles [22]. The emittance in the vertical plane is minimised by careful alignment of the magnets and tuning of the closed orbit to compensate for misalignments and field errors, as demonstrated at the CESR-TA facility [80].

The required small damping time constant requires large synchrotron radiation damping, which is provided by the insertion of 54 wigglers in each ring. This results in an energy loss of up to 7.7 MV per turn and up to 3.3 MW RF power to store the positron beam at the design current of 390 mA. This actually exceeds the average beam power of the accelerated positron beam, 2.6 MW at a 250 GeV.

Electron cloud (EC) and fast ion (FI) instabilities limit the overall current in the damping rings to about 400 - 800 mA, where the EC limit that affects the positrons is

 $<sup>^2</sup>$  The vertical emittance of the positrons is reduced from  $\epsilon_{\rm y}\approx 0.8\,\mu{\rm m}$  to 2 pm.

assumed to be more stringent. These instabilities arise from electrons and ions being attracted by the circulating beam towards the beam axis. A low base vacuum pressure of  $10^{-7}$  Pa is required to limit these effects to the required level. In addition, gaps between bunch trains of around 50 bunches are required in the DR filling pattern, which permits the use of clearing electrodes to mitigate EC formation. These techniques have been developed and tested at the CESR-TA facility [81]

In the damping rings, the bunch separation is only 6.4 ns (3.2 ns for a luminosity upgrade to 2625 bunches). Extracting individual bunches without affecting their emittance requires kickers with rise/fall times of 3 ns or less. Such systems have been tested at ATF [82].

The damping ring RF system will employ superconducting cavities operating at half the Main Linac frequency (650 MHz). Klystrons and accelerator modules can be scaled from existing 500 MHz units in operation at CESR and KEK [15, Sec. 6.6].

### 2.3.3. Low emittance beam transport: ring to Main Linac (RTML)

The Ring to Main Linac (RTML) system [15, Chap. 7] is responsible for transporting and matching the beam from the Damping Ring to the entrance of the Main Linac. Its main objectives are

- transport of the beams from the Damping Rings at the center of the accelerator complex to the upstream ends of the Main Linacs,
- collimation of the beam halo generated in the Damping Rings,
- rotation of the spin polarisation vector from the vertical to the desired angle at the IP (typically, in longitudinal direction).

The RTML consists of two arms for the positrons and the electrons. Each arm comprises a damping ring extraction line transferring the beams from the damping ring extraction into the main linac tunnel, a long low emittance transfer line (LTL), the turnaround section at the upstream end of each accelerator arm, and a spin rotation and diagnostics section.

The long transport line is the largest, most costly part of the RTML. The main challenge is to transport the low emittance beam at 5 GeV with minimal emittance increase, and in a cost-effective manner, considering that its total length is about 14 km for the 250 GeV machine.

In order to preserve the polarisation of the particles generated in the sources, their spins are rotated into a vertical direction (perpendicular to the Damping Ring plane) before injection into the Damping Rings. A set of two rotators [83] employing superconducting solenoids allows to rotate the spin into any direction required.

At the end of the RTML, after the spin rotation section and before injection into the bunch compressors (which are considered part of the Main Linac, not the RTML [84]), a diagnostics section allows measurement of the emittance and the coupling between the horizontal and vertical plane. A skew quadrupole system is included to correct for any such coupling.

A number of circular fixed-aperture and rectangular variable-aperture collimators in the RTML provide betatron collimation at the beginning of the LTL, in the turn around and before the bunch compressors.

#### 2.3.4. Bunch compressors and Main Linac



FIG. 12: Artist's rendition of the ILC Main Linac tunnel. The shield wall in the middle has been removed. ©Rey.Hori/KEK.

The heart of the ILC are the two Main Linacs, which accelerate the beams from 5 to 125 GeV. The linac tunnel, as depicted in Figs. 12 and 13, has two parts, separated by a shield wall. One side (on the right in Fig. 12) houses the beamline with the accelerating cryomodules as well as the RTML beamline hanging on the ceiling. The other side contains power supplies, control electronics, and the modulators and klystrons of the High-Level RF system. The concrete shield wall (indicated as a darkgrey strip in in Fig. 12) has a thickness of 1.5 m [20]. The shield wall allows access to the electronics, klystrons and modulators during operation of the klystrons with cold cryomodules, protecting personnel from X-ray radiation emanating from the cavities caused by dark currents. Access during beam operation, which would require a wall thickness of  $3.5 \,\mathrm{m}$ , is not possible.

The first part of the Main Linac is a two-stage bunch compressor system [15, Sec. 7.3.3.5], each consisting of an accelerating section followed by a wiggler. The first stage operates at 5 GeV, with no net acceleration, the second stage accelerates the beam to 15 GeV. The bunch compressors reduce the bunch length from 6 to 0.3 mm.

After the bunch compressors, the Main Linac continues for about 6 km with a long section consisting entirely of cryomodules, bringing the beam to 125 GeV.



FIG. 13: Cross section through the Main Linac tunnel.

a. RF distribution: Each cryomodule contains 9 cavities, or for every third module, 8 cavities and a package with a superconducting quadrupole, corrector magnets, and beam position monitor. Nine such modules, with a total of 117 cavities, are powered by 2 klystrons and provide 3.83(4.29) GeV at a gradient of 31.5(35) MV/m. Table II gives an overview over the units that form the linacs. The waveguide distribution system allows an easy refurbishment to connect a third klystron for a luminosity upgrade. The 50 % RF power increase would allow 50 % higher current through smaller bunch separation, and longer beam pulses because of a reduced filling time, so that the number of bunches per pulse and hence the luminosity can be doubled, while the RF pulse duration of 1.65 ms stays constant.

b. Cryogenic supply: A 9 module unit forms a cryo string, which is connected to the helium supply line with a Joule-Thomson valve. All helium lines are part of the cryomodule, obviating the need for a separate helium transfer line. Up to 21 strings with 189 modules and 2.4 km total length can be connected to a single plant; this is limited by practical plant sizes and the gas-return header pressure drop.

Unit	Comprises	Length	Voltage
Cavity	$1.038\mathrm{m}$ active length	$1.25\mathrm{m}$	$32.6/36.2\mathrm{MV}$
Cryomodule	$8^2/_3$ cavities	$12.65\mathrm{m}$	$282/314{ m MV}$
RF Unit	4.5 cryomodules	$58.2\mathrm{m}$	$1.27/1.41{ m GV}$
Cryostring	2 RF units	$116.4\mathrm{m}$	$2.54/2.82{ m GV}$
Cryounit	up to 21 cryostrings	$2454\mathrm{m}$	$53.4/39.3\mathrm{GV}$

TABLE II: Units that make up the main linacs. The voltage takes into account that the beam is  $5^{\circ}$  shifted in phase ("off crest") for longitudinal stability, and is given for an average gradient of 31.5/35 MV/m. A RF unit is powered by one klystron, each cryostring is connected by a valve box to the liquid helium supply, and a cryounit is supplied by one cryogenic plant. Total lengths include additional space between components.

c. Cost reduction from larger gradients: Figure 14 shows the layout of the cryogenic supply system for the

250 GeV machine. At the top, the situation is depicted for the gradient of  $31.5 \,\mathrm{MV/m}$  with a quality factor of  $Q_0 = 1.0 \cdot 10^{10}$ , as assumed in the TDR [15]. In this case, the access points PM±10 would house two cryogenic plants, each supplying up to 189 cryomodules or an equivalent cryogenic load. In this configuration 6 large plants in the access halls plus 2 smaller plants in the central region would be needed. The bottom picture shows the situation for a gradient of 35 MV/m with  $Q_0 = 1.6 \cdot 10^{10}$ , as could be expected from successful R&D. The increased gradient would allow reduction of the total number of cryomodules by roughly 10% from 987 to 906. The increased quality factor would reduce the dynamic losses such that 4 cryo plants would provide sufficient helium.

In general, the accelerator is designed to make good use of any anticipated performance gain from continued high gradient R&D, in the case that raising the gradient is seen to be beneficial from an economical point of view, without incurring unwanted technology risk.

#### 2.3.5. Beam delivery system and machine detector interface

The Beam Delivery System (BDS) transports the  $e^+/e^$ beams from the end of the main linacs, focuses them to the required small beam spot at the Interaction Point (IP), brings them into collision, and transports the spent beams to the main dumps [15, Chap. 8]. The main functions of the BDS are

- measuring the main linac beam parameters and matching it into the final focus.
- protecting beamline and detector from mis-steered beams  $^{3}$ .
- removing large amplitude (beam-halo) and offmomentum particles from the beam to minimize background in the detector.
- accurately measuring the key parameters energy and polarisation before and after the collisions.

The BDS must provide sufficient diagnostic and feedback systems to achieve these goals.

The BDS is designed such that it can be upgraded to a maximum beam energy of 500 GeV; components such as the beam dumps, that are not cost drivers for the overall project but would be cumbersome to replace later, are dimensioned for the maximum beam energy from the beginning. In other places, such as the energy collimation dogleg, those components necessary for 125 GeV beam operation are installed and space for a later upgrade is reserved.

<sup>&</sup>lt;sup>3</sup> On the electron side, the protective fast beam abort system is actually located upstream of the positron source undulator.



FIG. 14: Cryogenic layout for a gradient of 31.5 MV/m (top) and 35 MV/m (bottom) [2]. "Module space" indicates how many cryomodules can be physically installed, "cryomodules" and "RF unit" indicates the number of actually installed modules and klystrons (one klystron per 4.5 cryomodules). "E gain" indicates the energy gain in GeV. "BC", "ML", "e+inj", "e- inj" and "UND" refer to the sections with need for liquid helium: bunch compressor, main linac, 5GeV boosters in the positron and electron source, and the positron source undulator section, respectively. PM±8, 10, 12 refer to access hall locations, "C" to cryo plants; meter numbers on top indicate the length of the corresponding section.

Overall, the BDS is 2254 m long from the end of the main linac (or the undulator and target bypass insert of the positron source on the electron side, respectively) to the IP.

a. Diagnostics and collimation section: The BDS starts with a diagnostics section, where emittance, energy and polarisation are measured and any coupling between the vertical and horizontal planes is corrected by a set of skew quadrupoles. The energy measurement is incorporated into the machine protection system and can, *e.g.*, extract off-momentum bunches caused by a klystron failure in the main linac that would otherwise damage the machine or detector. An emergency dump [21] is dimensioned such that it can absorb a full beam pulse at

500 GeV, sufficient for 1 TeV operation.

The diagnostics section is followed by a collimation system, which first removes beam halo particles (betatron collimation). Then, off-momentum particles are removed. In this energy collimation section, sufficient dispersion must be generated by bending the beam in a dogleg, while avoiding excessive synchrotron radiation generation in dispersive regions that leads to an increase of the horizontal emittance. This emittance dilution effect grows as  $E_{\rm beam}^6$  at constant bending radius for the normalised emittance, and determines the overall length of the energy collimation section for a maximum 500 GeV beam energy to about 400 m. b. Final focus with feedback system and crab cavities: The final focus system demagnifies the beam to the required spot size of  $516 \times 7.7 \,\mathrm{nm^2}$  by means of a final quadrupole doublet. Even the relatively small energy spread of  $\approx 0.1\%$  leads to a significant spread of the focal length of the doublet and requires a correction to achieve the desired beam size, which is realised by a local chromaticity correction scheme [85].

To bring the beams to collision with the neccessary nanometre accuracy requires a continuous compensation of drift and vibration effects. Along the ILC, the pulse length and bunch separation (727  $\mu$ s and 554 ns, respectively) are large enough to allow corrections between pulses as well as within a bunch train (intratrain feedback). Beam-beam offsets of a fraction of the beam size lead to a measurable deflection of the outgoing beams, and these measurements are used to feed fast stripline kickers that stabilize the beam. Finally, the 3.9 GHz crab cavities close to the interaction point are incorporated that rotate the bunches to compensate for the 14 mrad beam crossing angle [15, Sect. 8.9].

c. Test results from ATF2: The Accelerator Test Facility 2 (ATF2) was built at KEK in 2008 as a test bench for the ILC final focus scheme [14, Sec. 3.6]. Its primary goals were to achieve a 37 nm vertical beam size at the interaction point (IP), and to demonstrate beam stabilisation at the nanometre level [86, 87]. After scaling for the different beam energies (ATF2 operates at  $E_{\text{beam}} = 1.3 \text{ GeV}$ ), the 37 nm beam size corresponds to the TDR design value of  $\sigma_y^* = 5.7 \text{ nm}$  at 250 GeV beam energy. As Fig. 15 shows, this goal has been reached within 10% [88] by the successive application of various correction and stabilisation techniques, validating the final focus design, in particular the local chromaticity correction [89].

The fifth generation FONT5 feedback system [90] for the ILC and CLIC has also been tested at the ATF2, where a beam stabilisation to 41 nm has been demonstrated [91].

Since November 2016, intensity-dependence effects on the ATF2 beam size have been studied extensively. They show a degradation of the beam size with increasing intensity that is compatible with the effect of wakefields. Simulations and experiments in ATF2 show that the effect is not important when scaled to ILC. Also, it could be mitigated by including a dedicated "wakefield knob" in the routine tuning procedure.

d. Machine detector interface (MDI): The ILC is configured to have two detectors that share one interaction point, with one detector in data taking position at any time, in a so-called "push-pull" operation [14, Sec. 8.4]. Both detectors are mounted on movable platforms that allow an exchange of the detectors within approximately 24 hours.

In the push–pull scheme, the innermost final focus quadrupole "QD0", a slim, superconducting magnet package combined with a sextupole for local chromaticity correction, is installed within the detectors. The other



FIG. 15: Beamsizes achieved at the Accelerator Test Facility 2 (ATF2) as a function of time [92]. The latest result (41 nm [88]) is within 10% of the goal beam size of 37 nm.

part of the final focus doublet ("QF1") is located outside the detector on a bridge, and does not move with the detector. Since the TDR, the free space  $L^*$  between interaction point and the QD0 edge has been harmonised to a common value of  $L^* = 3.5 \text{ m}$  [18], which facilitates the design of a final focus optics that delivers optimal and equal performance to both detectors.

The detectors are located in an underground cavern. In contrast to the TDR design, it is foreseen to have a large vertical access shaft [19], which permits a CMS–style detector installation concept, in which the detectors are assembled in large modules in a surface hall and lowered into the hall by means of a gantry crane capable of lowering pieces up to 4000 t. As the CMS experience shows, this concept significantly reduces the schedule risk associated with the experimental hall, since the cavern needs to be available for detector installation only one or two years prior to commissioning.

e. Main dump: The main beam dumps [15, Sect. 8.8] are rated for a maximum beam power of 17 MW [21], enough for a 1 TeV upgrade of the accelerator. The main dump design is based on the successful SLAC 2.2 MW beam dump [93]. It utilises water at 10 bar pressure (to prevent boiling) as absorber medium. The main engineering challenges lie in the safe recombination of the produced oxyhydrogen gas and in the safe containment and disposal of radioisotopes, in particular tritium and <sup>7</sup>Be produced from spallation processes. The entry window is another component that has to be carefully designed.

f. Measurement of beam energy, luminosity, and beam polarisation: Two energy spectrometers, one located 700 m upstream of the IP, the other 55 m downstream, provide independent and complementary measurements of the beam energy with an accuracy of 100 ppm [94].

The luminosity is measured to  $10^{-3}$  accuracy from low angle Bhabha scattering in the so-called LumiCal (see Sect. 6.2.5) at polar angles from 30 to 90 mrad. Additional calorimeters (BeamCal) in the region 5 to 30 mrad provide a fast signal that is sensitive to the beam sizes and offsets of the colliding beam, and that can thus be used for their tuning, as part of an intra-beam feedback system (see Sec. 2.3.5).

Beam polarisation is measured with 0.25% accuracy

by means of Compton scattering: electrons that scatter off green or infrared light laser photons lose enough energy that they can be detected in a spectrometer; their momentum spectrum is used to fit the beam polarisation [95]. Two such polarimeters are located 1800 m upstream and 150 m downstream of the IP, which allows to interpolate the precise polarisation at the IP and control the systematics, including effects from precession of the polarisation vector by transverse fields and depolarising effects in the interaction, which lead to a sizeable variation of the polarisation within the bunch during the collision (see Sect. 8.3.1).

#### 2.4. Upgrade options

Given the high initial investment for a facility as large as the ILC, it is mandatory to have an interesting physics programme for several decades, with the possibility to adapt the programme to the needs arising from the knowledge obtained by the LHC, the ILC itself, all other particle physics experiments, and other domains of physics such as cosmology. Several options exist for upgrades of the ILC in terms of energy, luminosity, and beam polarisation.

#### 2.4.1. Energy upgrade

The obvious advantage of a linear collider is its upgradeability in energy. Basically, the main linacs can be extended as far as desired, at constant cost per added beam energy, with some added cost for the relocation of the turn arounds and bunch compressors. Additional costs arise when the beam delivery system (BDS), including the beam dumps, has to be extended to handle the increased beam energy. The current ILC BDS is designed to be easily upgradeable for centre of mass energies up to 1 TeV at minimal cost.

Depending on the actual gradient achieved for the construction of the ILC, up to 171 cryomodules could be installed in addition to those needed to reach 250 GeV, which would increase the centre-of-mass energy by about 54 GeV to around 304 GeV, as Fig. 14 shows, and possibly require the installation of two additional cryo plants.

A further energy upgrade would require extension of the tunnel. The Kitakami site can accommodate a total accelerator length of at least 50 km, more than enough for a 1 TeV centre–of–mass energy. Any extension of the accelerator would proceed by adding new cryomodules at the low energy (upstream) ends of the accelerator. There is no need to move modules already installed.

An upgrade would likely proceed in two phases: a preparation phase while the accelerator is still operated and produces data, and a refurbishment phase where the accelerator is shut down.

During the preparation phase, the necessary components—in particular the cryomodules, klystrons, and modulators—would be acquired and built. At the same time, civil engineering would proceed with the excavation of new access tunnels, underground halls, and the main tunnel. Recent studies conducted during road tunnel construction in the Kitakami area, in the same rock formation as foreseen for the ILC, indicate that the level of vibrations caused by tunnelling activities would allow to bring the new tunnels quite close to the existing ones before machine operation would be affected [96], minimising the shutdown time necessary.

During the installation phase, the newly built tunnels would be connected to the existing ones, the beam lines at the turn-around and the wiggler sections of the bunch compressors would be dismantled, and the new cryomodules would be installed as well as the new turn-around and bunch compressors. At the same time, any necessary modifications to the positron source and the final focus can be made. With the cryomodules ready for installation at the beginning of the shut down period, it is estimated that the shutdown could be limited to about a year for an energy upgrade.

#### 2.4.2. Luminosity upgrade

The luminosity of the ILC can be increased by increasing the luminosity per bunch (or per bunch charge), or increasing the number of bunches per second [97].

Increasing the luminosity per bunch requires a smaller vertical beam spot size, which may be achieved by tighter focusing and/or smaller beam emittance. Studies indicate that with enough operating experience, there is potential for a further luminosity increase. This route to increased luminosity is, however, invariably linked to higher beam disruption, which brings a risk of a luminosity loss due to mis-steering the beam. Thus, a very accurate feedback system is required.

The ILC design also has the potential to increase the number of colliding bunches per second, by doubling the number of bunches per pulse, and possibly by increasing the pulse repetition frequency.

Doubling the number of bunches per pulse to 2625 would require a smaller bunch spacing, requiring the installation of 50 % more klystrons and modulators. Since the RF pulse length of 1.65 ms is unchanged, the cryogenic load is essentially unchanged. Doubling the number of bunches would double the beam current in the damping rings. For the positron damping ring, this may surpass the limitations from electron cloud (EC) instabilities. To mitigate this risk, the damping ring tunnel is large enough to house a third damping ring, so that the positron current could be distributed over two rings.

The pulse repetition rate (5 Hz in the baseline configuration) is limited by the available cryogenic capacity, the damping time in the damping rings, and the target heat load in the positron source target. The damping rings are designed for a 100 ms damping time and thus capable of a repetition rate of up to 10 Hz, twice the nominal rate. Operation at an increased repetition rate would be possible if after an energy upgrade the machine is operated below its maximum energy (e.g., 250 GeV operation of a 500 GeV machine for a larger low-energy data set), or if additional cryogenic capacity is installed.

#### 2.4.3. Polarisation upgrade

The baseline design foresees at least 80% electron polarisation at the IP, combined with 30% positron polarisation for the undulator positron source. At beam energies above 125 GeV, the undulator photon flux increases rapidly. Photon polarisation is maximal at zero emission angle; it is decreased and even inverted at larger angles. Thus, collimating the surplus photon flux at larger emission angles increases the net polarisation. Studies indicate that 60% positron polarisation at the IP may be possible at 500 GeV centre–of–mass energy with the addition of a photon collimator.

#### 2.5. Civil engineering and site

In 2014, the ILC Strategy Council announced the result of its candidate site evaluation for the best possible ILC site in Japan [98]. The evaluation was conducted by a number of Japanese experts from universities and industry, and reviewed by an international commitee. It considered technical as well as socio-environmental aspects, and concluded that the candidate site in the Kitakami region is best suited for the ILC.



FIG. 16: The Kitakami candidate site for the ILC [99].

The site (Fig. 16) is located in the Japan's northern Tohoku region, not far from Sendai with its international airport, in the prefectures of Iwate and Miyagi. The closest cities are Ichinoseki, Oshu, and Kitakami, which all offer Shinkansen (bullet train) access to Sendai and Tokyo. The closest harbour is in the city of Kesen-Numa. The coastal region in this area was severely hit by the great Tohoku earthquake in 2011. Both prefectures are supportive of the ILC project and view it as an important part of their strategy to recover from the earthquake disaster. The Kitakami site was largely selected because of its excellent geological condition. The proposed ILC trajectory lies in two large, homogeneous granite formations, the Hitokabe granite in the north and Senmaya granite to the south. The site provides up to 50 km of space, enough for a possible 1 TeV upgrade or more, depending on the achievable accelerating gradient. Extensive geological surveys have been conducted in the area, including boring, seismic measurements, and electrical measurements [100], as shown in Fig. 17. The surveys show that the rock is of good quality, with no active seismic faults in the area.

Earthquakes are frequent throughout Japan, and the accelerator and detectors need proper supports that isolate them from vibrations during earthquakes and micro tremors [101]. Proven technologies exist to cope with all seismic events, including magnitude 9 earthquakes such as the great Tohoku earthquake.

Vibration measurements taken during the construction of a road tunnel show that accelerator operation would be possible during the excavation of a tunnel for an energy upgrade [102].



FIG. 17: Geological situation at the Kitakami site.

#### 2.6. Cost and schedule

For the Technical Design Report, the construction cost of the ILC accelerator was carefully evaluated from a detailed, bottom-up, WBS (Work Breakdown Structure)based cost estimation [15, Sect. 15]. The TDR estimate distinguishes two cost categories: Value accounts for materials and supplies procured from industry and is given in ILCU (ILC Currency Unit, where 1 ILCU = 1 US\$ in 2012 prices), and Labour accounts for work performed in the participating institutions and is given in personhours or person-years<sup>4</sup>.

<sup>&</sup>lt;sup>4</sup> One person–year corresponds to 1700 working hours.



FIG. 18: Breakdown of Value costs into accelerator systems (left) and technical systems (right) for the 250 GeV ILC accelerator, assuming that cost reduction measures are successful and a gradient of 35 MV/m can be reached.

The Value of acquired goods reflects its worth in the local currency of the purchasing institution. Therefore, conversion of Value between currencies is performed based on Purchasing Power Parities (PPP), which are regularly evaluated and published by the OECD [103, 104], rather than currency exchange rates. The PPP values reflect local price levels and thus depend on the type of goods and the country, but fluctuate significantly less than currency exchange rates. Therefore, conversions from ILCU to other currencies cannot not be made on the basis of exchange rates to the U.S. dollar, but on PPP values.

The TDR estimate covers the cost of the accelerator construction, assumed to last 9 years plus one year of commissioning. It includes the cost for the fabrication, procurement, testing, installation, and commissioning of the whole accelerator, its components, and the tunnels, buildings *etc.*, and the operation of a central laboratory at the site over the construction period. It does not, however, cover costs during the preparation phase preceding the start of construction work ("ground breaking"), such as design work, land acquisition, infrastructure (roads, electricity, water) for the site.

Based on the TDR cost estimate, an updated cost estimate was produced for the 250 GeV accelerator. This updated cost estimate includes the cumulative effect of the changes to the design since the TDR (see Sect. 2.1), and evaluates the cost for the reduced machine by applying appropriate scaling factors to the individual cost contributions of the TDR cost estimate.

The resulting Value estimate for the ILC accelerator at 250 GeV is 4,780-5,260 MILCU [2] in 2012 prices, where the lower number assumes a cavity gradient of 35 MV/m, while the higher number is based on the TDR number of

 $31.5 \,\mathrm{MV/m}$ . In addition,  $17,165 \,\mathrm{kh}$  (thousand personhours) are required of institutional Labour.

In 2018, the ILC Advisory Panel of the Japanese Ministry of Education, Culture, Sports, Science and Technoloy (MEXT) concluded its review of the ILC [105]. For this review, costs were evaluated in Japanese Yen in 2017 prices, taking into account the local inflation for goods and construction costs. For the purpose of this estimate, also the Labour costs were converted to Yen to yield 119.8 G¥, resulting in a total range of the accelerator construction cost of  $635.0 - 702.8 \,\text{G¥}$ , where the range covers uncertainties in the civil construction costs (18 G¥) and of the gradient (49.8 G¥). For the this estimate, conversion rates of 1 US\$ = 100 JP¥ and  $1 \in = 1.15 \,\text{US}$ \$ were assumed.

Operation costs of the accelerator and the central laboratory are estimated to be  $36.6 - 39.2 \,\text{G}$  (about  $318 - 341 \,\text{M}$ ) per year.

### 3. ILC RUNNING SCENARIOS

One of the key advantages of  $e^+e^-$  colliders is the ability to collect individual datasets at a series of different center-of-mass energies and beam polarisation settings. While each measurement one might wish to make has its own prefered data-taking mode, the combination with datasets collected at other beam energies and/or beam polarisations provides a unique robustness against systematic uncertainties. For example, a recent PhD thesis [106] studied Dark Matter searches with consideration of non-neglibigle systematic uncertainties and showed that one obtains better results by sharing a given amount of total integrated luminosity between datasets with dif-



FIG. 19: The nominal 22-year running program for the staged ILC, starting operation at 250 GeV with the current baseline beam parameters for the 250 GeV runs [4].

ferent beam polarisations rather than by investing the same total amount of luminosity into the (statistically) most favourable polarisation configuration.

Any physics projection will therefore depend on the exact running scenario, i.e. the ensemble of the integrated luminosities collected at the individual center-of-mass energies with the various polarisation settings. The ILC as currently under political consideration in Japan will be limited to a center-of-mass energy of 250 GeV. Already at this energy, the ILC offers a formidable physics programme, which is described in detail in the following Sec. 4. The intrinsic upgradability to higher energies, however, is a key feature of a linear collider, which clearly sets it apart from any circular  $e^+e^-$  collider. In order to illustrate the full potential of the ILC, the upgrade options introduced in Sec. 2.4 are therefore included in the running scenarios. The timelines presented here are based on technological possibilities and physics requirements only, and do not include funding considerations.

For the physics conclusions given in this paper, we have assumed the energy and luminosity evolution of the ILC shown in Fig. 19. At each energy, the time is shared among the various choices for beam polarization in the manner explained in Sec. 3.2. The full physics program is projected to take 22 years, including a realistic learning curve for the establishment of luminosity and scheduled downtimes for luminosity and energy upgrades. In this schedule, the ILC would accumulate  $2 \text{ ab}^{-1}$  at 250 GeV by year 11. It woud then add datasets of  $0.2 \text{ ab}^{-1}$  at 350 GeV and  $4 \text{ ab}^{-1}$  at 500 GeV by year 22.

The interplay between different datasets has been studied in detail in [107], with a special focus on the optimisation of the Higgs precision measurements, resulting in a standard running scenario for ILC physics projections. The time evolution of this running scenario has been adapted to the staged construction of the ILC as first presented in [4].

In this section, we will discuss the considerations that

have led to the choice of this running scenario, the evolution of this scenario in accord with the design of the ILC accelerator, and the flexibility of the plan to respond to changes in machine specifications or physics discoveries.

## 3.1. Center-of-mass energies and integrated luminosities

The three center-of-mass energies for ILC best motivated by our current knowledge are:

- $\sqrt{s} = 250 \,\text{GeV}$  for collecting data near the threshold of the Higgsstrahlungs process,
- $\sqrt{s} = 350 \,\text{GeV}$  for scanning the threshold for top quark pair production, and
- $\sqrt{s} = 500 \,\text{GeV}$  or somewhat above for studying  $t\bar{t}$  production in the continuum and enabling  $t\bar{t}H$  and ZHH production.

Table III gives the total integrated luminosities foreseen at these energies for three alternative running scenarios. These scenarios are described in [107], which presented a detailed evaluation of these and other possibilities. For comparison, the integrated luminosities assumed in the Snowmass community study [108] is given in the last column. Since 2015, the scenario H20 has been the reference scenario for ILC physics projections.

	$\int \mathcal{L} dt   [\mathrm{fb}^{-1}]$					
$\sqrt{s}$	G20	H20	I20	Snow		
$250{ m GeV}$	500	2000	500	1150		
$350{ m GeV}$	200	200	1700	200		
$500{ m GeV}$	5000	4000	4000	1600		

TABLE III: Proposed total target integrated luminosities for  $\sqrt{s} = 250, 350, 500 \text{ GeV}$  based on 20 "real-time" years of ILC operation under scenarios G20, H20 and I20. The total integrated luminosities assumed for Snowmass are listed for comparison based on 13.7 "real-time" years. From [107].

It must be stressed, however, that flexibility in the run plan remains one of the key assets of the ILC. This plan can be adjusted whenever new insights, discoveries either from the (HL-)LHC or from the ILC itself, require us to do so. In particular, the center-of-mass energy of the ILC can always be lowered from the nominal maximum energy without loss of efficiency, as long as the electron beam energy remains sufficiently high for positron production. In fact, the operation of the SCRF cavities below the maximum gradient saves significant cryogenic and RF power, which in turn can be invested into higher instantaneous luminosity.

Future  $e^+e^-$  colliders could also provide important physics measurements at other center-of-mass energies. Physics goals that motivate other choices are the highstatistics study of Z and W, the exploration of the thresholds for any new color-singlet particles that might appear in the ILC energy region, and data-taking at additional center of mass energies to optimize the determination of Effective Field Theory parameters. The lower center-of-mass energies could be realized by doubling the repetition rate of the electron linac to 10 Hz and adding a by-pass around the positron source for every second bunch train. Today, however, the priority of these issues seems lower than that for the abovementioned three energies. Therefore they are not explicitly included in the current run plan of the ILC or in the current set of machine parameters. Over a longer term, we plan to extend the linac to reach energies of 1 TeV or higher. Table IV lists target integrated luminosities approriate to physics studies at these additional energies.

$\sqrt{s}$	$90{ m GeV}$	$160{ m GeV}$	$1\mathrm{TeV}$
$\int \mathcal{L} dt \; [\mathrm{fb}^{-1}]$	100	500	8000

TABLE IV: Proposed total target integrated luminosities for other  $\sqrt{s}$ . From [107].

#### 3.2. Beam polarisation

At center-of-mass energies of up to 500 GeV, the ILC beams are foreseen to be polarised with absolute values of at least 80% for the electrons and at least 30% for the positrons. At  $1 \,\mathrm{TeV}$ , the positron polarisation will reach at least 20%. As an upgrade option, the positron polarisation can be increased to 60% for center-of-mass energies around 500 GeV; this is discussed in Sec. 2.4.3. The accelerator design comprises sets of spin rotators which in principle allow one to prepare any desired direction of the polarisation vectors at the IP. However in the detailed running scenarios, we consider only longitudinal polarisation. The sign of the beam polarisations can be flipped on a train-by-train basis. This allows us to collect datasets with different helicity configurations quasi-concurrently compared to the typical time scales of changes in the accelerator or detector configuration, calibration and alignment. In a joint analysis of these datasets, large parts of the experimental systematic uncertainties cancel. This is particularly important to minimize the systematic errors in the measurement of the left-right polarization asymmetry, a quantity that carries a great deal of information for every process that will be studied at the ILC. But this idea has many other applications. The joint interpretation of the different datasets allows us to treat many systematic effects as nuisance parameters in global fits, and thereby to measure and subtract these effects [109].

The role of positron polarisation specifically at an initial 250-GeV stage of the ILC has been discussed in detail in a recent document [110]. In the case of a global fit to polarised total and differential cross-sections of various electroweak processes, it is shown there that the uncertainties on some observables increase by up to a factor of 10 in the absence of positron polarisation due to the lack of redundancies required for ultimate control of systematic uncertainties (see Sec. 8.3). As we will see in Sec. 4.6, the left-right asymmetry  $A_{LR}(HZ)$  of the Higgsstrahlungs cross section plays an important role in our technique for obtaining a model-independent fit to Higgs couplings. Although the measurement of the absolute normalization of the Higgsstrahlungs cross section was not explicitly included in the study summarized in [110], analogous deteriorations would also be expected for this quantity.

A part of the power of positron polarisation is that it allows one to collect four independent data sets with different mixtures of the physics reactions under study. Tables V through VIII give our standard assumptions for the sharing of the total integrated luminosity (c.f. Tab. III and IV) between the four possible beam helicity combinations. Due to the importance of  $A_{LR}(HZ)$  [3, 111] noted above, the sharing for 250 GeV, which was originally foreseen [107] to emphasize the sgn( $P(e^-), P(e^+)$ ) = (-, +) configuration, is now adjusted to provide equal amounts of luminosity for (-, +)and (+, -) [3, 4].

These integrated luminosities and polarisation configurations, especially as specified in Tab. VI for the H20 running scenario, define the reference scenario for all ILC physics projections. The order in which the various energies are surveyed will of course depend on the machine evolution and staging plan.

	fraction with $sgn(P(e^{-}), P(e^{+})) =$				
	(-,+)	(+,-)	(-,-)	(+,+)	
$\sqrt{s}$	[%]	[%]	[%]	[%]	
$250 \mathrm{GeV} \ (2015)$	67.5	22.5	5	5	
$250\mathrm{GeV}$ (update)	<b>45</b>	<b>45</b>	5	5	
$350{ m GeV}$	67.5	22.5	5	5	
$500{ m GeV}$	40	40	10	10	

TABLE V: Relative sharing between beam helicity configurations proposed for the various center-of-mass energies. The update of the luminosity sharing for 250 GeV originates from the importance of the left-right asymmetry of the Higgsstrahlung cross section in the EFT-based Higgs coupling fit.

	int. luminosity with $sgn(P(e^{-}), P(e^{+})) =$				
	(-,+)	(+,-)	(-,-)	(+,+)	
$\sqrt{s}$	$[{\rm fb}^{-1}]$	$[{\rm fb}^{-1}]$	$[{\rm fb}^{-1}]$	$[{\rm fb}^{-1}]$	
$250 \mathrm{GeV} \ (2015)$	1350	450	100	100	
$250\mathrm{GeV}$ (update)	900	900	100	100	
$350{ m GeV}$	135	45	10	10	
$500{ m GeV}$	1600	1600	400	400	

TABLE VI: Integrated luminosities per beam helicity configuration resulting from the fractions in table V in scenario H20. The update of the luminosity sharing for 250 GeV originates from the importance of the left-right asymmetry of the Higgsstrahlung cross section in the EFT-based Higgs coupling fit.

	fraction with $sgn(P(e^{-}), P(e^{+})) =$					
	(-,+)	(+,-)	(-,-)	(+,+)		
$\sqrt{s}$	[%]	[%]	[%]	[%]		
$90{ m GeV}$	40	40	10	10		
$160{ m GeV}$	67.5	22.5	5	5		
$1\mathrm{TeV}$	40	40	10	10		

TABLE VII: Relative sharing between beam helicity configurations proposed for low energy and 1 TeV running. From [107].

	integrated	luminosity wi	th $\operatorname{sgn}(P(e^{-}))$	$), P(e^+)) =$
	(-,+)	(+,-)	(-,-)	(+,+)
$\sqrt{s}$	$[\mathrm{fb}^{-1}]$	$[{\rm fb}^{-1}]$	$[{\rm fb}^{-1}]$	$[{\rm fb}^{-1}]$
$90{ m GeV}$	40	40	10	10
$160{ m GeV}$	340	110	25	25
$1\mathrm{TeV}$	3200	3200	800	800

TABLE VIII: Integrated luminosities per beam helicity configuration resulting from the fractions in table VII. From [107].

#### 3.3. Time evolution and upgrade options

The possible real-time evolution of the integrated luminosity was studied in detail in [107]. It is important to note that the plans given in that study assumed that the full 500 GeV machine would be available from the beginning. With the introduction of a staged construction plan for the ILC, the time ordering of different runs needed to be adjusted. However, the details of trade-offs between scenarios is most fully documented in [107], so we will first review that study and the logic of its conclusions. After this, we will describe our current plan for the run scenario including the constraints from staging.

#### 3.3.1. Running scenarios for the 500-GeV Machine

In the study [107], the peak luminosities used for each centre-of-mass energy are based on the numbers published in the ILC TDR [14]. But then, the plans took advantage of the reduced linac electrical power and cryogenic loads when operating the full 500 GeV machine at lower gradients. This in particular allows 10-Hz and 7-Hz running, respectively, at the 250 GeV and 350 GeV centre-of-mass energies. In addition, a luminosity upgrade (from 1312 to 2625 bunches per pulse) was been considered; this could require the installation of an additional positron damping ring, as described in Sec. 2.4.2.

More specifically, the study [107] made the following assumptions:

• A full calendar year is assumed to represent eight months running at an efficiency of 75% as assumed in the ILC RDR [112]. This corresponds approximately to  $Y = 1.6 \times 10^7$  seconds of integrated running, thus 60% more than a "Snowmass year" of  $10^7$  seconds.

- The start of "Year 1" is the start of running for physics. After the end of construction, there is one year foreseen for machine commissioning only, which is not shown on the plots.
- A ramp-up of luminosity performance, defined as a set of yearly ramp factors  $f \leq 1$ , is in general assumed after: (a) initial construction and 'year 0' commissioning; (b) a downtime for a luminosity upgrade; (c) a change in operational mode which may require some learning curve (*e.g.*, going to 10-Hz collisions).
- If the peak instantaneous luminosity is L, then the nominal integrated luminosity for any given calendar year is  $\int \mathcal{L}dt = f \times L \times Y$ , where f is the ramp factor associated with that year.
- The peak instantaneous luminosities are those corresponding to the TDR beam parameters at 250, 350 and 500 GeV, as shown in Tab. I.
- For the initial physics run after construction and year 0 commissioning, the RDR ramp of 10%, 30%, 60% and 100% over the first four calendar years is always assumed.
- The ramp after the shutdown for installation of the luminosity upgrade is assumed to be slightly shorter (10%, 50%, 100%) with no year 0.
- Going down in centre of mass energy from 500 GeV to 350 GeV or 250 GeV is assumed to have no ramp associated with it, since there is no modification (shutdown) of the machine.
- Going to 10-Hz operation at 50% gradient does assume a ramp however (25%, 75%, 100%), since 10-Hz affects the entire machine including the damping rings and sources.

Under these assumption, a possible real-time scenario for collecting the integrated luminosities of the H20 scenario (c.f. Tab III) is shown in Fig. 20. Since it was assumed that the full 500-GeV machine would be available from the start, the first foreseen run was intended to collect a dataset of  $500 \,\mathrm{fb}^{-1}$  at  $\sqrt{s} = 500 \,\mathrm{GeV}$  in order to observe for the first time ever  $t\bar{t}$  production via the electroweak force, to survey the full kinematic reach for possible new particles and, last but not least, to collect a comprehensive set of Higgs precision data, with similar contributions from the Higgsstrahlung and WW fusion processes (see Fig. 44).

After this general-purpose survey at the maximum energy, it was planned to collect dedicated datasets at lower energies, at the  $t\bar{t}$  production threshold, for a precision determination of a theoretically well-defined top mass, and somewhat above the ZH production threshold, near the maximum of the cross section. The ZH measurements at 250 GeV would be a very important component of the program even under the assumption that energies



FIG. 20: The nominal 20-year running program for the 500-GeV ILC [107].

of 500 GeV are immediately available. This is true for two reasons. First, in Higgsstrahlung production, each Higgs boson is tagged by the recoil Z. There are many measurements that rely on this tag to identify Higgs bosons or to measure absolute rates without the need to make assumptions about the Higgs decay modes. These include the measurement of the normalised total cross section for the Higgsstrahlung process, the measurement of absolute branching ratios of the Higgs boson and the search for invisible and exotic decays. At 500 GeV, far above the threshold, recoil measurements become less characteristic, due to the more substantial ISR and increased amount of beamstrahlung with respect to 250 GeV, and are subject to additional backgrounds. Other measurements depend on precise reconstruction of the kinematics of the  $e^+e^- \rightarrow ZH$  process. For example, the ultimate precision on the Higgs mass will be obtained using the kinematics of Z recoil. The search for deviations from the SM predictions for Higgs decays requires as input a very precise value of this mass; see Sec. 8.2.1. Another reaction that depends crucially on precise kinematic measurements is the CP analysis of the  $H \to \tau^+ \tau^-$  decay, discussed in Sec. 8.2.8.

For a 500 GeV machine running at 250 GeV, the luminosity can be straightforwardly increased by a factor of 2 from the TDR value by the increase of the repetition rate for bunch trains from 5 to 10 Hz. This improvement was incorporated in the plan H20 shown in Fig. 20 even at the initial stage of 250 GeV running.

The H20 plan also included provision for an additional luminosity upgrade by doubling the number of bunches in each bunch train. This upgrade requires machine improvements as described in Sec. 2.4.2, and after these improvements all further data would be taken in this mode. This would give a total  $4 \text{ ab}^{-1}$  data sample at 500 GeV. A sample of this size is required for meaningful precisions on the top Yukawa coupling and on the Higgs self-coupling. These measurements remain by far statistically limited and thus would profit from any further increase

of the luminosity. In case of the top Yukawa coupling, it was noted that it is absolutely crucial to reach 500 GeV, since already at 490 GeV, thus when falling short of the target energy by only 2%, the precision of the measurement would worsen by nearly a factor of 2. On the other hand, a moderate increase of the center-of-mass energy by 6% to 530 GeV would improve the precision on the top-Yukawa coupling by a factor of 2. This should be considered in the planning of the energy upgrade of an inital 250 GeV machine, see also discussion in Sec. 2.4.1.

Finally the H20 scenario planned a run at 250 GeV, now with 4 times the TDR luminosity, to finish the collection of a  $2 \text{ ab}^{-1}$  data set. This run would provide the ultimate precision on the Higgs boson mass and the total ZH cross section. It should be stressed again that the current focus on three fixed center-of-mass energies does not preclude running at any other desired intermediate energy, *e.g.* for scanning the production threshold of newly discovered particles.

At the end of this 20 year program, we envision a further doubling of the energy to 1 TeV. This upgrade was presented already in the ILC TDR and is reviewed in Sec. 2.4.1. This energy upgrade could possibly be preceeded by a run at the Z pole if it is required by the physics.

#### 3.3.2. Running scenarios for the staged machine

With the introduction of the staging plan for the ILC machine construction, it was necessary to change the time ordering of the various energy steps in the program described in the previous subsection. However, the total integrated luminosities to be collected at each centerof-mass energy, which were already optimized for the physics goals, were left untouched. Thus, all physics projections based on the H20 scenario remained valid albeit the results will arrive in a different time order. Figure 21 shows the original plan for the time evolution of the staged H20 scenario. The assumptions differ from those listed in the previous subsection in the following points:

- No 10 Hz operation is assumed since in the 250 GeV machine the cryomodules will be operated at full gradient and thus no spare cryo- and RF-power is available. Technically, it would be possible to increase the repetition rate (and thus the luminosity) at any time provided that resources for installing the additional cryo- and RF-power and for covering the higher operation costs could be found. This option is *not* included in the staging scenario.
- The luminosity upgrade by doubling the number of bunches per train (c.f. Sec. 2.4.2) is a smaller investment than the energy upgrade and will therefore happen first. In this plan, the second positron damping ring and the additional cryo- and RFpower needed for the luminosity doubling would



FIG. 21: The nominal 26-year running program for the staged ILC, starting operation at 250 GeV without the possibility to operate at 10 Hz [4]. The integrated luminosities are the same of for the original H20 scenario.

already be installed at the start of 500 GeV operation. Then the entire 500 GeV run would be done at 2 times the TDR luminosity.

- The energy upgrade (described in Sec. 2.4.1) requires only a relatively short machine shutdown of about one year, since major parts of the new tunnel can be constructed and the new parts of the machine can be installed without disturbing the operation of the 250-GeV machine. A shutdown is necessary only during the construction of the connections of the new parts of the machine to the older ones.
- After the energy upgrade the same ramp fractions as for a completely new machine are assumed, thus 10%, 30%, 60% and 100% over the first four calendar years.

With these assumptions, the real-time for realization of the full H20 program increases from 20 to 26 years, mostly due to the much longer time to collect the  $2 \text{ ab}^{-1}$  at 250 GeV without 10 Hz operation.

In order to mitigate the absence of the 10 Hz operation, which would require additional investments beyond the minimal 250-GeV machine, cost neutral ways to increase the luminosity at 250 GeV have been studied, as discussed in Sec. 2. In 2017, a new set of beam parameters for the 250-GeV ILC was officially adopted [22]. It is this parameter set that is shown in the column "initial" of Tab. I. The 65% increase in instantaneous luminosity w.r.t. the TDR parameters is achieved by reducing the horizontal emittance by a factor of 2. This leads to a larger luminosity in each bunch crossing and thus to an increase of beamstrahlung, background from  $e^+e^-$  pairs and pile-up from low- $p_t \gamma \gamma \rightarrow$  hadrons events. Neither these effects, nor the slightly wider luminosity spectrum which results from the increased beamstrahlung are included in the physics case studies presented in the following sections, since no new Monte-Carlo samples could be produced (and analysed) since the new beam parameters became available. However, even with the new beam parameters the background conditions at  $250\,\mathrm{GeV}$  do not become worse than what is expected at 500 GeV, a case already studied in detail. The ILC detectors have actually been designed for high performance in the more difficult beam conditions at 1 TeV. Therefore, the impact of the new beam parameters on the majority of the physics analyses is expected to be minor. The analysis most strongly affected is the mass measurement of the Higgs boson via the leptonic recoil method, described in Sec. 8.2.1. For this analysis, the new beam parameters have been estimated to result in a relative degradation of the ultimate precision on the Higgs mass by about 25% [113] compared to the same amount of total luminosity collected with the TDR beam parameters. This still corresponds to an impressive Higgs mass measurement to better than 20 MeV.

We have already shown in Fig. 19 the default running scenario for the staged ILC based on the new beam parameters for 250 GeV [22]. Compared to Fig. 21, the total run time shortens from 26 years to 22 years, thus recovering about 2/3 of the original increase in running time. A full-scale Monte-Carlo production with the new beam parameters and based on the ILD detector concept is planned for 2019.

None of the running scenarios explicitly includes the option to increase the positron polarisation to 60% when operating at a center-of-mass energy of 500 GeV. Numerous studies [106, 110, 114–116] have shown that all physics measurements will profit from the corresponding increases in effective luminosity and effective polarisation. In this respect, all physics projections for 500 GeV are still quite conservative.

### 4. PHYSICS CASE – 250 GEV

The core of the physics case for the ILC is to make high-precision measurements of the properties of the Higgs boson. The Higgs field has a central role in the SM. It is responsible for the masses of all known elementary particles. It is also responsible for those aspects of the SM that are hardest to understand—-the presence of spontaneous gauge symmetry breaking, and the hierarchy of quark and lepton masses. Also, within the SM, the the flavor mixing and CP violation in weak interactions arise from the quark-Higgs Yukawa couplings, and neutrino masses, whatever their origin, require a coupling of neutrinos to the Higgs field. If we wish to learn more about these features of the fundamental laws of nature, an obvious course is to measure the Higgs boson as well as we are able. We will argue in this section and the succeeding ones that ILC will be able to determine the mass of the Higgs boson to a part in  $10^4$  and the major couplings of the Higgs boson to better than 1% accuracy. This will qualitatively sharpen the picture of the Higgs

boson that we will obtain even from the high-luminosity stage of the LHC.

This set of measurements, and other measurements available for the first time at the ILC, will open new paths in the search for new fundamental interactions beyond the SM. Though the SM seems to account for all elementary particle phenomena observed up to now, it is manifestly incomplete. It not only does not answer but actually is incapable of answering the questions posed in the previous paragraph. It also cannot address basic facts about the universe in the large, in particular, the excess of matter over antimatter and the origin of the cosmic dark matter. To make progress, we need observational evidence from particle physics of violations of the SM. These will provide clues that can show the way forward.

Up to now, we have sought evidence for new interactions from direct searches for new particles at LEP, the Tevatron, and the LHC, from measurements of the Wand Z bosons, and from searches for anomalies in flavor physics. We are now approaching the limits of these techniques with current particle physics facilities. The ILC will extend our search capabilities in precision measurements of W boson couplings and fermion pair production, and will provide new opportunites for the direct discovery of new particles. But, most of all, it will open a completely new road through the high-precision study of the Higgs boson.

#### 4.1. Mysteries of the Higgs boson

It is often said that the Higgs boson, as observed at the LHC, is an uninteresting particle, since it conforms so well to the expectations from the SM. In fact, aside from our knowledge of the Higgs boson mass, the measurements make so far at the LHC tell us almost nothing about the true nature of this particle. We now explain this statement, and, in the process, clarify the requirements for measurements of the Higgs boson couplings that can give insight into physics beyond the SM.

New physics can correct the Higgs boson couplings in many ways. However, in all cases, the size of the corrections is limited by the Decoupling Theorem, enunciated by Haber in [117]: If the new particles that modify the SM have minimum mass M, then the corrections to the SM predictions for the Higgs boson couplings are of size

$$a m_H^2 / M^2 . (1)$$

where the coefficient a is of order 1. The exclusions of new particles through searches at the LHC suggest that M is at least close to 1 TeV. Then the effects of new physics are limited to levels below 10%. We will illustrate this result with explicit models in the next subsection.

The proof of the theorem is simple and illustrative. It can be shown that the SM is actually the most general renomalizable quantum field theory with  $SU(3) \times$  $SU(2) \times U(1)$  gauge symmetry and the known particle content. If we add new particles with masses of M and above, we can assess their influence on the Higgs boson by integrating them out of the theory. This adds to the Lagrangian a set of new terms with the SM symmetries. The terms in the new Lagrangian can be organized by their operator dimension as

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{M^2} \sum_{i} c_i \mathcal{O}_{6i} + \frac{1}{M^4} \sum_{j} d_j \mathcal{O}_{8j} + \cdots \quad (2)$$

where  $\mathcal{L}_{SM}$  is the SM Lagrangian,  $\mathcal{O}_{6i}$  are operators of dimension 6,  $\mathcal{O}_{8j}$  are operators of dimension 8, *etc.* Shifts in the SM parameters due to new physics are not observable, since these parameters are in any case fit to experiment. Then the leading observable corrections are of order  $M^{-2}$ .

This theorem has a striking consequence. Instead of a model with a single Higgs doublet, as we have in the SM, nature could be providing a model with two or more Higgs fields, composite Higgs fields, even a whole Higgs sector. All of this possible complexity is hidden from us by the Decoupling Theorem.

The theorem has an appealing corollary, though. Since the SM is the most general renormalisable model, once its parameters are known, its predictions for the Higgs couplings are determined precisely. These predictions do depend on measured SM parameters such as  $m_b$ ,  $m_c$ , and  $\alpha_s$ , but it is argued in Ref. [118] that lattice QCD will determine these well enough to fix the SM predictions for Higgs to part-per-mil accuracy. Then, if we can observe corrections to the SM predictions at the 1% level, these corrections and the evidence that they give for new physics cannot hide.

## 4.2. Examples of new physics influence on the Higgs boson

Many models of physics beyond the SM illustrate the points made in the previous section. These examples point to a goal of 1% accuracy for the measurement of Higgs boson couplings in the major decay modes.

Models with two Higgs doublets contain 5 physical Higgs particles: two neutral CP-even states h, H, a neutral CP-odd state A, and a pair of charged scalars  $H^{\pm}$ . These states are mixed by two angles  $\alpha, \beta$ . The lighter CP-even state h is identified with the observed Higgs boson. Its couplings to fermions depend on the mixing angles. For example, in the "Type II" case,

$$g(Hb\bar{b}) = -\frac{\sin\alpha}{\cos\beta}\frac{m_b}{v} \quad g(Hc\bar{c}) = \frac{\cos\alpha}{\sin\beta}\frac{m_c}{v} .$$
(3)

However, the mixing angles are connected to the masses in such a way that when the additional bosons become heavy, their effects in (3) also become small,

$$-\frac{\sin\alpha}{\cos\beta} = 1 + \mathcal{O}(\frac{m_Z^2}{m_A^2}) , \qquad (4)$$

conforming to the Decoupling Theorem. In Type II models, the *b* and  $\tau$  Yukawa couplings are shifted together by



FIG. 22: Deviation from the SM prediction for the  $Hb\bar{b}$  coupling over a parameter space of grand-unified SUSY models, from [119]. Models in the upper left-hand corner are excluded by current LHC searches. Models above the dashed line are expected to be excluded at the HL-LHC. The color-code indicates the magnitude of the coupling deviation, in %.

about 5% for  $m_A = 500$  GeV, and by decreasing amounts as all of the additional bosons become heavier.

Supersymmetry (SUSY) models contain Type II two-Higgs-double sectors, but they also contain other effects that modify the Higgs boson couplings. Mixing between the scalar partners of  $b_L$  and  $b_R$  can generate a shift of the  $Hb\bar{b}$  coupling through loop diagrams. The magnitude of this effect in grand-unified SUSY models is shown in Fig. 22 [119]. Note that it is possible to have a large shift of the Higgs boson coupling for parameter values at which the SUSY particles are too heavy to be discovered at the LHC. Thus, the search for shifts in the Higgs couplings away from the SM predictions provides a method of searching for this new physics that is independent of, and largely orthogonal to, the direct search for SUSY particles. Other surveys of this effect in [120, 121] confirm this idea.

SUSY models typically predict very small shifts of the HWW and HZZ couplings, but other types of models can affect these couplings directly. Models in which the electroweak phase transition becomes first-order and allows baryogenesis at the weak scale often involve mixing of the Higgs field with a heavy singlet field. This gives

$$g(HWW) = \frac{2m_W^2}{v}\cos^2\phi \approx \frac{2m_W^2}{v}(1 - \frac{1}{2}\phi^2) , \qquad (5)$$

where  $\phi \sim m_H/m_S$ , and similarly for the HZZ coupling [122]. In composite models of the Higgs field, the Higgs boson often appears as a Goldstone boson of a new strong interaction theory, giving a coupling modification by  $(1 - v^2/f^2)^{1/2}$ , where f is the Goldstone boson decay constant [123]. This effect is similar to that in (5).

Models of Higgs compositeness, "Little Higgs" models, and models with extra space dimensions all contain new heavy vectorlike fermions T. Typically, these fermions obtain a fraction of their mass from the Higgs mechanism (perhaps by mixing with the top quark) that is of order  $u^2/u^2$ . Then there induce corrections of this order to

(perhaps by mixing with the top quark) that is of order  $m_t^2/m_T^2$ . Then they induce corrections of this order to the loop-generated Higgs couplings g(Hgg) and  $g(H\gamma\gamma)$ . Corrections as large as 10% can be generated in specific models [124]. The same mixing and compositeness effects modify the  $Ht\bar{t}$  coupling [125].

An interesting picture emerges. Almost all models of new physics generate corrections to the Higgs boson couplings. Almost always, these corrections are small, below the 10% level, in accord with the Decoupling Theorem. However, in precision experiments that make these coupling deviations visible, each type of new physics affects the Higgs couplings in different ways. In general,

- The  $Hb\bar{b}$  and  $H\tau\tau$  couplings are sensitive to models with additional Higgs doublets.
- The  $Hb\bar{b}$  coupling is sensitive to heavy SUSY particles with left-right mixing.
- The *HWW* and *HZZ* couplings are sensitive to mixing of the Higgs field with singlet fields, and to composite structure of the Higgs boson.
- The Hgg and  $H\gamma\gamma$  are sensitive to models with new vectorlike fermions.
- The *Htt̄* coupling is sensitive to models with composite Higgs bosons and top quarks.

In each new physics model, the deviations from the SM predictions for the Higgs couplings form a pattern. With precision experiments, it is possible not only to discover the existence of new physics but also to read the pattern and gain clues as to the way forward. A worked example of such model discrimination at the level of precision expected at the ILC is presented in Section 7 of Ref. [3].

## 4.3. Limitations of the LHC measurements on the Higgs boson

Today, the LHC experiments are achieving 20% uncertainties in their measurements of Higgs boson couplings. Over the lifetime of the LHC, including its highluminosity stage, these experiments will acquire a factor of 30 more data. Shouldn't this lead to Higgs coupling measurements of the required high precision? We believe that the answer to this question is no. We give a highlevel argument here. A detailed comparison of the expected ILC capabilities with those of the high-luminosity LHC will be presented in Sec. 11.3.

We find three points relevant to this comparison. First, the measurement of Higgs boson decays at the LHC is extremely challenging because of the difficulty of distinguishing signal from background. In the two decay modes in which the Higgs boson was discovered,  $H \rightarrow \gamma \gamma$  and  $H \to 4\ell$ , Higgs events are apparent, because all products of the Higgs are observed and the Higgs mass can be reconstructed with high accuracy. Unfortunately, these modes correspond to tiny branching ratios, 0.2% and 0.02% of Higgs decays, respectively. For more typical decay modes, Higgs boson decay events have no obvious differences in appearance from SM background reactions with larger rates. For example,  $H \rightarrow WW \rightarrow e\nu\mu\nu$ events differ from  $q\bar{q} \rightarrow WW \rightarrow e\nu\mu\nu$  events only in subtle features of the final state. To discover the Higgs boson in one of the major channels, the LHC experiments start from samples that are 10:1 background to signal in the highest significance regions. (For  $H \to b\bar{b}$ , the ratio is 20:1.) They then extract the signal by multivariate analysis and the use of machine-learning classifiers. It is already a triumph that ATLAS and CMS have been able to obtain significant observations.

Measuring the Higgs couplings with high precision is even more of a challenge. It is currently beyond the state of the art to determine the efficiency for the rejection of SM background events from these signal regions to 1% accuracy. The residual background events must be subtracted from the Higgs signal, and so this 1% would translate to a 10% accuracy on the Higgs  $\sigma \times BR$  or a 5% error on the coupling. To go beyond this level is truly daunting. Nevertheless, the studies reported in the HL-LHC Yellow Book [126] demonstrate that the HL-HLC can be expected to push beyond this level and reach accuracies on Higgs boson couplings of 2–4%.

This brings us to the second point. As we have emphasized already, the modifications of the Higgs boson couplings from new physics are expected to be small. In the previous section, we have argued that new physics interactions typically affect specific Higgs boson couplings at a level of 5% or smaller. A 2% measurement of such a coupling would not meet even the  $3\sigma$  criterion for positive evidence of new physics.

Finally, one must take into account that the HL-LHC measurements will ultimately be limited by the systematic understanding of backgrounds. Any deviation in Higgs couplings observed at the LHC is likely to be questioned (as, for example, the  $t\bar{t}$  forward-backward asymmetry from the Tevatron was) without a clear means of confirming the result. One sometimes hears that the LHC can measure ratios of branching ratios with improved accuracy, but this statement is not borne out by results presented in Ref. [126], since each mode has different backgrounds and requires its own dedicated analysis.

In contrast, as we will argue below, the observation of Higgs coupling deviations at the ILC at 250 GeV will be very robust. It will be be statistics-limited, and it can be confirmed by experiments at 500 GeV that bring in a new production reaction with an independent data set.

4.4. 
$$e^+e^- \rightarrow ZH$$

The arguments just presented call out for a different way to measure Higgs boson couplings. In this method, Higgs boson events should be apparent with a simple



FIG. 23: Event displays of  $e^+e^- \to ZH$  events with  $Z \to \mu^+\mu^-$ , from full simulation: Left:  $H \to \tau^+\tau^-$ , ILD detector model; Right:  $H \to b\bar{b}$ , SiD detector model.

discriminator that can then be refined for high-accuracy  $\sigma \times BR$  measurements. Ideally, this method should identify Higgs boson events independently of the decay mode, allowing the measurement of the total cross section for Higgs production and the discovery of exotic and unanticipated Higgs decays.

This new method will be provided by the ILC. It is the measurement of the reaction  $e^+e^- \rightarrow ZH$  at 250 GeV. At an  $e^+e^-$  collider at this energy, it is true to a first approximation that any Z boson observed with a lab energy of 110 GeV is recoiling against a Higgs boson. The backgrounds to this signature (present at about 30% of the signal level before cuts) come from radiative  $e^+e^- \rightarrow Z\gamma$  and  $e^+e^- \rightarrow ZZ$ , reactions that are well-understood and computed from electroweak theory at the 0.1% level.

The reaction  $e^+e^- \rightarrow ZH$  provides *tagged* Higgs decays. Thus, events can be selected independently of the Higgs decay mode. Then (1) the total cross section for this reaction can be measured, giving a means of absolutely normalizing Higgs boson couplings; (2) Higgs branching ratios can be measured by counting, independently of the production cross section; and, (3) exotic decay modes of the Higgs boson can be observed as products recoiling against the Z tag. Some event displays, from full simulation, are shown in Fig. 23.

#### 4.5. Search for exotic Higgs decays

The fact that the reaction  $e^+e^- \rightarrow ZH$  yields tagged Higgs decays opens the possibility of another type of search for new physics. The Higgs field is unique among SM fields in that it can form a dimension-2 operator  $\Phi^{\dagger}\Phi$ with zero SM quantum numbers. If there is any sector of fields that contains its own scalar field  $\Sigma$ , there will in general be a renormalizable coupling

$$\Delta \mathcal{L} = \eta \, \left( \Phi^{\dagger} \Phi \right) \left( \Sigma^{\dagger} \Sigma \right) \,. \tag{6}$$

The coupling constant  $\eta$  is dimensionless, so the connection can be made at any (high) mass scale. Thus it is possible for the Higgs boson to access a sector of elementary particles that have no other connection to the fields of the SM.

If there is a new sector of particles with zero SM quantum numbers such that some of those particles have pairproduction thresholds below 125 GeV, those particles should appear in Higgs boson decays. If the particle that makes up cosmic dark matter is light enough to be produced in this way, the Higgs boson will have decays to invisible final states. It is also possible that the new particles are unstable with respect to decay back to SM models. Such decays could produce a number of different exotic final states, including 4b,  $4\tau$ ,  $b\overline{b}$  + invisible states, and new particles with long lifetimes [127]. With the data sample of the 250 GeV ILC, it is possible to search for all of these decay modes. For invisible Higgs decays, the expected 95% CL exclusion limit on the branching ratio is  $3 \times 10^{-3}$ , and for visible or partially visible modes the limits are in the range  $10^{-3}$ - $10^{-4}$  [128].

## 4.6. Effective Field Theory framework for Higgs coupling determinations

Though the goals of measuring the SM and exotic branching ratios of the Higgs boson are already very important, experiments at the ILC allow a further step. The theory predictions described in Sec. 4.2 refer to absolute partial decay widths. These are related to the Higgs branching ratios by

$$\Gamma(H \to A\overline{A}) = \Gamma_{tot} \cdot BR(H \to A\overline{A}) . \tag{7}$$

The Higgs boson total width is very small—4 MeV in the SM—and it is not expected that any proposed collider can measure this value directly with percent-level precision. However, as we will now show, the ILC can determine the total width of the Higgs in a way that is highly model-independent and allows a 1% absolute normalization of Higgs coupling constants.

A possible method to determine the Higgs width is to multiply each HAA coupling by a parameter  $\kappa_A$ , and then fit these prarameters using data from  $e^+e^- \rightarrow ZH$ . In this simple method, the total cross section for  $e^+e^- \rightarrow$ ZH is proportional to  $\kappa_Z^2$  and so the  $\kappa_A$  parameters can be absolutely normalized. This method has been used in much of the literature on Higgs coupling determinations, including [129]. In that paper, invisible and visible but exotic decay modes were treated by including these two partial widths as two additional parameters in the fit. Using as inputs the measureable  $\sigma \times BR$ s for SM Higgs decay channels and Higgs decays to invisible final states, plus the total cross section for  $e^+e^- \rightarrow ZH$ , the ILC data would give a well-defined fit to the  $\kappa_A$  parameters.

There are two problems with this method. First, the method is not completely model-independent. Modelling the effects of new physics as a general set of dimension-6 operators as in (2), we find two different Lorentz structures for the modifications of the HZZ vertex,

$$\Delta \mathcal{L} = (1 + \eta_Z) \frac{m_Z^2}{v} h Z_\mu Z^\mu + \zeta_Z \frac{1}{2v} h Z_{\mu\nu} Z^{\mu\nu} , \qquad (8)$$

where  $Z_{\mu}$  is the gauge field and  $Z_{\mu\nu}$  is the field strength, and a similar pair of structures for the *HWW* vertex. The  $\zeta_V$  coefficients have interesting phenomenological significance. In weakly coupled models such as supersymmetry, these couplings are generated only by loop diagrams and have very small values; however, in composite Higgs models these coefficients can be comparable to the  $\eta_V$  coefficients. This makes it important to be able to determine the two couplings independently determined from data. The second problem with the method given in the previous paragraph is that it does not make the most effective use of the data set from  $e^+e^-$  colliders. The total width of the Higgs boson is determined from the ratio  $\sigma(e^+e^- \to ZH)/\Gamma(H \to ZZ^*)$ . Since branching ratio for  $H \to ZZ^*$  is only 3%, this strategy sacrifices a factor 30 in statistics.

A much more effective method for fitting Higgs boson couplings is described in [3]. In this method, we model the effects of new physics by the most general set of dimension-6 operators that can appear in (2). The complete set of  $SU(3) \times SU(2) \times U(1)$ -invariant leptonand baryon-number conserving dimension-6 operators includes 59 terms [130]. However, for the analysis of  $e^+e^$ collider data, we can restrict ourselves to electron reactions producing the Higgs boson and other color-singlet states. Since there is a single SM effective Lagrangian that should apply to all processes, this method allows us to combine data on Higgs production with additional data sets from  $e^+e^- \rightarrow W^+W^-$  and precision electroweak measurements. It is also possible to make use of additional observables for Higgs production beyond simple rates. In particular, the angular distribution and polarization asymmetry in  $e^+e^- \rightarrow ZH$  play important roles. These considerations give the method based on Effective Field Theory much more power in extracting the most accurate estimates of the Higgs boson couplings from the data.

It is sometimes considered a restriction that the EFT model contains only operators of dimension 6 without considering operators of dimension 8 and higher. However, there is a useful analogy to precision electroweak measurements. There, the effects of the top quark and the Higgs boson are well-modeled by the S and T parameters [131]—which are part of the dimension-6 effective field theory description—even though the masses of these particles are not far above the Z mass. Only when new particles are discovered and one wishes to compute their effects in detail is it necessary to go beyond the leading corrections. Very light new particles can have a different effect that is not accounted for by Effective Field Theory, since they can provide new Higgs decay channels that give additional contributions to the Higgs width. We take these possible effects into account explicitly as additional parameters in our global fit, as we will explain in Sec. 11.1.

After we describe the experimental methods and the expected measurement uncertainties for Higgs production in Sec. 8 and for W pair production in Sec. 9, we will present formal projections for uncertainties in Higgs couplings in Sec.11, making use of the EFT method.



FIG. 24: Feynman diagrams contributing to the process  $e^+e^- \rightarrow W^+W^-$  when contributing dimension-6 operators are included.

We will show that the data set expected for the ILC at 250 GeV will measure the  $Hb\bar{b}$  couplings to 1% accuracy, the HWW and HZZ couplings to better than 0.7%, and the other major SM Higgs couplings to accuracies close to 1%. These measurements should be statistics-limited. Above 250 GeV, a second Higgs production reaction,  $e^+e^- \rightarrow \nu\bar{\nu}h$  through W boson fusion becomes important. We will show that, using the additional data on  $e^+e^- \rightarrow ZH$  and the independent measurements from the W fusion reaction, the uncertainties on Higgs couplings will decrease by another factor of 2.

### 4.7. $e^+e^- \to W^+W^-$

The reaction  $e^+e^- \rightarrow W^+W^-$  contributes to the analysis described above, but it has its own independent interest. This reaction provides an excellent way to test for the presence of dimension-6 operators that involve the Wand Z fields. The Feynman diagrams contributing to the reaction are shown in Fig. 24. The process involves interference between *s*-channel diagrams with  $\gamma$  and Z exchanges and a *t*-channel diagram with neutrino exchange. In the SM, there are large cancellations among these diagrams, but these are not respected by the dimension-6 contributions. Thus, the dimension-6 coefficients appear in the cross section formula enhanced by a factor  $s/m_W^2$ .

The largest part of the dimension-6 effect can be described by shifts of the form factors for the  $WW\gamma$  and WWZ vertices. These vertices can be parametrized as [132]

$$\Delta \mathcal{L} = ig_V \left\{ V^{\mu} \left( \hat{W}^{-}_{\mu\nu} W^{+\nu} - \hat{W}^{+}_{\mu\nu} W^{-\nu} \right) + \kappa_V W^{+}_{\mu} W^{-}_{\nu} \hat{V}^{\mu\nu} + \frac{\lambda_V}{m_W^2} \hat{W}^{-\rho}_{\mu\nu} \hat{W}^{+}_{\rho\nu} \hat{V}^{\mu\nu} \right\}, \qquad (9)$$

where V = A or Z. In the SM,  $g_{1A} = e$ ,  $g_{1Z} = es_w/c_w$ and the other coefficients are zero at the tree level. The result  $g_{1A} = e$  is exact due to the QED Ward identity. The dimension-6 operator corrections generate a 3-parameter shift of the other 5 coefficients. These shifts can in principle be measured both at electron and at hadron colliders. However, measurements in  $e^+e^-$  have definite advantages. First, it is possible to use final states with hadronic W decays to determine the complete kinematics of each event and, using this information, to separate the production of transverse and longitudinal W bosons. Then, using beam polarization and W final-state polarization, the 3 possible shifts of the form factors can be measured separately. Second, the greater intrinsic accuracy of measurements in  $e^+e^-$  give excellent results at a center of mass energies of 250–500 GeV. At hadron colliders, the factor  $s/m_W^2$  can be much larger, and one can take advantage of this by observing the reaction at WW pair masses above 1 TeV. However, this can lead to ambiguities due to the possible influence of dimension-8 operators, whose effects grow as  $(s/m_W^2)^2$  [133].

In Sec. 9 below, after describing the experimental study of  $e^+e^- \rightarrow W^+W^-$ , we will show that the ILC at 250 GeV is expected to improve the precision of W form factor measurements by an order of magnitude over expected results from the HL-LHC.

4.8. 
$$e^+e^- \rightarrow f\overline{f}$$

Fermion pair production provides a search for new forces that couple directly to the electron. At LEP and LHC,  $e^+e^-$  and  $q\bar{q}$  annihilation are used as probes for new gauge bosons appearing in the *s*-channel and for signals of fermion compositeness.

The comparison with LEP 2 is instructive. The ILC will operate at an energy not so far above that of LEP 2 (250 GeV vs. 180–208 GeV) but with much higher luminosity (2  $ab^{-1}$  vs. a total of 1 fb<sup>-1</sup> over 4 experiments). For statistics-limited measurements, this gives a factor

$$\left[\frac{s \cdot \int \mathcal{L}|_{ILC}}{s \cdot \int \mathcal{L}|_{LEP}}\right]^{1/2} \approx 60 \tag{10}$$

improvement in sensitivity to deviations from the SM, or an improvement of 7.5 in the mass scale that can be accessed. Though the comparison depends on the particular model, this corresponds to the ability to observed new vector bosons at 5–6 TeV and contact interaction scales of 70 TeV, comparable to the projected reach of the HL-LHC.

In addition, the information from ILC is very specific. Measuring the cross section for  $e^+e^- \rightarrow f\bar{f}$  in the forward and backward directions for  $e_L^-$  and  $e_R^-$  beams gives four different observables, each of which corresponds to a different dimension-6 effective interaction. Discovery of an anomaly points directly to a model interpretation, either with an s-channel resonance or with new interactions at higher energy. This information can be put together with results of resonance searches at the LHC.

The reaction  $e^+e^- \rightarrow b\bar{b}$  deserves special consideration. In models in which the Higgs boson is composite, typically either the  $t_L$  or the  $t_R$  must be composite also to generate a large enough t quark mass. The  $b_L$  is the SU(2) partner of the  $t_L$  and so must have the same admixture of composite structure. If it is the  $t_R$  that is more composite, it is not required that the  $b_R$  is composite, but this often happens in models. This can generate few-percent corrections to the rates for  $e_{L,R}^-e^+ \rightarrow b_R\bar{b}_L$ at the ILC [134, 135]. It is possible that this effect, rather than effects in Higgs decays, would be the first indication of a composite Higgs sector.

## 4.9. Search for pair-production of new particles

Despite the wide range of direct searches for new particle pair production at the LHC, those searches have blind spots corresponding to physically interesting models. The two most important of these are:

- 1. Insensitivity to new particles with electroweak interactions only that decay to an invisible partner with a mass gap of less than 5 GeV. Though this case seems quite special, this is exactly the set of properties predicted for the charged Higgsino of SUSY models. Dark matter scenarios involving coannihilation can also fall into this blind spot, since in those models there is an electroweak partner separated from the dark matter particle by  $k_BT$ at the thermal dark matter freezeout temperature of 5-10 GeV.
- 2. Insensitivity to production of pairs of invisible particles observed through radiation of an initial-state gluon. At the LHC, such "mono-gluon" events have as a background initial state radiation in the Drell-Yan process, and the sensitivity to such events is limited by the precision of our knowledge of the Drell-Yan cross section.

In both cases, the ILC can detect these new physics events for particle masses almost up to half of the collider center of mass energy.

The experimental aspects of these particle seaches are discussed in Sec. 12. A broader review of the opportunities for new particle discovery at  $e^+e^-$  colliders can be found in [136].

#### 4.10. The central role of beam polarisation

One theme that runs through all of the analyses discussed in the following sections is the important role of beam polarisation. The use of beam polarisation may be unfamiliar to many readers, since all recently operated colliders - the Tevatron, PEP-II and KEKB, and the LHC – have had unpolarised beams. In hadronic collisions, the effects of polarisation are relatively small, first, because the dominant QCD interactions conserve parity and, second, because the proton is a composite particle, so high proton polarisation translates to much smaller polarisation for the constitutent quarks and gluons. At a high-energy  $e^+e^-$  collider, the situation is very different. The dominant interaction is the electroweak interaction, which has order-1 parity asymmetries in its couplings. The beam particles are elementary, so that 80% beam polarisation translates to 80% polarisation in the colliding partons. This implies that polarisation effects are large at  $e^+e^-$  colliders and can be used to great advantage.

It is very challenging to achieve high beam polarisation in circular colliders, especially for longitudinal polarisation. Transverse beam polarisation was observed at LEP in single- and separated-beam operation but not for colliding beams [137]. However, a linear electron or positron collider naturally preserves longitudinal beam polarisation. The design of the ILC has been thought through to produce, maintain, and control beam polarisation for both electrons and positrons, as has been explained in Sec. 2.3.1. This brings advantages for physics that we now discuss.

There are three major uses of beam polarisation in the experiments planned for ILC:

- 1. Measurement of helicity-dependent electroweak couplings.
- 2. Suppression of backgrounds and enhancement of signals.
- 3. Control of systematic uncertainties.

We discuss the first two of these points here. The third, which is particularly important to claim a discovery from precision measurements, is discussed in Sec. 8.3. A comprehensive review of the role of polarisation with many more examples can be found in [116], and, for positron polarisation in particular, in [110].

To begin, we need some notation. Let  $P_{e^-}$  and  $P_{e^+}$  be, respectively, the longitudinal polarisations of the electron and positron colliding beams, equal to +1 for completely polarised right-handed beams and -1 for completely polarised left-handed beams. Let  $\sigma_{RR}$ ,  $\sigma_{RL}$ ,  $\sigma_{LR}$ ,  $\sigma_{LL}$  be the cross sections for a given process with completely polarised beams of the four possible orientations. Since the electron has only two spin states, the cross section for general beam polarisations is given by

$$\sigma_{P_{e^-}P_{e^+}} = \frac{1}{4} \{ (1 + P_{e^-})(1 + P_{e^+})\sigma_{\mathrm{RR}} + (1 - P_{e^-})(1 - P_{e^+})\sigma_{\mathrm{LL}} + (1 + P_{e^-})(1 - P_{e^+})\sigma_{\mathrm{RL}} + (1 - P_{e^-})(1 + P_{e^+})\sigma_{\mathrm{LR}} \}, \qquad (11)$$

For s-channel  $e^+e^-$  annihilation processes, helicity conservation implies that only  $\sigma_{RL}$  and  $\sigma_{LR}$  are nonzero. In this case Eq. (11) reduces to the simpler form

$$\sigma_{P_{e^-}P_{e^+}} = 2\sigma_0(\mathcal{L}_{\text{eff}}/\mathcal{L}) \left[1 - A_{\text{LR}}P_{\text{eff}}\right]$$
(12)

where  $\sigma_0$  is the unpolarised cross section, and  $\mathcal{L}_{\text{eff}}$  and  $P_{\text{eff}}$  are the effective luminosity and polarisation, defined, respectively, as

$$P_{\text{eff}} = \frac{P_{e^-} - P_{e^+}}{1 - P_{e^+} P_{e^-}} \quad \text{and} \quad \mathcal{L}_{\text{eff}} = \frac{1}{2} (1 - P_{e^+} P_{e^-}) \mathcal{L} .$$
(13)

The coefficient  $A_{\rm LR}$  is the intrinsic left-right asymmetry of the reaction cross section,

$$A_{\rm LR} = \frac{\sigma_{\rm LR} - \sigma_{\rm RL}}{\sigma_{\rm LR} + \sigma_{\rm RL}} \ . \tag{14}$$

In the electroweak interactions, it is typical that lefthanded fermions have larger coupling constants than right-handed fermions. Then, choosing  $P_{e^-}$  to be lefthanded (negative) and  $P_{e^+}$  to be right-handed (positive) can confer important advantages. Consider, for example, the typical ILC values  $P_{e^-} = -80\%$ ,  $P_{e^+} = +30\%$ . Then the effective polarization Eq. (13) for the measurement of  $A_{\rm LR}$  values is  $P_{\rm eff} = 90\%$ . The Higgsstrahlung process has a rather small polarisation asymmetry,  $A_{\rm LR} = 0.151$ . Still, the luminosity is enhanced from the unpolarised case by 40%.

Such substantial values of the beam polarisations can be applied to physics measurements in the following ways:

- In  $e^+e^- \to f\bar{f}$ , the  $e_L^-$  and  $e_R^-$  couple to different linear combinations of the *s*-channel  $\gamma$  and *Z* propagators. Beam polarisation allows us to measure the couplings to these vector bosons independently. In addition, an *s*-dependent change in the polarisation asymmetry can signal the presence of a new *s*-channel resonance.
- Similarly, in  $e^+e^- \rightarrow W^+W^-$ , the separation of  $\gamma$  and Z couplings can be combined with information from the W production angle and polarisations to completely disentangle the 14 complex parameters (28 real parameters) in the most general Lagrangian for triple gauge vertices.
- In  $e^+e^- \rightarrow ZH$ , measurement of the polarisation asymmetry plays an important role in disentangling the various of parameters that enter the EFT analysis of Higgs boson couplings.
- If new particles are discovered in pair-production at the ILC, measurement of the production cross section with different beam polarisation settings allows their electroweak quantum numbers to be determined unambiguously.

We will illustrate all of these points in the sections to follow.

It is also possible to take advantage of differences in the polarisation effects on signal and background cross sections to enhance signals and control backgrounds. Unlike annihilation processes, radiative Bhabha scattering and 2-photon processes have nonzero  $\sigma_{LL}$  and  $\sigma_{RR}$ , so it is possible to test strategies for the suppression of these backgrounds using data sets with in which  $P_{e^-}$  and  $P_{e^+}$  have the same sign. The reaction  $e^+e^- \rightarrow W^+W^-$  has a relatively large cross section among annihilation processes and is often the dominant background to studies of or searches for other processes. However, this process also has a large polarisation asymmetry, with  $\sigma_{LR}/\sigma_{RL} \approx 30$ . Then running with  $P_{e^-} = +80\%$ ,  $P_{e^+} = -30\%$  essentially turns off this background.

As an example of the effectiveness of background suppression, we show in Fig. 25 a comparison of searches for invisible dark matter particles  $\chi$  in the mono-photon



FIG. 25: Comparison of the 95% confidence lower limit on the mediator scale for dark matter production using the

mono-photon channel, for different assumptions on luminosity and polarisation. See Sec. 12 for a description of the analysis [106]. Note that this plot considers *statistical uncertainties only.* The corresponding comparison *including systematic uncertainties* is shown in Fig. 59.

mode  $e^+e^ \rightarrow$   $\gamma$  +  $\chi\chi$  under different assumptions on luminosity and polarisation. The predicted 95% confidence lower limit on the mediator scale  $\Lambda_{95}$  is shown as a function of the  $\chi$  mass. The expected limit for an unpolarized collider is shown as the black solid curve. For this analysis, the statistically optimal choice is that of (+80%, -30%) polarisation; this gives the projected limit shown in the green dot-dash curve in the figure. This mode might not be chosen in practice, however, because the optimal polarisation setting will be different for other studies (e.q., Higgs measurements) that might be done in the same run. But the figure also shows that a data set of 1.6  $ab^{-1}$  with optimal polarisation is considerably more powerful than a data set of 4  $ab^{-1}$  with unpolarised beams. The red dotted curve shows the result for the H20 scenario with polarisations given in Tab. V. For clarity, the figure includes statistical errors only.

The influence of polarisation on systematic errors is equally important. Where experiments with unpolarised beams give one measurement, experiments with both electron and positron beams polarised give 4 independent measurements. These can be used as cross-checks for the understanding of systematics, and also to form combinations in which the dominant systematic errors cancel. We will discuss this point in more detail in Sec. 8.3.

# 5. PHYSICS CASE –BEYOND 250 GEV

A key advantage of linear colliders is the possibility to upgrade the center-of-mass energy. The energy reach of circular electron-positron colliders of a given circumference is limited by synchrotron radiation, and this is difficult to overcome because of the steep growth of synchrotron losses with energy. Linear colliders, however, can be upgraded to reach higher center of mass energies either by increasing the length of the main linacs or by installing linac components that support higher accelerating gradients.

In the major particle physics laboratories, the lifetime of collider elements and infrastructure has rarely been limited to the scope of the project they were designed and built for. A famous example is the Proton Synchrotron at CERN. Initially commissioned in 1959, it is still in operation as part of the accelerator complex that prepares protons for injection in the Large Hadron Collider. In this accelerator complex, the expensive civil engineering efforts to construct each component are reused, so that their cost is effectively shared. The tunnel that was constructed for LEP now hosts the Large Hadron Collider and its luminosity upgrade. In very much the same way, we expect that the ILC will form the seed for a facility that contributes to the cutting edge of particle physics for decades. For electron-positron collisions, any facility at energies much higher than those already realised must be a linear collider in a long, straight tunnel. The ILC naturally offers a setting for this program.

The ILC project today would be an  $e^+e^-$  collider of 250 GeV in the center of mass. But, already, considerable thought and planning has already gone into the extension of this machine to higher energies. In this section, we will briefly describe the further physics opportunities that the ILC will offer at 350 GeV, 500 GeV, and beyond. The physics goals for higher-energy  $e^+e^-$  colliders has already been discussed extensively in the literature. Particularly useful references are the volumes presenting detailed studies carried out for the ILC [129, 138] and CLIC [139–141] design reports.

#### 5.1. Scope of ILC energy upgrades

As explained in Sec. 2.4.1, the ILC TDR includes provisions for running of the ILC at 500 GeV and 1 TeV. The most obvious energy upgrade path is an extension of the linear accelerator sections of the colliders, which provides an increase in center-of-mass energy that is proportional to the length of the linacs. The design of the ILC presented in the TDR [1, 14, 15] envisaged a center-of-mass energy of 500 GeV in a facility with a total length of 31 km. The ILC TDR also documents a possible extension to 1 TeV based on current superconducting RF technology. Space for a tunnel of 50 km length is available at the Kitakami site in Japan, enough to accomodate a 1 TeV machine based on the TDR technology.

An even larger increase in center-of-mass energy may be achieved by exploiting advances in accelerator technology. The development of cavities with higher accelerating gradient can drive a significant increase in the energy while maintaining a compact infrastructure. Superconducting RF technology is evolving rapidly. Important progress has been made toward developing cavities with a gradient well beyond the 35 MV/m required for the ILC [35, 41] and even beyond the 45 MV/m envisaged for the 1 Tev ILC. In the longer term, alternate-shape or thin-film-coated Nb<sub>3</sub>Sn cavities or multi-layer coated cavities offer the potential of significantly increased cavity performance [14]. Novel acceleration schemes may achieve even higher gradients. The CLIC drive beam concept has achieved accelerating gradients of up to 100 MV/m [142]. Finally, the advent of acceleration schemes based on plasma wakefield acceleration or another advanced concept could open up the energy regime up to 30 TeV. A report of the status of accelerator R&D and remaining challenges is found in Refs. [143, 144], with further details and a brief description of the potential of such a machine in the addendum [145].

Thus, the ILC laboratory has paths to evolve into a laboratory for electron-positron collisions at higher energies, and possibly even to a laboratory that can offer the highest parton-parton center of mass energies achievable at any collider.

## 5.2. Improvement of ILC precision at higher energy

Operation of the ILC at higher energies will produce new data sets that will substantially improve the capabilites of the ILC for all of the physics topics presented in Sec. 4. The ILC simulation studies included extensive studies at 500 GeV and also studies at 1 TeV in the center of mass. We will present the results of these studies together with our studies from 250 GeV in the following sections.

Data-taking at higher energies will improve the results from 250 GeV and give access to new SM reactions. Let us first summarize the expected improvements in the areas that we have discussed so far:

- For Higgs production, running at 500 GeV will add a new data set of  $e^+e^- \rightarrow ZH$  events. It will also provide a substantial data set of  $e^+e^- \rightarrow \nu \overline{\nu} H$ events, corresponding to WW fusion production of the Higgs boson. With these new samples, it will be possible to confirm any anomalies in the Higgs boson coupling seen at 250 GeV and to provide an independent comparison of the ZZ and WWcouplings. Though the backgrounds to the Higgs production processes are relatively small for both reactions, they are different in the two cases, providing a nontrivial check of some systematics. In global analysis, as we will see in Sec. 11, the addition of 500 GeV data leads to a decrease in the uncertainties on Higgs boson couplings by about a factor of 2 and a decrease in the uncertainty on the Higgs total width by a factor 1.6.
- For WW production, running at 500 GeV will give a data set of roughly the same size as that obtained at 250 GeV. Further, since the effects of anomalous W couplings, or the corresponding dimension-6 operators, increase as  $s/m_W^2$ , the new data set will
provide much more sensitive constraints on their effects.

- For  $f\overline{f}$  production, similarly, the possible new effects due to heavy gauge bosons or contact interactions scale as  $s/M^2$ , where M is the new mass scale. The discovery potential for M, or new limits, will increase by a factor close to 2.
- For new particle searches, the reach in  $e^+e^-$  pair production is close to half the  $e^+e^-$  centre-of-mass energy. The improvement in reach is particularly relevant for color-singlet particles such as heavy Higgs bosons, electroweakinos, Higgsinos, and dark matter particles.

All of these observations illustrate the more general point that higher energy can be an important tool in tests of the SM using Effective Field Theory. We have emphasized that an analysis within EFT allows a more incisive search for new physics effects on Higgs boson couplings by bringing together a large number of observables from different physical processes. In the EFT formulae, the various operator contributions have different energy-dependence, with certain operators having an impact that grows strongly with energy. Thus there is great advantage in combining a data set taken at 250 GeV with one or more data sets taken at higher energies.

## 5.3. New Higgs physics at higher energy

Beyond the improvement in areas that we have already discussed, the operation of the ILC above 250 GeV can give access to new and important SM reactions. Among Higgs boson couplings, there are two that are inaccessible at 250 GeV. These are the top quark Yukawa coupling and the Higgs boson self-coupling. In Secs. 8.5 and 10.5, we will describe the measurement of these couplings at the ILC at 500 GeV and above. Since these couplings can show large deviations from the SM expectation in certain classes of new physics models, it is necessary to measure these couplings accurately to complete the full picture of the Higgs boson interactions.

The interest in the top quark Yukawa coupling is obvious. The top quark is the heaviest SM particle, and, within the SM, its mass is proportional to this coupling constant. If there are new interactions that promote the large value of the top quark mass, the Yukawa coupling will receive corrections, and so it is important to probe for them.

The measurement of the trilinear Higgs coupling is an equally important goal of a complete program of study for the Higgs boson. While the measurement of the Higgs field vacuum expectation value and the mass of the Higgs boson express the mass scale of the Higgs field potential energy and its variation, the trilinear Higgs coupling gives information on the shape of the potential energy function and brings us closer to understanding its origin.

The trilinear Higgs coupling is sensitive to the nature of the phase transition in the early universe that led to the present state of broken electroweak symmetry. The SM predicts a continuous phase transition. This has implications for models of the creation of the matterantimatter asymmetry that we observe in the unverse today. According to Sakharov's classic analysis [146], the net baryon number of the universe needed to be created in an epoch with substantial deviations from thermal equilibrium in which CP- and baryon-number-violating interactions were active. The baryon number of the universe could have been created at the electroweak phase transition, making use of new CP-violating interactions in the Higgs sector, but only if the phase transition was strongly first-order. In explicit models, this typically requires large deviations of this coupling, by a factor 1.5–3, from its SM value [147].

#### 5.4. Study of the top quark in $e^+e^-$ reactions

In addition, the extension of the ILC to higher energies will allow the precision study of the top quark. This is an essential goal of precision experiments on the SM, for two reasons. First, similarly to the Higgs boson, the top quark stands closer to the essential mysteries of the SM than any other quark or lepton. It is heavier than the next lighter fermion, the b quark, by a factor of 40 and heavier than the lightest quark, the u quark, by a factor of  $10^5$ . The reasons for this are unknown, but they must be related to other mysteries of the Higgs sector and SM mass generation. In fact, it is not understood whether the top quark is a "heavy" quark because of special interactions that the other quarks do not share or, alternatively, whether the top quark is an "ordinary" quark receiving an order-1 mass while the masses of the other quarks are highly suppressed. Competing extensions of the SM such as supersymmetry and composite Higgs models differ in their answers to this question.

Second, the fact that the top quark has spin, couples to the parity-violating weak interactions, and decays to nonzero spin particles through  $t \rightarrow bW$  gives a large number of independent observables for each  $t\bar{t}$  production process. An  $e^+e^-$  collider with beam polarization can take advantage of all of these observables, especially if it can produce  $t\bar{t}$  well above threshold at 500 GeV in the center of mass.

Thus, top quark physics is a place in which we expect to find deviations from the predictions of the SM, in a setting where we have many handles to search for these new physics effects. The top quark physics potential of the ILC is discussed in Section 10.

# 5.5. Direct searches for physics beyond the Standard Model

The energy upgrade of the ILC greatly significantly extends the reach of direct searches for signatures of extensions of the Standard Model. Searches for new particles at the ILC provide robust, loophole-free discovery potential. Once a significant signal is observed the properties and interactions of the new particle can be characterized with excellent precision. The discovery reach for massive particles is primarily limited by the kinematics of the process, with mass limits for pair-produced particles typically reaching half the center of mass energy. An energy upgrade to 500 GeV or 1 TeV therefore yields an immediate extension of the mass reach.

The possibility of an energy upgrade renders a linear collider facility a very flexible tool, allowing it to react to new discoveries at the LHC, at the ILC or elsewhere. The potential of the higher-energy stages for searches is evaluated in more detail in Section 12.

In the following sections, we will present the capabilities of the ILC in all of these areas. Our discussion will be based on explicit simulation studies using the accelerator properties and run plan described in Secs. 2 and 3 and the detector models to be presented in Sec. 6.

## 6. DETECTORS

#### 6.1. Introduction

The ILC accelerator is planned with one interaction region, equipped with two experiments. The two experiments are swapped into the Interaction Point within the so-called "push-pull" scheme. The experiments have been designed to allow fast move-in and move-out from the interaction region, on a timescale of a few hours to a day. In 2008 a call for letters of intent was issued to the community. Following a detailed review by an international detector advisory group, two experiments were selected in 2009 and invited to prepare more detailed proposals. These are the SiD detector and the ILD detector described in this section. Both prepared detailed and costed proposals which were scrutinised by the international advisory group and included in the 2012 ILC Technical Design Report [5]. In this section the two proposals are briefly introduced.

The ILC detectors are designed to make precision measurements on the Higgs boson, W, Z, t, and other particles. They are able to meet the requirements for such measurements, first, because the experimental conditions are naturally very much more benign than those at the LHC, and second, because the detector collaborations have developed technologies specifically to take advantage of these more forgiving conditions.

An  $e^+e^-$  collider gives much lower collision rates and events of much lower complexity than a hadron collider, and detectors can be adapted to take advantage of this. The radiation levels at the ILC will be modest compared with the LHC, except for the special forward calorimters very close to the beamline, where radiation exposure will be an issue. This allows the consideration of a wide range of materials and technologies for the tracking and calorimeter systems. The generally low radiation levels allow the innermost vertex detector elements to be located at very small radii, significantly enhancing the efficiency for short-lived particle identification. More generally, the relatively benign ILC experiment environment permits the design of tracking detectors with minimal material budget (see Sec. 7.3). This allows the detectors to meet the stringent requirement on the track mo-

tors to meet the stringent requirement on the track momentum resolution which is driven by the need to precisely reconstruct the Z mass in the Higgs recoil analysis. This requirement translates into a momentum resolution nearly an order of magnitude better than achieved in the LHC experiments.

At the same time, although they are studying electroweak particle production, it is essential that the ILC detectors have excellent performance for jets. At an  $e^+e^-$  collider, W and Z bosons are readily observed in their hadronic decay modes, and the study of these modes plays a major role in most analyses. To meet the requirements of precision measurements, the ILC detectors are optimized from the beginning to enable jet reconstruction and measurement using the particle-flow algorithm (PFA). This drives the goal of 3% jet mass resolution at energies above 100 GeV, a resolution about twice as good as has been achieved in the LHC experiments.

Finally, while the LHC detectors depend crucially on multi-level triggers that filter out only a small fraction of events for analysis, the rate of interactions at the ILC is sufficiently low to allow running without a trigger. The ILC accelerator design is based on trains of electron and positron bunches, with a repetition rate of 5 Hz, and with 1312 bunches (and bunch collisions) per train (see Sec. 2, Tab. I). The 199 ms interval between bunch trains provides ample time for a full readout of data from the previous train. While there are background processes arising from beam-beam interactions, the detector occupancies arising from these have been shown to be manageable.

The combination of extremely precise tracking, excellent jet mass resolution, and triggerless running gives the ILC, at 250 GeV and at higher energies, a superb potential for discovery.

To meet these goals an ambitious R&D program has been pursued throughout the past 10 years or so to develop and demonstrate the needed technologies. The results of this program are described in some detail in Ref. [148]. The two experiments proposed for the ILC, SiD and ILD, utilise and rely on the results from these R&D efforts.

Since the goals of SiD and ILD in terms of material budget, tracking performance, heavy-flavor tagging, and jet mass resolution are very demanding, we feel it important to provide information about the level of detailed input that enters our performance estimates. These are best discussed together with the event reconstruction and analysis framework that we will present in Sec. 7. In that section, we will present estimates of detector performance as illustrations at the successive stages of event analysis.

## 6.2. The SiD detector

The SiD detector is a general-purpose experiment designed to perform precision measurements at the ILC. It satisfies the challenging detector requirements resulting from the full range of ILC physics processes. SiD is based



FIG. 26: The SiD detector concept.

on the paradigm of particle flow, an algorithm by which the reconstruction of both charged and neutral particles is accomplished by an optimised combination of tracking and calorimetry. The net result is a significantly more precise jet energy measurement which results in a di-jet mass resolution good enough to distinguish between Wsand Zs. The SiD detector (Fig. 26) is a compact detector based on a powerful silicon pixel vertex detector, silicon tracking, silicon-tungsten electromagnetic calorimetry, and highly segmented hadronic calorimetry. SiD also incorporates a high-field solenoid, iron flux return, and a muon identification system. The use of silicon sensors in the vertex, tracking, and calorimetry enables a unique integrated tracking system ideally suited to particle flow.

The choice of silicon detectors for tracking and vertexing ensures that SiD is robust with respect to beam backgrounds or beam loss, provides superior charged particle momentum resolution, and eliminates out-of-time tracks and backgrounds. The main tracking detector and calorimeters are live only during a single bunch crossing, so beam-related backgrounds and low-pT backgrounds from  $\gamma\gamma$  processes will be reduced to the minimum possible levels. The SiD calorimetry is optimised for excellent jet energy measurement using the particle flow technique. The complete tracking and calorimeter systems are contained within a superconducting solenoid, which has a 5 T field strength, enabling the overall compact design. The coil is located within a layered iron structure that returns the magnetic flux and is instrumented to allow the identification of muons. All aspects of SiD are the result of intensive and leading-edge research aimed at achieving performance at unprecedented levels. At the same time, the design represents a balance between cost and physics performance. The key parameters of the SiD design are listed in Table IX.

#### 6.2.1. Silicon-based tracking

The tracking system (Fig. 27) is a key element of the SiD detector concept. The particle flow algorithm requires excellent tracking with superb efficiency and twoparticle separation. The requirements for precision mea-

TABLE IX: Key parameters of the baseline SiDdesign. (All dimension are given in cm).

SiDBarrel	Technology	In rad	Out rad	z extent
Vtx detector	Silicon pixels	1.4	6.0	$\pm$ 6.25
Tracker	Silicon strips	21.7	122.1	$\pm 152.2$
ECAL	Silicon pixels-W	126.5	140.9	$\pm$ 176.5
HCAL	Scint-steel	141.7	249.3	$\pm 301.8$
Solenoid	5 Tesla SC	259.1	339.2	$\pm 298.3$
Flux return	Scint-steel	340.2	604.2	$\pm 303.3$
SiDEndcap	Technology	In z	Out z	Out rad
Vtx detector	Silicon pixels	7.3	83.4	16.6
Tracker	Silicon strips	77.0	164.3	125.5
ECAL	Silicon pixel-W	165.7	180.0	125.0
HCAL	Scint-steel	180.5	302.8	140.2
Flux return	Scint/steel	303.3	567.3	604.2
LumiCal	Silicon-W	155.7	170.0	20.0
BeamCal	Semicond-W	277.5	300.7	13.5



FIG. 27: r-z view of vertex detector and outer tracker.

surements, in particular in the Higgs sector, place high demands on the momentum resolution at the level of  $\delta(1/p_T) \sim 2 - 5 \times 10^{-5}/\text{GeV}/c.$ 

Highly efficient charged particle tracking is achieved using the pixel detector and main tracker to recognise and measure prompt tracks, in conjunction with the ECAL, which can identify short track stubs in its first few layers to catch tracks arising from secondary decays of longlived particles. With the choice of a 5 T solenoidal magnetic field, in part chosen to control the  $e^+e^-$ -pair background, the design allows for a compact tracker design.

## 6.2.2. Vertex detector

To unravel the underlying physics mechanisms of new observed processes, the identification of heavy flavours will play a critical role. One of the main tools for heavy flavour identification is the vertex detector. The physics goals dictate an unprecedented spatial three-dimensional point resolution and a very low material budget to minimise multiple Coulomb scattering. The running conditions at the ILC impose the readout speed and radiation tolerance. These requirements are normally in tension. High granularity and fast readout compete with each other and tend to increase the power dissipation. Increased power dissipation in turn leads to an increased material budget. The challenges on the vertex detector are considerable and significant R&D is being carried out on both the development of the sensors and the mechanical support. The SiD vertex detector uses a barrel and disk layout. The barrel section consists of five silicon pixel layers with a pixel size of 20  $\times$  20  $\mu$ m<sup>2</sup>. The forward and backward regions each have four silicon pixel disks. In addition, there are three silicon pixel disks at a larger distance from the interaction point to provide uniform coverage for the transition region between the vertex detector and the outer tracker. This configuration provides for very good hermeticity with uniform coverage and guarantees excellent charged-track pattern recognition capability and impact parameter resolution over the full solid angle. This enhances the capability of the integrated tracking system and, in conjunction with the high magnetic field, makes for a very compact system, thereby minimising the size and costs of the calorimetry.

To provide for a very robust track-finding performance the baseline choice for the vertex detector has a sensor technology that provides time-stamping of each hit with sufficient precision to assign it to a particular bunch crossing. This significantly suppresses backgrounds.

Several vertex detector sensor technologies are being developed. One of these is a monolithic CMOS pixel detector with time-stamping capability (Chronopixel [149]), being developed in collaboration with SRI International. The pixel size is about 10  $\times$  10  $\mu$ m<sup>2</sup> with a design goal of 99% charged-particle efficiency. The time-stamping feature of the design means each hit is accompanied by a time tag with sufficient precision to assign it to a particular bunch crossing of the ILC - thus the name Chronopixel. This reduces the occupancy to negligible levels, even in the innermost vertex detector layer, yielding a robust vertex detector which operates at background levels significantly in excess of those currently foreseen for the ILC. Chronopixel differs from the similar detectors developed by other groups by its capability to record time stamps for two hits in each pixel while using standard CMOS processing for manufacturing. Following a series of prototypes, the Chronopixel has been proven to be a feasible concept for the ILC. The three prototype versions were fabricated in 2008, in 2012, and in 2014. The main goal of the third prototype was to test possible solutions for a high capacitance problem discovered in prototype 2. The problem was traced to the TSMC 90 nm technology design rules, which led to an unacceptably large value of the sensor diode capacitance. Six different layouts for the prototype 3 sensor diode were tested, and the tests demonstrated that the high capacitance problem was solved.

With prototype 3 proving that a Chronopixel sensor

can be successful with all known problems solved, optimal sensor design would be the focus of future tests. The charge collection efficiency for different sensor diode options needs to be measured to determine the option with the best signal-to-noise ratio. Also, sensor efficiency for charged particles with sufficient energy to penetrate the sensor thickness and ceramic package, along with a trigger telescope measurement, needs to be determined. Beyond these fundamental measurements, a prototype of a few cm<sup>2</sup> with a final readout scheme would test the longer trace readout resistance, capacitance, and crosstalk.

A more challenging approach is the 3D vertical integrated silicon technology, for which a full demonstration is also close.

Minimising the support material is critical to the development of a high-performance vertex detector. An array of low-mass materials such as reticulated foams and silicon-carbide materials are under consideration. An alternative approach that is being pursued very actively is the embedding of thinned, active sensors in ultra lowmass media. This line of R&D explores thinning active silicon devices to such a thickness that the silicon becomes flexible. The devices can then be embedded in, for example, Kapton structures, providing extreme versatility in designing and constructing a vertex detector.

Power delivery must be accomplished without exceeding the material budget and overheating the detector. The vertex detector design relies on power pulsing during bunch trains to minimise heating and uses forced air for cooling.

## 6.2.3. Main tracker

The main tracker technology of choice is silicon strip sensors arrayed in five nested cylinders in the central region and four disks following a conical surface with an angle of 5 degrees with respect to the normal to the beamline in each of the end regions. The geometry of the endcaps minimises the material budget to enhance forward tracking. The detectors are single-sided silicon sensors, approximately  $10 \times 10 \text{ cm}^2$  with a readout pitch of 50  $\mu$ m. The endcaps utilise two sensors bonded backto-back for small angle stereo measurements. With an outer cylinder radius of 1.25 m and a 5 T field, the charged track momentum resolution will be better than  $\delta(1/p_T) = 5 \times 10^{-5}/(\text{GeV}/c)$  for high momentum tracks with coverage down to polar angles of 10 degrees. A plot of the momentum budget as a function of polar angle is shown in Fig. 28.

The all-silicon tracking approach has been extensively tested using full Monte-Carlo simulations including full beam backgrounds. Besides having an excellent momentum resolution it provides robust pattern recognition even in the presence of backgrounds and has a real safety margin, if the machine backgrounds will be worse than expected.



FIG. 28: Material in the SiD detector, in terms of fractions of a radiation length, as a function of the polar angle.

## 6.2.4. Main calorimeters

The SiD baseline design incorporates the elements needed to successfully implement the PFA approach. This imposes a number of basic requirements on the calorimetry. The central calorimeter system must be contained within the solenoid in order to reliably associate tracks to energy deposits. The electromagnetic and hadronic sections must have imaging capabilities that allow both efficient track-following and correct assignment of energy clusters to tracks. These requirements imply that the calorimeters must be finely segmented both longitudinally and transversely. In order to ensure that no significant amount of energy can escape detection, the calorimetry must extend down to small angles with respect to the beampipe and must be sufficiently deep to prevent significant energy leakage. Since the average penetration depth of a hadronic shower grows with its energy, the calorimeter system must be designed for the highestenergy collisions envisaged.

In order to ease detector construction the calorimeter mechanical design consists of a series of modules of manageable size and weight. The boundaries between modules are kept as small as possible to prevent significant non-instrumented regions. The detectors are designed to have excellent long-term stability and reliability, since access during the data-taking period will be extremely limited, if not impossible.

The combined ECAL and HCAL systems consist of a central barrel part and two endcaps, nested inside the barrel. The entire barrel system is contained within the volume of the cylindrical superconducting solenoid.

SiD's reliance on particle flow calorimetry to obtain a jet energy resolution of  $\sim 3\%$  demands a highly segmented (longitudinally and laterally) electromagnetic calorimeter. It also calls for a minimized lateral electromagnetic shower size, by minimizing the Moliere radius to efficiently separate photons, electrons and charged hadrons [150].

The SiD ECal design employs thirty longitudinal layers, the first twenty each with 2.50 mm tungsten alloy thickness and 1.25 mm readout gaps, and the last ten with 5.00 mm tungsten alloy. The total depth is 26 radiation lengths, providing good containment of electromagnetic showers.

Simulations have shown the energy resolution for electrons or photons to be well described by 0.17 /  $\sqrt{E} \oplus$  0.009, degrading a bit at higher energies due to changes in sampling fraction and a small leakage.

The baseline design employs tiled, large, commercially produced silicon sensors (currently assuming 15 cm wafers). The sensors are segmented into pixels that are individually read out over the full range of charge depositions. The complete electronics for the pixels is contained in a single chip, the KPiX ASIC [151], which is bump bonded to the wafer. The low beam-crossing duty cycle  $(10^{-3})$  allows reducing the heat load using power pulsing, thus allowing passive thermal management within the ECal modules.

Bench tests of the KPiX bonded sensor with a cosmic ray telescope trigger yielded a Landau distribution with a peak of the signal at about 4 fC is consistent with our expectation for minimum-ionizing particles (MIP) passing through the fully-depleted 320  $\mu$ m thick sensors. Crosstalk between channels has been managed and the noise distribution shows an RMS of 0.2 fC, well below the 4 fC MIP signal, and exceeding the ECal requirement.

The overall mechanical structure of the ECal barrel has been designed for minimal uninstrumented gaps. Input power and signals are delivered with Kapton flex cables. The KPiX chip has an average power less than 20 mW, resulting in a total heat load that is managed with a cold plate and water pipes routed into the calorimeter.

A first SiD ECal prototype stack of nine (of thirty) layers has been constructed and was exposed to a 12.1 GeV electron beam at the SLAC End Station Test Beam Facility. This data collection demonstrated good measurements of multiple particle overlap and reconstruction of overlapping showers [152]. Comparison of the deposited energy distribution in each of the nine layers also agrees well with simulations. An algorithm developed to count the number of incident electrons in each event was used to assess the ability of the calorimeter to separate two showers as a function of the separation of the showers, achieving 100% for separations of >10 mm.

The hadronic calorimeter has a depth of 4.5 nuclear interaction lengths, consisting of alternating steel plates and active layers. The baseline choice for the active layers is scintillator tiles read out via silicon photomultipliers. For this approach SiD is closely following the analog hadron calorimeter developments within the CALICE collaboration. In this context, the simulated HCAL energy resolution has been shown to reproduce well the results from the CALICE AHCAL prototype module exposed to pion beams.

## 6.2.5. Forward calorimeters

Two special calorimeters are foreseen in the very forward region: LumiCal for a precise luminosity measurement, and BeamCal for the fast estimation of the collision parameters and tagging of forward-scattered beam particles. LumiCal and BeamCal are both compact cylindrical electromagnetic calorimeters centered on the outgoing beam, making use of semiconductor-tungsten technology. BeamCal is placed just in front of the final focus quadrupole and LumiCal is aligned with the electromagnetic calorimeter endcap.

LumiCal makes use of conventional silicon diode sensor readout. It is a precision device with challenging requirements on the mechanics and position control, and must achieve a small Moliere radius to reach its precision targets. Substantial work has been done to thin the silicon sensor readout planes within the silicon-tungsten assembly. Dedicated electronics with an appropriately large dynamic range is under development.

BeamCal is exposed to a large flux of low-energy electron-positron pairs originating from beamstrahlung. These depositions, useful for a bunch-by-bunch luminosity estimate and the determination of beam parameters, require radiation hard sensors. The BeamCal has to cope with 100% occupancies, requiring dedicated frontend electronics. A challenge for BeamCal is to identify sensors that will tolerate over one MGy of ionizing radiation per year. Sensor technologies under consideration include polycrystalline chemical vapor deposition (CVD) diamond (too expensive to be used for the full coverage), GaAs, SiC, Sapphire, and conventional silicon diode sensors. The radiation tolerance of all of these sensor technologies has been studied in a high-intensity electron beam.

For SiD, the main activities are the study of these radiation-hard sensors, development of the first version of the so-called Bean readout chip, and the simulation of BeamCal tagging for physics studies. SiD coordinates these activities through its participation in the FCAL R&D Collaboration.

### 6.2.6. Magnet coil

The SiD superconducting solenoid is based on the CMS solenoid design philosophy and construction techniques, using a slightly modified CMS conductor as its baseline design. Superconducting strand count in the coextruded Rutherford cable was increased from 32 to 40 to accommodate the higher 5 T central field.

Many iron flux return configurations have been simulated in two dimensions so as to reduce the fringe field. An Opera 3D calculation with the Detector Integrated Dipole (DID) coil has been completed. Calculations of magnetic field with a 3D ANSYS program are in progress. These will have the capability to calculate forces and stress on the DID as well as run transient cases to check the viability of using the DID as a quench propagator for the solenoid. Field and force calculations with an iron endcap HCAL were studied. The field homogeneity improvement was found to be insufficient to pursue this option.

Conceptual DID construction and assembly methods have been studied. The solenoid electrical power system, including a water-cooled dump resistor and grounding, was established. Significant work has been expended on examining different conductor stabiliser options and conductor fabrication methods. This work is pursued as a cost- and time-saving effort for solenoid construction.

## 6.2.7. Muon system

The flux-return yoke is instrumented with position sensitive detectors to serve as both a muon filter and a tail catcher. The total area to be instrumented is very significant – several thousand square meters. Technologies that lend themselves to low-cost large-area detectors are therefore under investigation. Particles arriving at the muon system have seen large amounts of material in the calorimeters and encounter significant multiple scattering inside the iron. Spatial resolution of a few centimetres is therefore sufficient. Occupancies are low, so strip detectors are possible. The SiD baseline design uses scintillator technology, with RPCs as an alternative. The scintillator technology uses extruded scintillator readout with wavelength shifting fibre and SiPMs, and has been successfully demonstrated. Simulation studies have shown that nine or more layers of sensitive detectors yield adequate energy measurements and good muon detection efficiency and purity. The flux-return yoke itself has been optimised with respect to the uniformity of the central solenoidal field, the external fringe field, and ease of the iron assembly. This was achieved by separating the barrel and end sections of the yoke along a 30 degree line.

## 6.2.8. The machine-detector interface

A time-efficient implementation of the push-pull model of operation sets specific requirements and challenges for many detector and machine systems, in particular the interaction region (IR) magnets, the cryogenics, the alignment system, the beamline shielding, the detector design and the overall integration. The minimal functional requirements and interface specifications for the push-pull IR have been successfully developed and published [153, 154]. All further IR design work on both the detectors and machine sides are constrained by these specifications.

## 6.3. The ILD detector

The ILD detector has been developed by a protocollaboration with the goal to develop and eventually propose a fully integrated detector for the ILC.

The ILD detector concept has been designed as a multi-purpose detector. It should deliver excellent



FIG. 29: 3D-picture of the ILD detector.

physics performance for collision energies between 90 Gev and 1 TeV, the largest possible energy reach of the ILC. The ILD detector has been optimized to perform excellently at the initial ILC energy of 250 GeV (for more details see [5, 155]). An artist's view of the ILD detector is shown in Fig. 29.

The science which will be done at the ILC requires a detector that truly covers all aspects of the  $e^+e^-$  events. The tracking philosophy is very different from that of SiD, as will be discussed in a moment. However, similarly to SiD, the ILD detector has been designed to combine the traditional precision detector elements such as as vertex detectors and trackers in an overall design philosophy that optimizes jet reconstruction using particle flow.

#### 6.3.1. Vertexing and tracking

The high precision vertex detector positioned very closely to the interaction point is followed by a hybrid tracking layout, realised as a combination of silicon tracking with a time projection chamber, and a calorimeter system. The complete system is located inside a large solenoid providing a magnetic field of 3.5-4 T. On the outside of the coil, the iron return yoke is instrumented as a muon system and as a tail catcher calorimeter.

The vertex detector is realised as a multi-layer pixelvertex detector (VTX), with three super-layers, each comprising two layers. The detector has a pure barrel geometry. To minimise the occupancy from background hits, the first super-layer is only half as long as the outer two. Whilst the underlying detector technology has not yet been decided, the VTX is optimised for point resolution and minimum material thickness.

A system of silicon strip and pixel detectors surrounds the VTX detector. In the barrel, two layers of silicon strip detectors (SIT) are arranged to bridge the gap between the VTX and the TPC. In the forward region, a system of two silicon-pixel disks and five silicon-strip disks (FTD) provides low angle tracking coverage.

A distinct feature of ILD is a large volume time projection chamber (TPC) with up to 224 points per track. The TPC is optimised for 3-dimensional point resolu-



FIG. 30: Material in the ILD detector, in terms of fractions of a radiation length, as a function of the polar angle.

tion and minimum material in the field cage and in the end-plate. It also allows dE/dx-based particle identification. At the ILC, a TPC has a number of specific strengths which make this type of detector attractive. A time projection chamber offers true three-dimensional points, and offers many of those along a charged particle trajectory. The intrinsic disadvantage of a TPC, its slow readout speed, does not harm the performance at the ILC, since the time between bunches is relatively long, around 300 ns. On the other hand the large number of points offer superb pattern recognition capabilities, and allows the detailed reconstruction of kinks or decays in flight within its volume. This can be achieved at a very low material budget, rather uniformly distributed over the sensitive volume. The excellent performance of the system is particularly striking at low momenta, at a few GeV and below, where the combination of three dimensional reconstruction and low material allows the efficient and precise reconstruction of tracks.

Outside the TPC, a system of Si-strip detectors in between the TPC and the ECAL (SET), provide additional high precision space points which improve the tracking performance and provide additional redundancy in the regions between the main tracking volume and the calorimeters.

A key aspect of the ILD detector design is the low mass of the tracking system. The total material as a function of angle, in radiation lengths, is shown in Fig. 30.

## 6.3.2. Calorimetry

A highly segmented electromagnetic calorimeter (ECAL) provides up to 30 samples in depth and small transverse cell size, split into a barrel and an end cap system. For the absorber, Tungsten has been chosen; for the sensitive area, silicon diodes or scintillator strips are considered.

This is followed by a segmented hadronic calorimeter (HCAL) with up to 48 longitudinal samples and small

transverse cell size. Two options are considered, both based on a steel-absorber structure. One option uses scintillator tiles of  $3 \times 3 \text{ cm}^2$ , which are read out with an analogue system. The second uses a gas-based readout which allows a  $1 \times 1 \text{ cm}^2$  cell geometry with a semi-digital readout of each cell.

At very forward angles, below the coverage provided by the ECAL and the HCAL, a system of high precision and radiation hard calorimetric detectors (LumiCAL, Beam-CAL, LHCAL) is foreseen. The LumiCAL and Beam-CAL are based on technologies developed in the context of the FCAL collaboration. These detectors extend the calorimetric coverage to almost  $4\pi$ , measure the luminosity, and monitor the quality of the colliding beams. the LHCAL system bridges the electromagnetic endcap calorimeter with the forward systems.

## 6.3.3. Coil and yoke

A large volume superconducting coil surrounds the calorimeters, creating an axial *B*-field of nominally 3.5-4 Tesla.

An iron yoke, instrumented with scintillator strips or resistive plate chambers (RPCs), returns the magnetic flux of the solenoid, and, at the same time, serves as a muon filter, muon detector and tail catcher calorimeter.

### 6.3.4. Detector integration and performance

The ILD detector is designed to operate in the ILC interaction region with a push-pull scheme, allowing the rapid interchange of ILD with SiD. Detailed studies have been done to understand the impact this scheme might have on the detector and its design. In addition the ILD detector is optimised for operation in the seismic active region in the north of Japan. Extensive simulation studies for the main components have shown that the detector is stable against seismic events.

Key plots to evaluate the projected performances of the ILD and SiD detectors will be presented in the following chapter. These plots will also illustrate the successive stages of event reconstruction from raw data and will describe the level of detail that we have considered in making these estimates of performance. As we have already noted, the ILD and SiD detectors include many technologies that have been developed in close cooperation with R&D collaborations and have been extensively tested. For both detectors, the performance numbers of key systems are based on results from prototypes, wherever possible, and extrapolated to the full detector performance. This strong check against experimental results ensures that the performance numbers are reliable and are considered a realistic estimate of the ultimate detector performance.



FIG. 31: Schematic view of the hierarchical EDM in LCIO.

## 7. COMPUTING, EVENT RECON-STRUCTION, AND DETECTOR PER-FORMANCE

This section will describe the software framework used for ILC event analysis, working from raw data or digitized simulation data to physics objects. We will first describe the core software tools used by the detector groups. We will then follow the path by which this software to used to provide detailed detector models and model data sets, to reconstruct the data including as much realism as possible, and to produce the final physics objects for analysis. At the successive stages of this process, we will illustrate the intermediate results with performance plots that also can be used to benchmark the detector models. Finally, we will discuss the computing concept and costs for the ILC experiments.

More than 15 years ago the linear collider community started to develop common software tools to facilitate the development and optimization of detector concepts based on realistic simulations of physics interactions. These software tools eventually led to the creation of a common software ecosystem called *iLCSoft* [156]. The *iLCSoft* tools are used by both ILC detector concepts as well as by CLIC and partly by CEPC and FCC.

From the start, a strong emphasis has been placed on developing flexible and generic tools that can easily be applied to other experiments or new detector concepts. This approach of developing common tools wherever possible has helped considerably in leveraging the limited manpower and putting the focus on algorithm development that is crucial for the physics performance.

## 7.1. Core software tools

The foundation for the development of common software was laid with LCIO [157], the event data model (EDM) and persistency tool for linear collider studies. At the core of LCIO is a hierarchical EDM for any particle physics experiment, as shown in Fig. 31. It provides data classes for all phases of the event processing, starting



FIG. 32: Schematic view of DD4hep with its main components and interfaces.

from Monte Carlo truth information, continuing to generate raw data and digitization, and processing this to the final reconstruction and analysis. Objects at higher levels of the processing point back to the lower level constituting objects. As a specific design decision, there are no pointers back to the Monte Carlo truth but these can be added if needed using dedicated generic LCRelation objects. These relation objects can be used to create many-to-many relations between arbitrary types in the EDM. A special class LCGenericObject holds user defined data in named vectors of types int, float and double. This feature is used in many test beams for conditions data and raw data from the DAQ. LCIO provides APIs in C++, Java and Fortran, but today C++ is used almost exclusively.

The C++ application framework Marlin [158] provides an easy to use environment for developing software modules on all levels of processing and uses LCIO as its transient data format, i.e. all data that is read in or created by a software module (called *Processor*) are stored in the *LCEvent* class from LCIO. Marlin processors are self-documenting and controlled via xml-steering files. As processors have well defined input and output data, Marlin provides a "*Plug-And-Play*" environment, where any specific algorithm can easily be exchanged with another equivalent implementation for direct comparisons and benchmarking.

The generic detector description toolkit DD4hep [159, 160] provides a powerful tool for describing the detector geometries, materials and readout properties. DD4hep follows a modular component based approach and provides interfaces to full simulations with GEANT4 [161] via DDG4, to reconstruction programs via DDRec and to conditions data and alignment with DDCond and DDAlign respectively, see Fig. 32. DD4hep is an excellent example for the development of generic software tools for the wider HEP community and was one of the first incubator projects adopted by the Hep Software Foundation. While it was developed to address the needs of the linear collider community, it is now used by several other projects and is under evaluation by LHC experiments.



FIG. 33: Beam energy spectra for  $\sqrt{s} = 250$  GeV Set-A, created with GuineaPig (blue-dashed:  $e^-$ , red-solid  $e^+$ ).

## 7.2. Event generators

Both detector concepts have created large, realistic Monte Carlo samples with the full Standard Model physics as well as various BSM scenarios that have been used for the physics analyses presented in the following sections. In a first step, large generator samples with  $e^+e^-$  events are created with the Whizard [162] event generator. Whizard uses tree-level matrix elements and loop corrections to generate events with the final state partons and leptons based on a realistic beam energy spectrum, the so called *hard sub-process*. The hadronization into the visible final state is performed with Pythia [163] tuned to describe the LEP data.

The input spectrum is created with Guinea-Pig [164], a dedicated simulation program for computing beam-beam interactions at linear colliders. The two dominating effects of the strong beam-beam interactions are beam-strahlung, leading to the available luminosity spectrum (see Fig. 33), and the creation of incoherent  $e^+e^-$ -pairs that are the source of the dominant background at the ILC. These electrons and positrons are predominantly created in a forward cone as shown in Fig. 34. It is this cone that restricts the minimal allowed radius of the innermost layer of the vertex detector.

Another source of background at the ILC are  $\gamma \gamma \rightarrow hadrons$  events, due to bremsstrahlung and beamstrahlung photons. These types of events are generated for  $\gamma \gamma$  cms-energies from 300 MeV to 2 GeV with a dedicated generator based on Ref. [166]; for higher energies Pythia is used.



FIG. 34: Cone of background from incoherent  $e^+e^-$ -pairs, generated with Guinea-Pig and simulated in the 5 T B-field of the SiD detector (from [165]).



FIG. 35: Cut-away view of the tracking system as implemented in the *SIDLOI3* simulation model (from [5]).

## 7.3. Simulation

Both detector concepts have adopted DD4hep for describing their detector simulation models and use *ddsim*, a python application that is based on the DDG4 component, to provide a gateway to full simulations with GEANT4. In DD4hep the detector geometry is implemented in dedicated C++ modules for every subdetector and the actual parameters with dimensions and materials are provided via compact xml-files. DD4hep contains a large palette of predefined sub-detector drivers, allowing for an easy implementation of a new detector concept by providing suitable compact files. A dedicated software package lcgeo [167], which is shared by SiD, ILD and CLICdp, contains all subdetector drivers for the detector concepts under study by these groups, together with the corresponding compact parameter files.

Both detector concept groups have invested considerable effort into making their full-simulation models as realistic as possible, by

- following the exact dimensions and layout of detector elements from engineering models
- implementing correct material properties
- implementing precise descriptions of the actual detector technology
- adding realistic amounts of dead material from supports and services, such as cables and cooling pipes
- introducing realistic gaps and imperfections into the subdetectors

Care has been taken to include realistic material estimates in particular in the tracking region where the material budget has a direct impact on the detector performance. Figure 35 shows the tracking detector as implemented for the SiD simulation model. The average material budget in the tracking volume of the simulation models has already been shown in Sec. 6, Figs. 28 and 30, for SiD and ILD respectively.

Before the two concepts had decided to move to the common geometry description and simulation with DD4hep, they had implemented their detailed simulation models in Mokka [168] and slic [169]. These models have been ported into DD4hep preserving all features and dimensions, thus resulting in equivalent simulation results. Most of the physics analyses in the next sections are based on simulations using these older programs.

The high level of detail in the simulation models as described above is a key prerequisite for the realistic understanding of the expected detector performance and the physics reach of the ILC for both detector concepts.

## 7.4. Digitzation

The output of the detailed full simulations with GEANT4 from ddsim are *SimTrackerHit* and *Sim-CalorimeterHit* objects. These store the deposited energy in the sensitive detector elements, such as silicon wafers and calorimeter cells, together with the position and pointers to the *MCParticle* that created the energy deposition. In the digitization step, carried out in dedicated Marlin processors, these hits are converted into *TrackerHit* and *CalorimeterHit* objects, taking into account all relevant effects from the detector and the read-out electronics.

The *SimTrackerHits* contain the exact energyweighted position of the individual energy depositions in a given sensitive detector element. For silicon strip-and pixel detectors as well as the ILD-TPC, these positions are smeared according to resolutions that have been established from test beam campaigns for the different sensor technologies, thereby including effects from charge sharing, clustering and position reconstruction. Table X shows the point resolution parameters used for ILD.

In the TPC hit digitization, simulated hits that are closer than the established double-hit resolution of 2 mm

Subdetector		Point Resolution
VTX	$\sigma_{r\phi,z}$	$= 2.8 \mu \mathrm{m} \; (\mathrm{layer} \; 1)$
	$\sigma_{r\phi,z}$	$= 6.0 \mu m (layer 2)$
	$\sigma_{r\phi,z}$	$= 4.0 \mu m$ (layers 3-6)
SIT	$\sigma_{\alpha_z}$	$= 7.0 \mu \mathrm{m}$
	$\alpha_z$	$= \pm 7.0^{\circ}$ (angle with z-axis)
SET	$\sigma_{lpha_z}$	$= 7.0 \mu \mathrm{m}$
	$\alpha_z$	$= \pm 7.0^{\circ}$ (angle with z-axis)
FTD	$\sigma_r$	$= 3.0 \mu \mathrm{m}$
Pixel	$\sigma_{r_{\perp}}$	$= 3.0 \mu \mathrm{m}$
FTD	$\sigma_{lpha_r}$	$= 7.0 \mu \mathrm{m}$
Strip	$\alpha_r$	= $\pm 5.0^{\circ}$ (angle with radial direction)
TPC	$\sigma^2_{r\phi}$	$= (50^2 + 900^2 \sin^2 \phi + ((25^2/22) \times$
		$(4T/B)^2 \sin \theta (z/\mathrm{cm}) \mu \mathrm{m}^2$
	$\sigma_z^2$	$= (400^2 + 80^2 \times (z/\text{cm})) \mu\text{m}^2$
	w	here $\phi$ and $\theta$ are the azimuthal and
		polar angle of the track direction

TABLE X: Effective point resolutions as used in the digitization of the ILD tracking detectors. The parameterization for the TPC takes into account geometric effects due to the direction of the track with respect to the pad row and has been established from test beam data.

in  $r\phi$  and 5 mm in z are merged into one. For the silicon detectors this treatment is not necessary, due to the expected low occupancies.

The *SimCalorimeterHits* contain the total energy deposited in each calorimeter cell, together with the individual depositions from the individual Monte Carlo steps. For scintillating calorimeters Birk's Law is already applied during the simulation, resulting in different light yields for different particles. Dedicated digitizers take into account effects of non-uniformity of the light yield for scintillators as well as cross-talk between neighboring channels. The latter is important in particular for the simulation of (semi)-digital calorimeters using RPCs and is possible due to the availability of the individual simulation steps, containing the exact position of the energy deposition.

During the calorimeter digitization, a two step calibration is applied for every calorimeter type and sampling structure. In a first step the hits are calibrated to a MIP signal and in a second step, the total energy is calibrated to an absolute value of the cell energy in GeV. This calibration is an iterative procedure, based on the application of the full *particle flow algorithm* to single particle events with photons and  $K^0$ s and thereby repeatedly adjusting the calibration constants.

## 7.5. Reconstruction

## 7.5.1. Tracking

The first step of the event reconstruction consists of identifying the trajectories of charged particles based on the



FIG. 36: Schematic view of the MarlinTrk tracking tools available in iLCSoft. They are based on the LCIO event data model and the DDRec geometry description.

positions of their energy depositions in the detector (Sim-TrackerHits), typically referred to as pattern recognition. In a second step the kinematic parameters of these trajectories are fitted based on the known equations of motion in a magnetic field and the errors of the hit positions. Often both steps are carried out together, *e.g.*, by using a Kalman-Filter and simply referred to as Tracking.

The tracking packages in iLCSoft is called MarlinTrk and provides a generic tracking-API *IMarlinTrk* and underlying fitting code, using the Kalman-Filter package *KalTest* [170]. The *IMarlinTrk* interface provides code to iteratively add hits to a track segment, thereby updating the track parameters, extrapolation of the current track state to the next measurement surface or any given point in space. It uses LCIO as data model for the Track and TrackState with a *perigee* track parameterization with track curvature  $\omega$ , impact parameters  $d_0$  and  $z_0$  and direction parameters  $\phi_0$  and  $\tan(\lambda)$ . A palette of different pattern recognition algorithms are programmed against *IMarlinTrk* as shown in Fig. 36. ILD uses the following different algorithms in the different parts of the tracking region (for more details see Ref. [171]):

• SiliconTracking

Algorithm used in the innermost Si-tracking detector VXD and SIT, based on a brute-force triplet seeding followed by a road search using the extrapolation to the next layer provided in MarlinTrk.

• ForwardTracking

Stand alone pattern recognition in the FTD forward tracker using a Cellular-Automaton to find a (possibly large) set of track candidates that are reduced to a unique and consistent set through the use of a Hopfield Network.

• Clupatra

Pattern recognition algorithm for the TPC, based on topological clustering in the outer TPC pad row layers for seeding, followed by a Kalman-Filter based road search inwards.

• FullLDCTracking

A collection of algorithms for merging track segments from the previous algorithms and assignments of leftover hits followed by a final re-fit using a Kalman-Filter.

SiD had originally developed their stand-alone tracking software in the Java framework *LCSim* [172] using a triplet based seeding followed by a road search and a final track fit. More recently SiD has adopted the *ConformalTracking* algorithm originally developed for CLICdp. It uses a conformal mapping transforming circles going through the origin (IP) into straight lines which are then identified using a Cellular-Automaton.

The correct reconstruction of the kinematics of charged particles requires a sufficiently detailed description of the material the particles have traversed, in order to correctly account for effects of energy-loss and multiple-scattering in the fit. The DD4hep component DDRec provides dedicated surface classes for track reconstruction and fitting. These surface classes provide the geometric information of the corresponding measurement surfaces as well as material properties, averaged in a suitable way. Surfaces are also used to account for effects from dead material layers, such as support structures or cables and services.

The resulting tracking efficiencies for the ILD detector are shown as a function of the momentum and  $\cos(\theta)$  in Fig. 37.

The normalised transverse momentum resolution  $\sigma(1/p_T)$  for single-muon events the SiD detector model is shown in Fig. 38 together with fits using the parameterisation:

$$\frac{\sigma(p_T)}{p_T^2} = a \oplus \frac{b}{p \sin\theta} \tag{15}$$

Comparable results are obtained for ILD, and both detector concepts achieve their design goals for the momentum resolution of  $\sigma(p_T)/P_T^2 < 2 \times 10^{-5} \text{GeV}^{-1}$  for high momentum central tracks.

The impact parameter resolution as a function of polar angle for single-muon events in SiD is shown in Fig. 39 for different particle momenta. A resolution of a few  $\mu$ m is achieved for high mometum tracks over a large range of the polar angle down to ~ 20°.

The tracking software is completed with dedicated processors for the identification and reconstruction of kinks and  $V^0$ s. Tracks with kinks can arise from bremsstrahlung, typically for electrons, or a large angle deflection due to multiple scattering.  $V^0$ s are almost exclusively decays of  $K_s^0$  and  $\Lambda^0$  and gamma conversions.

## 7.5.2. Particle Flow:

The *particle flow algorithm* (PFA) aims at reconstructing every individual particle created in the event in order to take the best available measurement for the given particle type:

• charged particles

using the momentum measured in the tracking



FIG. 37: Tracking efficiency for  $t\bar{t}$ -events at  $\sqrt{s} = 500 \text{ GeV}$ in the ILD detector as a function of momentum  $(\cos(\theta) > .99)$  [upper] and  $\cos(\theta)$  (p > 1 GeV) [lower] for prompt tracks  $(d_{IP} < 10 \text{ cm})$ . Decays in flight are excluded and tracks are required to have left at least 4 hits in the detector. Background from  $e^+e^-$ -pairs for two bunch crossings is overlaid to the  $t\bar{t}$ -events.

detectors with the excellent resolution described above.

• photons

measured in the Ecal with an energy resolution of  $\sigma(E)/E \sim 17\%/\sqrt{(E/\text{GeV})}$ .

• neutral hadrons measured predominantly in the HCAL<sup>5</sup> with an energy resolution of  $\sigma(E)/E \sim 50\%/\sqrt{(E/\text{GeV})}$ .

<sup>&</sup>lt;sup>5</sup> Hadronic showers often start in the ECAL and might extend into the Muon system. This is taken into account in PandorPFA.



FIG. 38: Normalised transverse momentum resolution for single-muon events as function of momentum in the SIDLOI3 simulation model (from [5]). The dashed lines are fits to the data points according to eq. 15.



FIG. 39: Impact parameter resolution  $\sigma(d_0)$  for single-muon events as function of polar angle in the *SIDLOI3* simulation model (from [5]).

The best jet energy measurement in hadronic events would be achieved if the above algorithm would work perfectly. However in reality there is always confusion in the assignment of individual *CalorimeterHits* to Clusters and showers as well as in the assignment of tracks to clusters. This effect is demonstrated in Fig. 40 for PandoraPFA [173], the implementation of PFA available in iLCSoft that is used by both detector concepts.

The input to PandoraPFA are collections of Tracks, Kinks,  $V^0$ s and collections of all digitized *CalorimeterHits* together with some geometrical information retrieved from DDRec. Following [173] the main steps of the algorithm are:

• CalorimeterHits are clustered using a simple cone-



FIG. 40: Jet energy resolution (in %) for Z' events as a function of the jet energy in a realistic detector for PandoraPFA. Also shown are the effect of *confusion* and the result assuming *perfect PFA* (from [173]).

based algorithm, seeded either from isolated hits in the first calorimeter layers or by the projection of Tracks to the front face of the ECAL.

- the clustering algorithm is configured to prefer splitting of clusters rather than risking to falsely merge particles into single clusters.
- Clusters are associated to Tracks based on topological (position and direction) and kinematic (momentum and energy) consistency. In case of significant discrepancies a re-clustering is initiated.
- Clusters without associated Tracks are transformed into neutral *ReconstructedParticles* unless they can be more likely interpreted as fragments of charged particles.
- consistent Track-Cluster combinations are transformed into charged *ReconstructedParticles*.
- particle identification plugins are applied to label specific particle types, such as photons, electrons and muons.
- a dedicated weighting procedure known as *software compensation* is applied to the hits inside a cluster in order to equalize hadronic and electromagnetic shower components.

The final output collection of PandoraPFA is a set of objects called "PandoraPFO"s. This represents the final output of the *Reconstruction* process. This collection is either directly used for physics analyses or serves as input to higher-level reconstruction algorithms where necessary.



FIG. 41: Upper: Jet energy resolution for  $Z \rightarrow u, d, s$  events as a function of the jet energy in the standard ILD simulation model. Lower: The resulting jet energy scale for the same events.

Fig. 41 shows the jet energy resolution and jet energy scale that is achieved for two variants of the ILD detector for a dedicated event sample of hadronic  $Z \rightarrow u, d, s$  events. The jet energy resolution is evaluated using  $RMS_{90}(E)$ , the root mean square of the energy of the central 90% of the events. The restriction to u, d, s quarks is chosen to focus on the detector and PFA performance without the extra complication of missing energy due to neutrinos.

## 7.6. High-level reconstruction

After having reconstructed all of the individual particles in the event, the next step in the processing is the reconstruction of primary and secondary vertices. This is carried out in iLCSoft with the LCFIPlus [174] package that is also used for the tagging of heavy flavor jets.

The primary vertex of the event is found in a teardown procedure. First an initial vertex is fitted by a  $\chi^2$ -minimization using all charged tracks in the event and a constraint from the expected beam spot ( $\sigma_x =$ 516 nm,  $\sigma_y = 7.7$  nm,  $\sigma_z \sim 200 \ \mu m$  at  $E_{cms} = 250 \text{ GeV}$ ). Then all tracks with a  $\chi^2$ -contribution larger than a given threshold value are removed.

In a second step LCFIPlus tries to identify secondary vertices, starting out from forming all possible track-pairs from tracks not used in the primary vertex. The pairs have to fulfill suitable requirements with respect to their invariant mass, momentum direction and  $\chi^2$ .  $V^0$ s are excluded from these initial pairs. Secondary vertices are then formed using so far leftover tracks in an iterative procedure and eventually adding compatible tracks originally used in the primary vertex.

Secondary vertices and optionally isolated leptons can be used by LCFIPlus for jet clustering, aiming at high efficiency for correctly identifying heavy flavor jets. The actual jet clustering is then performed by using a conebased clustering with a Durham-like algorithm. Alternatively users can use  $k_T$  jet clustering algorithms from Fastjet [175], which is interfaced to Marlin in a dedicated package MarlinFastJet.

LCFIPlus also provides algorithms for jet flavor tagging using boosted decision trees (BDTs) based on suitable variables from tracks and vertices. Fig. 42 shows the mis-identification efficiency for jets from light quarks and c-quarks as a function of the b-tagging efficiency for the SiD detector using LCFIPlus.

There is a large palette of additional high level reconstruction algorithms available in iLCSoft addressing the needs for physics analyses, e.g.

- particle identification using dE/dx, shower shapes and multi-variate methods
- $\gamma\gamma$ -finders for the identification of  $\pi^0$ s and  $\eta$ s
- reconstructed particle to Monte-Carlo truth linker for cross checking analysis and reconstruction efficiencies
- tools for jet clustering using Monte-Carlo truth information
- processors for the computation of various event shapes

## 7.7. Fast simulation

In addition to the full simulation and reconstruction outlined in the previous sections, there is a need for simulation that can quickly generate substantial samples of



FIG. 42: Mis-identification efficiency of light quark jets (red points) and charm jets (green points) as beauty jets versus beauty identification efficiency in di-jets events at  $\sqrt{s} = 91 \text{ GeV}$  (from [5]).

simulated and reconstructed events. Situations where this is desirable include detector optimisation and new physics searches. In these cases, similar processes need to be simulated and reconstructed at a, possibly very large, number of different conditions. In the first case, one needs to modifying various aspects of the detector in steps, in the latter, one needs to explore the entire allowed parameter space of a theory for new physics. In addition to these cases, fast simulation is also an asset for simulating high cross section SM processes, such as  $\gamma\gamma$  processes, where the investment in processor power and intermediate storage might be prohibitively large to attain the goal that simulation statistics should be a negligible source of systematic uncertainty.

To meet these needs, a fast simulation program needs to be fast, flexible, and accurate. The SGV program [176] used at ILC meets these needs. The time to simulate and reconstruct an event is similar to the time it takes to generate it ( $\sim 1 - 10$  ms). The response of the detector is as far as possible calculated from the detector design (so there is no need to parametrisise pre-existing full simulation results). SGV has been shown to compare well both with full simulation and with real data [177].

The program uses a simplified "cylinders-and-discs" description of the detector, which is used to calculate the Kalman-filtered track-helix covariance matrix of each generated charged particle. By Cholesky decomposition of the covariance matrix, the track-parameters are simulated in a way such that all correlations are respected. The calorimetric response is calculated from the expected single-particle performance of the different components of the calorimetric system, for each particle impinging on it. Optionally, the effects of shower-confusion can be

included. To reduce the needed storage for a Giga-event size sample, event filtering can be applied at different steps of the processing, directly after generation, after the detector response is known, or after higher-level event analysis is done. Events passing all filters are output in LCIO DST-format, and can seamlessly be further analysed within the Marlin framework.

## 7.8. Computing concept

An initial computing concept for the ILC, including a first estimate of the required resources, has been developed by the LCC Software and Computing Group.

The foreseen computing concept follows in general terms that of the current LHC experiments and Belle II, with a strong on-site computing center complemented by large Grid-based computing resources distributed around the world. This concept is schematically shown in Fig. 43.

Due to the much lower event rates at the ILC compared to the LHC, we will be able to run in an un-triggered mode in which collision data from every bunch crossing will be recorded. At the experimental site, we require only limited computing resources for online monitoring, QA and data-buffering for a few days.

Prompt reconstruction, event building, and filtering of the interesting collisions will be performed at the main ILC campus. A small fraction of the initial raw data will be distributed to major participating Grid sites in the world for further skimming and final redistribution for physics analysis. A copy of the raw data from all bunch crossings will be kept to allow for future searches for new exotic signatures.

## 7.9. Computing resource estimate

Based on our detailed physics and background simulations, we estimate the total raw data rate of the ILC to be  $\sim 1.5$ GB/s.

The total estimated storage needs will be a few tens of PB/y. The computing power needed for simulation, reconstruction, and analysis will be a few hundred kHep-Spec06. Given that these numbers are already smaller than what is now needed by the LHC experiments, and given an expected annual increase of 15% and 20%, respectively, for storage and CPU at flat budget, we expect the overall computing costs for the ILC will be more than an order of magnitude smaller than those for the LHC.

## 8. PHYSICS SIMULATIONS: HIGGS

The physics case for the precision study for the Higgs boson presented in Section 4 will be realized through the measurement of total cross sections and  $\sigma \cdot BR$  values for the various final-states. The major Higgs production cross sections at the ILC are shown in Fig. 44 as a function of centre of mass energy for the optimal choice (-80%/+30%) of ILC beam polarisations. In Tab. XI, we present our estimates for the statistical errors that will be



FIG. 43: Computing concept foreseen for the ILC, distributed over on-site computing at the interaction region, the main campus and Grid-like offline computing.

obtained for the total cross section for  $e^+e^- \rightarrow ZH$  and for the  $\sigma \cdot BR$ s for this process and the WW fusion process, for a reference luminosity sample of 250 fb<sup>-1</sup> and for three different ILC energies. There is a similar table for the opposite beam polarisation state (+80%/-30%). In this case, the errors for ZH observables are almost the same, due to a compensation of lower background and lower signal cross sections. The WW fusion process has a much reduced cross section and comparably lower precision[3]. These estimates are based on full-simulation analyses using the tools presented in Sec. 7. The purpose of this section is explain how these numbers are obtained, what the factors are that limit them, and how these limitations might be relaxed.

We begin with the observation that precision Higgs

measurements will be much easier to obtain at a lepton collider than at a hadron collider. Table XII gives the typical signal efficiencies for ILC analyses and the corresponding signal to background ratios (S/B) after final cuts. The difference with LHC can be clearly seen using the example of  $H \rightarrow b\bar{b}$  measurements. The decay of  $H \rightarrow b\bar{b}$  has been discovered by ATLAS and CMS [178, 179] with a significance of  $5.4\sigma$ ,  $5.5\sigma$ , respectively, after producting about 4 million Higgs events per experiment. At the ILC, with only 400 Higgs events which will be produced with an integrated luminosity of 1.3 fb<sup>-1</sup> (corresponding to 2 days of running time), the decay of  $H \rightarrow b\bar{b}$  will be measured with a similar significance, around  $5.2\sigma$  according to the full simulation result [180]. The S/B ratios for these analyses are il-



FIG. 44: Cross sections for the three major Higgs production processes as a function of center of mass energy, from [138].



FIG. 45: Upper: signal  $H \rightarrow b\bar{b}$  and background events in different categories of S/B measured by ATLAS [178, 179] using LHC Run 2 data; lower: signal  $h \rightarrow b\bar{b}$  and

background events in the  $b\bar{b}$  mass spectrum expected from the ILC full simulation [180].

 $-80\% e^{-}, +30\% e^{+}$  polarization:

	$250 \mathrm{GeV}$		350 (	$350 { m GeV}$		$500 \mathrm{GeV}$	
	Zh	$\nu \overline{\nu} h$	Zh	$\nu \overline{\nu} h$	Zh	$\nu \overline{\nu} h$	
$\sigma$	2.0		1.8		4.2		
$h \rightarrow invis.$	0.86		1.4		3.4		
$h \to b\overline{b}$	1.3	8.1	1.5	1.8	2.5	0.93	
$h \to c \overline{c}$	8.3		11	19	18	8.8	
$h \to gg$	7.0		8.4	7.7	15	5.8	
$h \to WW$	4.6		$5.6^{*}$	$5.7^{*}$	7.7	3.4	
$h \to \tau \tau$	3.2		$4.0^{*}$	$16^{*}$	6.1	9.8	
$h \rightarrow ZZ$	18		$25^*$	$20^*$	$35^*$	$12^{*}$	
$h \to \gamma \gamma$	$34^{*}$		$39^{*}$	$45^{*}$	47	27	
$h \rightarrow \mu \mu$	72		$87^*$	$160^{*}$	120	100	
a	7.6		$2.7^{*}$		4.0		
b	2.7		$0.69^{*}$		0.70		
$\rho(a,b)$	-99.17		$-95.6^{*}$		-84.8		

TABLE XI: Projected statistical errors, in %, for Higgs boson measurements. The errors are quoted for luminosity samples of 250 fb<sup>-1</sup> for  $e^+e^-$  beams with -80% electron polarization and +30% positron polarization. Except for the first and last segments of each set, these are measurements of  $\sigma \cdot BR$ , relative to the Standard Model expectation. The top lines gives the error for the total cross section relative to the Standard Model and the 95% confidence upper limit on the branching ratio for Higgs to invisible decays. The

bottom lines in each half give the expected errors on the a and b parameters and their correlation (all in %) for  $e^+e^- \rightarrow Zh$  (see (21). All error estimates in this table are

based on full simulation, and the entries marked with a \* are extrapolated from full simulation results.

measurement	efficiency	S/B final.
$\sigma_{Zh}$ in $\mu^+\mu^-h$	88%	1/1.3
$BR(h \to b\overline{b})$ in $q\overline{q}h$	33%	1/0.89
$BR(h \to \tau \tau)$ in $q\overline{q}h$	37%	1/0.44
$BR(h \to WW)$ in $\nu \overline{\nu} h$	20%	1/1.6

TABLE XII: Typical signal efficiencies (second column) and signal over background ratio (S/B) after the final cuts (third column) for some of the representative Higgs measurements (first column) at the ILC.

lustrated in Fig. 45. Clearly, if one wishes to measure the rate for  $h \rightarrow b\bar{b}$ , there are strong advantages in starting from a situation in which the signal stands well above any background process that would need to be controlled. The challenge of physics at a linear collider is to make use of this advantage in the most optimal way and realize the potential to achieve very high precision.

A full simulation analysis contains two components. The first is the detector simulation. This provides the realistic interactions between each final state particle and any part of the detector that the particle passes through, including creation of new particles during the interaction; concrete algorithms for tracking, particle flow analysis, vertex reconstruction and particle identification; the resulting performance of the various detector resolutions for track momentum, jet energy, and impact parameters; and the efficiencies for tracking, flavor tagging, and isolated lepton finding. These aspects have already been described in Section 7. The second component is the event seletion, that is, the algorithms for discriminating between signal and background events. That will be our main concern in the discussion of this section.

First, however, we would like to emphasize to the reader a number of effects that are included in the detector modelling and event generation, and that must be included for a solid estimate of detection efficiencies and signal-background discrimination:

- beamstrahlung and ISR are implemented in the event generators for both signal and background processes. These effects are important for estimation of signal and background contributions in the analyses that make use of the nominal value of the centre-of-mass energy. A representative example is seen in Section 8.2.1, Fig. 46, for the determination of the Higgs boson mass from Z recoil. Both beamstrahlung and ISR effects will drag signal events from the more sensitive peak region to the less sensitive tail region, and at the same time will induce more background contribution in the signal region.
- overlay of beam background events is implemented in every signal and background event sample. This will affect the performance of reconstructed variables related to jets and hence degrades the signal and background discrimination. There is a method to partially remove the effect of this events which will be introduced in next section.
- full Standard Model background is checked in all of the analyses to be described, in order not to miss any significant contribution. For example, 2fermion events developed with a parton shower can become background for the 4-fermion signal. Another example is the background contribution to Higgs observables that comes from tail of the Breit-Wigner structure of a Z boson in  $e^+e^- \rightarrow ZZ$ . It is not correct neither to neglect the Z natural width nor to ignore the similar diagram with the  $\gamma$  propagator.
- explicit jet clustering and jet paring algorithms are used in all analyses. These often become the limiting factors in the analyses with 4 or more jets in the final state. The confusion between two color singlets, for instance Z and h in  $e^+e^- \rightarrow Zh \rightarrow 4jets$ , could produce a much wider spread of the reconstructed dijet invariant mass than that due to the pure detector resolution. Hence, simply smearing the dijet mass variable at the parton level according to the detector resolution is often too optimistic.
- *control of systematics* is taken into account in the design of every selection cut.

This section is organized as follows. In Sec. 8.1, we will introduce the common procedures for event selections.

Section 8.2 will discuss the analyses for the main Higgs observables. The analysis strategies and selection cuts in some representative channels will be discussed in great detail. Section 8.4 presents some estimates for improvement of the key algorithms in the future. Section 8.5 gives a dedicated discussion of the measurement of Higgs self-coupling.

### 8.1. Common procedures for event selections

The full simulation analysis at the event selection level can be described in two steps: *pre-selection* and *finalselection*. At the pre-selection step each signal event is characterized according to its final states at parton level by numbers of isolate leptons (meaning electron or muon unless otherwise stated), isolated taus, isolated photons and jets, and nature of missing momentum. Here isolated particle is meant to be not coming from a jet. The procedures for the pre-selection are typically as follows:

- isolated lepton finder, which will try to reconstruct the isolated leptons in each event. The main algorithms are implemented in the processor called IsolatedLeptonTagging in the iLCSoft, based on a multivariate method. It starts with selecting energetic electron/muon (momentum P > 5GeV), from the reconstructed particles collection. by requiring the particle has characteristic energy fractions deposited in each sub-detector, namely  $E_{ecal}/E_{tot}, E_{tot}/P, E_{yoke}$ , where  $E_{ecal}$  ( $E_{hcal}$ ) is the energy deposited in ECAL (HCAL),  $E_{tot}$  is the sum of  $E_{ecal}$  and  $E_{hcal}$ , and  $E_{yoke}$  is the energy deposited in Yoke. For electron, it is required that  $E_{ecal}/E_{tot} > 0.9$  and  $0.5 < E_{tot}/P < 1.3$ . For muon, it is required that  $E_{tot}/P < 0.3$  and  $E_{yoke} > 1.2$  GeV. The selected electron/muon is then further required to have impact parameters consistent with that from primary vertex. Double cones are then defined around that electron/muon, and variables such as the energies of the charged and neutral particles within a cone are utilized for isolation requirement. The exact criteria for isolation are realized by a MVA, trained using true isolated leptons as signal and leptons from jets as background. A cut on the MVA output is then required as the last step of isolated lepton finder.
- isolated tau finder, which will try to reconstruct the isolated taus. The main algorithms are implemented in TaFinder in the iLCSoft. It starts with finding the most energetic charged particle as a tau candidate. Then the remaining most energetic particle which is within a cone of  $\cos \theta = 0.99$  around the tau candidate will be combined to the tau candidate if the invariant mass of the combined tau candidate does not exceed 2 GeV. This combining step will be iterated until there is no any more particle to combine. The resulting combined tau candidate is identified as an isolated tau.

- isolated photon selection, which will try to reconstruct the isolated photon. A photon is first identified based on its cluster properties by PandoraPFA. For most of the signal processes with an isolated photon, it is usually sufficient to tag the most energetic photon which has energy larger than several tens of GeV, as the candidate isolated photon. If there are other photons within a very small cone of  $\cos \theta = 0.999$  around the candidate photon, those other photons are most probably split ones hence are merged into the candidate photon.
- overlay removal, which will try to remove the pileup beam background events in every event. An exclusive jet clustering is performed using longitudinal invariant  $k_t$  algorithm [181] for all the particles except the selected isolated lepton/tau/photon in above step. As a result, the particles from beam background events, which usually have very low- $p_t$ , are clustered into beam jets and are effectively removed by the exclusive jet clustering process. The input parameters such as R and number of required jets are carefully optimized for each signal process. Alternative algorithms include anti- $k_t$  [182] and Valencia [183].
- jet clustering and flavor tagging, are done using LCFIPlus as introduced in 7.6. All the particles belonging to the jets obtained in previous step are then re-clustered into a few jets using another inclusive jet clustering algorithm, Durham algorithm [184]. Each jet is flavor tagged using the reconstructed information of its secondary and tertiary vertices.

At the final-selection step, the reconstructed leptons, taus, photons and jets will be first combined to reconstruct W, Z, h or top according to the signal. Then various cuts will be applied to further suppress background events. Details are explained measurement by measurement in the following. Unless stated otherwise, the analysis is done at  $\sqrt{s} = 250$  GeV, a nominal integrated luminosity of 250  $\text{fb}^{-1}$  is assumed, and the cuts and results are illustrated with left-handed beam polarization  $e_L^- e_R^+ : P(e^-, e^+) = (-0.8, +0.3).$  Additional comments will be given when  $\sqrt{s}$  or right-handed beam polarization  $e_{R}^{-}e_{L}^{+}: P(e^{-}, e^{+}) = (+0.8, -0.3)$  has a significant impact on the results. The results are straightforwardly extrapolated into that for the running scenario introduced in Sec. 3 and are then used as input for the Higgs coupling determination by a global fit introduced in Sec. 4. The full information for the uncertainties of Higgs observables for  $e_L^- e_R^+$  and  $e_R^- e_L^+$  can be found in Tab.6 of Ref. [3].

## 8.2. Analyses for Higgs observables

## 8.2.1. $m_h$ and $\sigma_{Zh}$

The signal processes are  $e^+e^- \rightarrow Zh$ ,  $Z \rightarrow l^+l^-$  or  $q\bar{q}$ and  $h \rightarrow$ anything. Thanks to the known four momenta of initial states, the four momentum of final state h can be reconstructed as the recoil against the four momentum of Z, which is directly measured from its decay products  $l^+l^-$  or  $q\bar{q}$ . The mass of  $h(m_X)$  can therefore be reconstructed as

$$m_X^2 = s + m_Z^2 - 2E_Z\sqrt{s}, (16)$$

where  $m_Z$  and  $E_Z$  are measured mass and energy of Z respectively. The signal events can hence be tagged without looking at the decay products of h. This technique is traditionally called *recoil mass* technique, and the two types of signal processes  $(Z \to l^+ l^- \text{ and } Z \to q\bar{q})$  are called leptonic recoil and hadronic recoil channels. The recoil mass technique makes possible the measurement of the inclusive cross section of  $e^+e^- \to Zh \ (\sigma_{Zh})$ , that plays a unique role in the determination of the absolute values of Higgs couplings as explained in Sec. 4. Meanwhile, the Higgs mass  $(m_h)$  can be straightforwardly determined by the  $m_X$  spectrum. The detailed analyses for leptonic recoil channels  $\mu^+\mu^-h$  and  $e^+e^-h$  and for hadronic recoil channel  $q\bar{q}h$  can be found respectively in references [185] and [186–188]. For simplicity only the analysis for  $\mu^+\mu^-h$  channel is illustrated in detail here.

The event pre-selection in  $\mu^+\mu^-h$  channel starts with requiring at least two isolated muons with opposite charges and invariant mass  $(m_{ll})$  consistent with the Z mass (in the range  $m_{ll} \in [50, 130]$  GeV). It is quite possible that one or two muons in such a candidate muon pair are actually from Higgs decay, for instance from  $h \rightarrow ZZ^*/WW^*/\tau^+\tau^- \rightarrow \mu^+\mu^- + X$ . To minimize the possibility of this case, or to maximize the possibility that the candidate muon pair is indeed from the primary Z decay, the following strategy is taken: when there are more than one such candidate muon pairs, the pair which minimizes following  $\chi^2$ 

$$\chi^{2} = \left(\frac{m_{ll} - M_{Z}}{\sigma_{Z}}\right)^{2} + \left(\frac{m_{X} - M_{h}}{\sigma_{h}}\right)^{2}$$
(17)

is identified as from the primary Z decay. Here  $M_Z$ is 91.2 GeV,  $M_h$  is 125 GeV,  $\sigma_Z$  and  $\sigma_h$  are resolutions for Z mass and recoil mass reconstructions. After the pre-selection, the remaining background events are dominated by leptonic and semi-leptonic decays of  $e^+e^- \rightarrow ZZ$ , leptonic decay of  $e^+e^- \rightarrow WW$ , and leptonic decay of  $e^+e^- \rightarrow \gamma Z$ .

In the final selection, the cuts  $p_T^{ll} > 10$  GeV and  $|\cos \theta_{mis}| < 0.98$ , where  $p_T^{ll}$  is the transverse momentum of muon pair and  $\theta_{mis}$  is the polar angle of missing four momentum, are applied to suppress  $\gamma Z$  background events.  $E_{vis} > 10$  GeV, where  $E_{vis}$  is the visible energy other than the muon pair, and  $m_{ll} \in [73, 120]$  GeV are applied to suppress WW background events. ZZ as well as WW and  $\gamma Z$  background events are further suppressed by a dedicated BDT cut which is trained using distributions of polar angle of the muon pair. After a final cut that requires  $m_X \in [110, 155]$  GeV, the remaining



FIG. 46: Recoil mass spectrum against  $Z \to \mu^+ \mu^-$  for signal  $e^+e^- \to Zh$  and SM background at 250 GeV [185].



FIG. 47: Recoil mass spectrum against  $Z \to \mu^+ \mu^-$  for signal  $e^+e^- \to Zh$  and SM background at 500 GeV [185].

signal and background events are shown in the  $m_X$  spectrum in Fig. 46 for the  $Z \rightarrow \mu^+ \mu^-$  channel, where the signal peak is clearly seen. The overall signal efficiency is 88%, with an average signal over background ratio of 1/1.3.

The number of signal events and its statistical uncertainty are obtained by fitting  $m_X$  spectrum with signal component modeled by a kernel function and background component modeled by a third order polynomial, shown in Fig. 46. As shown by the green histogram in Fig. 46, the signal spectrum has a considerable non-Gaussian tail in the high mass end, which is due to the overestimate of effective  $\sqrt{s'}$  in  $e^+e^- \rightarrow Zh$  reaction when beamstrahlung and ISR effects are included, recall Eqn. 16. It's worth noting that these effects become so significant at  $\sqrt{s} = 500$  GeV, as shown in Fig. 47, that the measurement uncertainty could be underestimated by a factor of 2 if the effects are not properly included in the simulation.

For  $e_L^- e_R^+$ , the estimate of relative uncertainty on  $\sigma_{Zh}$  measurement  $(\delta\sigma_{Zh})$  is 2.5% for the leptonic recoil channel, where the contribution from  $e^+e^-h$  channel is

slightly smaller than  $\mu^+\mu^-h$  channel due to the higher electron bremsstrahlung. For  $e_R^-e_L^+$ ,  $\delta\sigma_{Zh}$  is estimated to be 2.9%. By combining the hadronic recoil channel,  $\delta\sigma_{Zh}$  is estimated to be 2.0% for both  $e_L^-e_R^+$  and  $e_R^-e_L^+$ , as shown in Tab. XI. The enabled measurement of leftright asymmetry for  $\sigma_{Zh}$  plays a very important role in the EFT fit as explained in Sec. 4. The Higgs mass  $m_h$ is also measured from the fit shown in Fig. 46. The estimate of  $m_h$  uncertainty is 14 MeV for ILC250, with the dominant contribution from  $\mu^+\mu^-h$  channel. The uncertainty in the Higgs boson mass  $(\delta m_h)$  does play a role as a source of systematic error for predictions of Higgs boson couplings. In most cases,  $\Delta m_h \sim 100$  MeV would be already sufficient, but this is not true for  $h \to ZZ^*$  or  $h \to WW^*$ . It has been pointed out in [118] that

$$\delta_W = 6.9 \cdot \delta m_h, \quad \delta_Z = 7.7 \cdot \delta m_h, \tag{18}$$

where  $\delta_W$  and  $\delta_Z$  are the relative errors for g(hWW) and g(hZZ) respectively. At ILC250, the 14 MeV accuracy for Higgs boson mass results in systematic errors of 0.1% for  $\delta_W$  and  $\delta_Z$ .

$h \rightarrow$		bb	cc	gg	$\tau\tau$	$WW^*$	$ZZ^*$	$\gamma\gamma$	$\gamma Z$
eff.	[%]	88.25	88.35	87.98	88.43	88.33	88.52	88.21	87.64

TABLE XIII: The efficiencies of the major SM Higgs decay modes, after all the event selection cuts, shown here for the case of the  $\mu^+\mu^-$ h channel and  $e_L^-e_R^+$  at  $\sqrt{s}=250$  GeV [185]. The uncertainties due to finite MC statistics on these values are below 0.14%.

As pointed out in the very beginning of this analysis, the key idea which enables the inclusive  $\sigma_{Zh}$  measurement is that the signal is tagged independently of Higgs decay modes. Hence it is crucial to examine whether all the pre-selection and final-selection cuts satisfy this criterion. This can be verified by checking the signal efficiency for each individual Higgs decay mode and evaluating the efficiency uniformity among all the decay modes. Table XIII lists the efficiencies of major SM Higgs decay modes after all cuts in the  $\mu^+\mu^-h$  channel. It is seen that there is no discrepancy in efficiencies of SM decay modes beyond 1%. This is not a surprise because the analysis strategies and selection cuts are carefully designed to make it so. The cut  $E_{vis} > 10$  GeV may deserve a few more words, since it apparently suppresses the  $h \rightarrow invisible$  mode. The strategy behind is that  $\sigma_{Zh}$  can be measured as

$$\sigma_{Zh} = \sigma_{Zh}^{vis} + \sigma_{Zh}^{inv}, \tag{19}$$

where  $\sigma_{Zh}^{vis}$  is the total cross section for all  $h \rightarrow visible$ modes, which is measured here, and  $\sigma_{Zh}^{inv}$  is the cross section for  $h \rightarrow invisible$  mode, which can be measured separately, described in Sec. 8.2.6. A detailed and quantitative analysis taking into account the possibility of existing BSM decay modes is performed in [185]. It concludes that the relative bias on  $\sigma_{Zh}$ , induced by the Higgs decay modes dependence, can be controlled at below 0.1% (0.2%) for the  $\mu^+\mu^-h$   $(e^+e^-h)$  channel, which is much smaller than the expected statistical uncertainty even at the full ILC250.

In the hadronic recoil channel, a more complicated strategy is applied in order to keep the analysis still decay modes independent. Instead of the simple categorization into visible and invisible modes in leptonic channel, the signal events in hadronic channel are categorized according to number of taus, number of leptons, and number of jets in the final state. In principle, as long as the categories are inclusive, we can design and optimize the selection cuts category by category. The studies in [186] show that by varying the SM decay branching ratios by  $\pm 5\%$  (absolute) in each decay mode, the bias on measured  $\sigma_{Zh}$  is at most around 0.5% relatively. More efforts would be needed in future to further reduce the bias to a much lower level in particular even under assumption that there would be other unknown exotic decay modes. At higher  $\sqrt{s}$ , the hadronic recoil analysis generally becomes less challenging, because the two jets from primary Z are more boosted hence are easier to be identified from the Higgs decay products, as studied in [187, 188] for  $\sqrt{s} = 350$  and 500 GeV.

## 8.2.2. $\sigma_{\nu\nu h}$ and $\sigma_{eeh}$

The second leading Higgs production process,  $e^+e^- \rightarrow \nu \overline{\nu} h$  via *W*-fusion, provides a direct measurement for *hWW* coupling. It plays a crucial role in the global fit based on  $\kappa$  formalism, and still helps improve the global fit results based on EFT formalism even though the cross section is not very large at  $\sqrt{s} = 250$  GeV,  $\sigma_{\nu\nu h} = 14$  fb for  $e_L^- e_R^+$ . The signal channel used is  $e^+e^- \rightarrow \nu \overline{\nu} h$ ,  $h \rightarrow b\overline{b}$ , in which direct observable is  $\sigma_{\nu\nu h} \cdot BR_{bb}$ . Together with  $BR_{bb}$  measurement by Zh process,  $\sigma_{\nu\nu h}$  is then measured. The analysis is briefly described here, and more details can be found in [189, 190].

The signal final states consist of two b-jets and two missing neutrinos. The pre-selection starts with vetoing events with one or more isolated leptons. Then jet-clustering and flavor tagging are performed with expected number of jets equals 2. The two jets are required that in each jet there are at least 6 reconstructed particles and  $Y_{3\rightarrow 2} < 0.1$ , where  $Y_{3\rightarrow 2}$  is the jet distance value from 3 jets to 2 jets step defined by Durham algorithm. The b-tagging of the two jets are required to be btag1 > 0.8and btag 2 > 0.2. The di-jet invariant mass is required to be  $m_{bb} \in [110, 150]$  GeV. The missing mass, defined as the recoil mass against the di-jet, is required to be larger than 20 GeV. After the pre-selection, the remaining dominant background events are from  $\gamma Z \ (Z \to b\bar{b})$ ,  $\nu \overline{\nu} Z \ (Z \to b\overline{b}) \text{ and } Zh \ (Z \to \nu \overline{\nu}, h \to b\overline{b}).$ 

In the final selection,  $\gamma Z$  and  $\nu \overline{\nu} Z$  background events are further highly suppressed by a BDT cut, which is trained using input variables di-jet mass, polar angle of di-jet, angle between two jets, and  $Y_{2\rightarrow 1}$ . The remaining signal and background events are plotted in the missing mass spectrum, shown in Fig. 48 (upper). The signal effi-



FIG. 48: Missing mass spectrum (upper) and Higgs mass spectrum (lower) for the signal  $e^+e^- \rightarrow \nu \overline{\nu} h, h \rightarrow b\overline{b}$  and the SM background at 250 GeV and 500 GeV respectively [189, 190].

ciency is 36% and the average signal over background ratio is around 1/4. The most dominant background events turn out to come from  $Zh \ (Z \to \nu \overline{\nu})$  and have significant overlap with signal events in the missing mass spectrum. This is because the invariant mass of  $\nu \overline{\nu}$  of signal events can not be far away from  $M_Z$ , limited by available phase space at  $\sqrt{s} = 250$  GeV. Therefore it is necessary to fit simultaneously  $\sigma_{\nu\nu h} \cdot BR_{bb}$  and  $\sigma_{Zh} \cdot BR_{bb}$ . Note a useful constraint can be added into the fit that  $\sigma_{Zh} \cdot BR_{bb}$  is also measured using  $Z \to l^+l^-$  and  $Z \to q\overline{q}$  channels. As a result, the estimate of relative uncertainty on  $\sigma_{\nu\nu h} \cdot BR_{bb}$ is 8.1%, shown in Tab. XI, and the correlation between  $\sigma_{\nu\nu h} \cdot BR_{bb}$  and  $\sigma_{Zh} \cdot BR_{bb}$  is -34%.

The left-handed beam polarisation does help significantly the  $\sigma_{\nu\nu h}$  measurement here, simply because it enhances the cross section by a factor of 2.34. The  $\sigma_{\nu\nu h}$  can be measured much better at  $\sqrt{s} = 500$  GeV, shown in 48 (lower), thanks to a fact of 10 increase on cross section and much easier separation with Zh ( $Z \rightarrow \nu \overline{\nu}$ ).

The third leading Higgs production process,  $e^+e^- \rightarrow e^+e^-h$  via Z-fusion, is not easy to measure due to its very small cross section at  $\sqrt{s} = 250$  GeV,  $\sigma_{eeh} = 0.7$  fb. A full simulation analysis is performed and suggests that this process is already discoverable at  $\sqrt{s} = 250$  GeV with 2 ab<sup>-1</sup> and  $\sigma_{eeh}$  can be measured with a significance



FIG. 49: Template of b-likeliness versus c-likeness for signal  $h \to b\bar{b}/c\bar{c}/gg$  (bottom left/middle/right) events, and for  $h \to others /$  SM background (top middle/right) events, and distribution for all the events (top left), in  $Z \to qq$  channel normalized to 250 fb<sup>-1</sup>. The b-likeness is defined as a combined function of the two b-tags (say  $x_1$  and  $x_2$ ) of the two jets from h candidate:  $b - \text{likeness} = \frac{x_1 x_2}{x_1 x_2 + (1-x_1)(1-x_2)}$ . The c-likeness is defined in a similar way.

of  $9\sigma$  [180]. At  $\sqrt{s} = 500$  GeV, the significance will be significantly improved to  $60\sigma$ .

and h candidates by minimizing the  $\chi^2$  defined as

$$\chi^2 = \left(\frac{m_{j_1 j_2} - M_Z}{\sigma_Z}\right)^2 + \left(\frac{m_{j_3 j_4} - M_h}{\sigma_h}\right)^2,$$

8.2.3. BR
$$(h \rightarrow bb/c\overline{c}/gg)$$

The capabilities of making precise measurements for  $BR(h \to c\bar{c}/qg)$  demonstrate another unique advantage of a lepton collider, enabled by: (1) clear separation between b-jets, c-jets and light quark/gluon jets thanks to the excellent flavor tagging performance introduced in Sec. 7; and (2) the democracy about cross sections between Higgs processes and other SM background processes induced by electroweak interactions. The branching ratios BR $(h \rightarrow b\bar{b}/c\bar{c})$  offer important measurements of the Yukawa couplings between the Higgs boson and third/second generation quarks. BR $(h \rightarrow qq)$  offers a direct measurement of the hgg coupling, This is complementary to that at the LHC, where this coupling is obtained from the Higgs production cross section, and has much smaller theoretical uncertainties. These measurements are performed using the leading Higgs production process  $e^+e^- \rightarrow Zh$ . All the major Z decay channels  $Z \to l^+ l^-, Z \to \nu \overline{\nu}$  and  $Z \to q \overline{q}$  are used in the analyses; see details in Ref. [191].

We now discuss in more detail the analysis procedure for the  $Z \to q\bar{q}$  channel. The signal final states consist of four jets, common for  $h \to b\bar{b}/c\bar{c}/gg$ . In the pre-selection, all the particles in each event are first clustered into four jets using Durham algorithm. The four jets are paired into two di-jet pairs,  $j_1j_2$  and  $j_3j_4$ , as for respectively Z

where  $m_{j_1j_2}$   $(m_{j_3j_4})$  is the invariant mass of  $j_1j_2$   $(j_3j_4)$ , and  $\sigma_Z$  (= 4.7 GeV) and  $\sigma_h$  (= 4.4 GeV) are the widths of invariant mass spectra of Z and h respectively determined using MC truth information. A cut  $\chi^2 < 10$  is applied. In the final-selection, to suppress the leptonic or semi-leptonic background events, the number of charged particles in each jet is required to be > 4. To suppress the  $q\bar{q}$  background events, the jet clustering parameter  $Y_{4\rightarrow 3}$  is required to be consistent with 4-jet characteristic, that  $\log Y_{4\to 3} > -2.7$ . In addition two cuts are applied on the event thrust and thrust angle, that thrust < 0.9and  $|\cos \theta_{\rm thrust}| < 0.9$ . The remaining background events are dominated by  $q\bar{q}q\bar{q}$ , mainly from hadronic decays of WW and ZZ. A cut on the angle between  $j_3$  and  $j_4$  is applied,  $105^\circ < \theta_{j_3 j_4} < 160^\circ.$  A kinematic fitting is performed, using four-momentum conservation constraints plus the constraint  $m_{j_1j_2} - m_{j_3j_4} = M_Z - M_h$ . Then, two cuts are applied on the fitted Z and h masses, that  $m_{j_1j_2} \in [80, 100]$  GeV and  $m_{j_3j_4} - M_h \in [-15, 10]$  GeV. As a final cut, a multivariate likelihood is derived and required to be Likelihood > 0.375. After all the cuts, the signal efficiency is 26%, with an average S/B ratio of around 1/10, including all events of  $h \to b\bar{b}/c\bar{c}/gg$  (note the S/B ratio for  $h \to b\bar{b}$  events is much higher).

A template fit is then performed to extract the numbers of signal events  $h \to b\bar{b}$ ,  $h \to c\bar{c}$  and  $h \to gg$  respectively, for which it is crucial that the different signal events are distinguishable with themselves as well as with background events. The templates are constructed as 3-D histograms using 3 variables, namely b-likeness, c-likeness and bc-likeness defined for the two jets  $j_3$  and  $j_4$  (as from h candidate). Five templates are made using separated MC samples: signal  $h \to b\bar{b}$ ,  $h \to c\bar{c}$ ,  $h \to gg$ , SM background and  $h \to$  others background. The projected 2-D templates for b-likeness versus c-likeness are shown in Fig. 49, each of which has been normalised to an integrated luminosity of 250 fb<sup>-1</sup>. It demonstrates that the three types of signal events can indeed be clearly distinguished with themselves and with background events, thanks to the excellent flavor tagging performance and good signal over background ratio.

We just used  $Z \to q\bar{q}$  channel to illustrate the analysis, it is worth commenting that  $Z \to \nu\bar{\nu}$  channel is as powerful as  $Z \to q\bar{q}$  channel despite its branching ratio is a factor of 3 smaller. This is largely due to the factor that the signal and background discrimination in  $Z \to q\bar{q}$ channel is much degraded by performance of the realistic jet clustering and jet pairing algorithms at now, as a result of which the S/B ratio in  $Z \to q\bar{q}$  channel is a factor of 5 lower than that in  $Z \to \nu\bar{\nu}$  channel. From the perspective of a better jet clustering or jet pairing algorithm in future, the analysis in  $Z \to q\bar{q}$  channel can be significantly improved.

By combining  $Z \to q\bar{q}/\nu\bar{\nu}/l^+l^-$  channels, the estimates of statistical uncertainties for  $\sigma_{Zh} \cdot BR_{bb}, \sigma_{Zh} \cdot BR_{cc}$ and  $\sigma_{Zh} \cdot BR_{gg}$  are respectively 1.3%, 8.3% and 7.0%, shown in Table XI.

8.2.4. BR
$$(h \rightarrow WW^*/ZZ^*)$$

The measurements of branching ratios of  $h \rightarrow WW^*/ZZ^*$  play an important role in the global fit as the Higgs total width is determined by

$$\Gamma_h = \frac{\Gamma_{WW}}{BR_{WW}} = \frac{\Gamma_{ZZ}}{BR_{ZZ}}$$

Depending on how each W/Z decays and how Higgs is produced, there are quite many signal channels that can be used. The analysis strategies as well as the signal background discrimination also vary quite a lot channel by channel. For Zh production and  $h \to WW^*$ , the signal channels are listed in Table XIV, where the channels with marks are studied based on full simulation and enter the combined estimate of statistical uncertainty. The details of event selections can be found in [192–194]. One of the dominant background processes in all channels is  $e^+e^- \rightarrow W^+W^-$ , suppression of which can be helped by the right-handed beam polarisations. Due to the multiple jets in the signal final states, the analysis could also benefit significantly from an improved jet clustering algorithm in future. The estimate of statistical uncertainties for  $\sigma_{Zh} \cdot BR_{WW}$  is 4.6%, shown in Table XI. It's worth noting from Table XIV that there are still many more channels which yet to be employed in full simulation in future to improve the  $\sigma_{Zh} \cdot BR_{WW}$  measureTABLE XIV: Signal channels in  $e^+e^- \rightarrow Zh$ ,  $h \rightarrow WW^*$ and their branching ratios. The entries marked with \* or \*\* are currently studied by full simulation and enter the combined result. The entry marked with \*\* is based on CEPC studies.



FIG. 50: Higgs mass spectrum for the signal  $e^+e^- \rightarrow \nu \overline{\nu} h, h \rightarrow WW^* \rightarrow qqqq$  and the SM background events, normalized to 500 fb<sup>-1</sup> at 500 GeV [189].

ment, in particular the fully hadronic channel  $Z \to q\bar{q}$ and  $WW^* \to qqqq$  that has the largest branch ratio.

At  $\sqrt{s} = 500$  GeV, the  $BR(h \to WW^*)$  measurement can also be improved significantly by including Higgs production via W-fusion. Two signal channels  $e^+e^- \rightarrow \nu \overline{\nu} h$ ,  $h \to WW^* \to qqqq/qql\nu$  have been studied based on full simulation. As an illustration, the remained signal and background events in  $WW^* \rightarrow qqqq$  channel after all cuts are plotted in Fig. 50 in the reconstructed h mass spectra. The signal peak can be clearly observed with the dominant background from  $\nu \overline{\nu} h$  ( $h \rightarrow others$ ),  $\nu \overline{\nu} Z$  and  $W^+W^-$ . The average S/B ratio is around 1/1.6 in the  $M(h) \in (114, 142)$  GeV region. The estimate of statistical uncertainty for  $\sigma_{\nu\overline{\nu}h} \cdot BR_{WW}$  is 3.4% with 250 fb<sup>-1</sup> at  $\sqrt{s} = 500$  GeV, shown in Table XI. It is worth noting here the significant impact of overlay events. Figure 51 shows the reconstructed h mass spectra for signal events in cases of no overlay, with overlay but using inclusive Durham jet clustering algorithm, overlay removal using anti- $k_T$  algorithm, and overlay removal using a new MVA based algorithm; see details in [189]. It can be said that the performance of h mass reconstruction, in the realistic case even with an optimized overlay removal algorithm to date, is still far away from the perfect case of no overlay. Therefore the  $\sigma_{\nu \overline{\nu} h} \cdot BR_{WW}$  measurement will benefit a lot from a better overlay removal algorithm in future.

For  $BR(h \to ZZ^*)$  measurement, in general it is more challenging due to its small branching ratio. Though



FIG. 51: Higgs mass spectrum for the signal  $e^+e^- \rightarrow \nu \overline{\nu} h, h \rightarrow WW^* \rightarrow qqqq$  in different cases of overlay: no overlay (solid black) illustrating the performance of perfect overlay removal; without overlay and without applying any removal algorithm (dashed black); overlay removal with traditional exclusive jet clustering algorithm, anti- $k_T$  here (blue); overlay removal with a new method based on MVA, optimized for this particular signal channel (red). The histograms are normalized to 500 fb<sup>-1</sup> at  $\sqrt{s} = 500$  GeV [189].

the analysis can be done similarly by combining analyses optimized in many individual channels, a different strategy was used in [108]. All the signal events are selected against background with a single multivariate method using many variables as input. As a result, the estimate of statistical uncertainty for  $\sigma_{Zh} \cdot BR_{ZZ}$  is 18%, shown in Tab. XI.

8.2.5. BR(
$$h \rightarrow \tau^+ \tau^-$$
)

The measurement of  $BR_{\tau\tau}$  provides a very important probe of the Higgs couplings to third generation fermions. And it is going to be one of the most precise Higgs measurements at the ILC, thanks to the relatively large branching ratio and very clean signal and background separation. The full simulation is performed using the leading Higgs production process  $e^+e^- \rightarrow Zh$  and all the decay channels from  $Z \to q\bar{q}/\nu\bar{\nu}/l^+l^-$ ; see details in [195]. The  $\tau$  is reconstructed using TaFinder and the four momenta of missing neutrinos are calculated using collinear approximation. The remained signal and background events in  $Z \rightarrow q\bar{q}$  channel are shown in Fig. 52. The S/B ratio is higher than 2/1. The signal efficiency is 36% and the dominant background is from  $e^+e^- \rightarrow ZZ \rightarrow q\bar{q}\tau^+\tau^-$ . The estimate of statistical uncertainty for  $\sigma_{Zh} \cdot BR_{\tau\tau}$  is 3.2%, shown in Table XI.

## 8.2.6. $BR(h \rightarrow invisible/exotic)$

As introduced in 8.2.1, the recoil technique enables that Higgs events can be tagged without looking into the Higgs decay products. This feature is extremely use-



FIG. 52: MVA output for the signal  $e^+e^- \rightarrow q\bar{q}h, h \rightarrow \tau^+\tau^$ and the SM background at 250 GeV [195].



FIG. 53: Recoil mass spectrum against  $Z \to q\bar{q}$  for signal events  $e^+e^- \to Zh, h \to invisible$  assuming  $BR(h \to invisible) = 10\%$  and SM background events at 250 GeV for the right-handed beam polarisation [196].

ful for probing Higgs to invisible or other exotic decays. Full simulation studies are performed for  $e^+e^- \rightarrow Zh$ ,  $h \rightarrow$  invisible using two signal channels  $Z \rightarrow q\bar{q}$  and  $Z \to l^+ l^-$ ; see details in [196–198]. The dominant contribution comes from  $Z \to q\bar{q}$  channel. After all the cuts, the recoil mass spectrum for the remaining signal and background events is plotted in Fig. 53. The main background events come from  $ZZ/\nu\overline{\nu}Z \rightarrow \nu\overline{\nu}q\overline{q}$  and  $WW \rightarrow qql\nu$ . The signal peak would be seen clearly for the value  $BR(h \rightarrow \text{invisible}) = 10\%$  assumed in the figure. The actual sensitivity is much greater. We estimate the 95% C.L. upper limit for  $BR(h \rightarrow invisible)$  to be 0.86% for the left-handed beam polarisations, as shown in Tab. XI. An upper limit factor of 1.5 lower can be obtained for the right-handed beam polarisations, thanks to the much reduced background level.

Other exotic decays have not been studied based on full simulation. Nevertheless according to the fast simulation results in Ref. [128], at ILC250 we would be able to probe partially visible exotic decays with branching ratios of  $10^{-3}$  or below.

The measurement of the SM rare decay branching ratios BR( $h \rightarrow \mu^+ \mu^- / \gamma \gamma / \gamma Z$ ) are a bit challenging at the ILC, mainly due to the limited number of signal events. We expect significant contributions from HL-LHC for these measurements. Full simulations are performed in [199, 200], and the estimates of statistical uncertainties for  $\sigma_{Zh} \cdot BR_{\mu\mu}$  and  $\sigma_{Zh} \cdot BR_{\gamma\gamma}$  are respectively 72% and 34%, shown in Table XI.  $BR(h \rightarrow \gamma Z)$  is also studied based on full simulation [201], a significance of  $2\sigma$  would be expected with full ILC250.

## 8.2.8. Higgs CP properties

Higgs CP properties can be measured via the  $h\tau\tau$  coupling at the tree level,

$$\Delta \mathcal{L}_{h\tau\tau} = -\frac{\kappa_{\tau} y_{\tau}}{\sqrt{2}} h \tau^+ (\cos \Psi_{CP} + i \sin \Psi_{CP} \gamma_5) \tau^-, \quad (20)$$

where the CP phase angle  $\Psi_{CP}$  is determined using the transverse spin correlation between the two  $\tau$ , as shown in Fig. 54 (upper) in the  $\Delta \phi$  (angle between transverse spins of two  $\tau$ ) distribution for different values of  $\Psi_{CP}$ . The spin of each  $\tau$  is estimated using the polarimeter vector which can be fully reconstructed in some of  $\tau$  decay modes, such as  $\tau \to \pi \nu / \rho \nu$ , taking advantage of precise measurements for impact parameters; see the method detail in [202]. Full simulation studies are performed using signal channels  $Z \to q\bar{q}/l^+l^-$  and  $h \to \tau^+\tau^-$  in [203]. Figure 54 shows the distribution of reconstructed  $\Delta \phi$ for the remained signal and background events in one of the golden event categories. The estimate of statistical uncertainties for CP phase angle is  $4.3^{\circ}$  with full ILC250. Note that the Higgs CP violating effects can also be probed in hZZ coupling using the *b* parameter shown in next section.

# $8.2.9.\,$ Angular analyses for anomalous HVV couplings

The hZZ coupling can be deviated from SM not only in total strength but also in Lorentz structures, which can be detected by measuring differential cross sections. Full simulation studies are performed using  $e^+e^- \rightarrow Zh$ events for measuring following effective hZZ couplings:

$$\Delta \mathcal{L}_{hZZ} = (1+a)\frac{m_Z^2}{v}hZ_{\mu}Z^{\mu} + \frac{1}{2}\frac{b}{v}hZ_{\mu\nu}Z^{\mu\nu} + \frac{1}{2}\frac{\tilde{b}}{v}hZ_{\mu\nu}\tilde{Z}^{\mu\nu},$$
(21)

where the first *a*-term is a rescaling of SM hZZ coupling, the second *b*-term and the third  $\tilde{b}$ -term represent respectively anomalous CP-even and CP-odd hZZ couplings. The total cross section  $\sigma_{Zh}$  is sensitive to both *a* and *b* parameters, but *b* is distinguished from *a* in the differential cross sections; see Fig. 55 (upper) how *Z* production angle depends on values of *b*.  $\sigma_{Zh}$  depends on  $\tilde{b}$  rather weakly, only quadratically. But the angle between



FIG. 54: Upper:  $\Delta \phi$  distributions at MC Truth level for different values of  $\Psi_{CP}$  for the signal  $e^+e^- \rightarrow q\bar{q}h, h \rightarrow \tau^+\tau^-$  at 250 GeV; Lower: reconstructed  $\Delta \phi$  distributions after all cuts in the dominant category for the SM signal (in red) and the SM background (blue) respectively [203].

 $\Delta \phi$  [rad]

Zh production plane and Z decay plane, namely  $\Delta\Phi$ , is very sensitive to  $\tilde{b}$ ; see Fig. 55 (lower) for  $\Delta\Phi$  distributions for different values of  $\tilde{b}$ . The analysis details can be found in [204]. The estimate of statistical uncertainties for a and b are 0.076 and 0.027 respectively, with a large correlation  $\rho = -99.17\%$ , shown in Table XI. This large correlation can be significantly reduced by measurements at  $\sqrt{s} = 500$  GeV, as shown in Fig. 56, because the effect of b-term is momentum dependent. The CP violating parameter  $\tilde{b}$  can be determined with a statistical uncertainty of 0.004 for the full ILC250, with almost no correlation with a or b.

## 8.3. Systematic uncertainties, and the importance of beam polarisation

For the studies of the Higgs boson in which we wish to claim that precisely measured deviations from the SM can give a discovery of new physics, we must be certain that systematic errors are both small and wellconstrained. In this section, we will discuss the sources of systematic error that we consider in our Higgs coupling analysis.

We will also discuss the capability that the ILC gives to control systematic uncertainties using the availability



FIG. 55: Upper (lower):  $\cos \theta_Z \ (\Delta \Phi)$  distributions at MC Truth level for different values of anomalous coupling  $b \ (\tilde{b})$ for the signal  $e^+e^- \rightarrow \mu^+\mu^-h, h \rightarrow everthing$  at 250 GeV; [204].

of polarized beams. In precision measurement, it is useful, whereever possible, to measure effects correlated to sources of systematic uncertainty. For this, it is crucial to always have one more degree of freedom that (statistically) absolutely required. In the ILC program, electron and positron polarisation provide tools to validate estimates of systematic errors, and to reduce these sources of uncertainty. In Sec. 4.10, when we reviewed in general terms the importance of the use of beam polarisation to meet the physics goals of the ILC, we did not emphasize this aspect of the physics implication of polarisation. But it is clear that, for each measurement that can be done at an unpolarized collider, a collider with control of the polarization for each beam can provide four independent data sets. We will explain in this section how this tool can be used not only to estimate but also to reduce systematic errors.

# 8.3.1. Systematic uncertainties considered in the Higgs coupling fit

The evaluation of systematic uncertainties for experiments which have not yet been built is a difficult task and will to some extent always remain guess-work until real data have been taken. To some extent, we can rely on the experience from previous  $e^+e^-$  experiments, especially at LEP, where many uncertainties could be controlled to a typical level of 1%. The ILC detector designs, which aim for higher precision, make use of this experience, as explained in Sec. 6. Assuming this basic level of performance, detailed studies of systematic uncertainties at the ILC have concentrated on cases where the statistical uncertainties are expected to be significantly below 1%, and on searches in channels with large irreducible backgrounds. An example for the first case is a global analysis of total rates and differential distributions of various 2-fermion and 4-fermion SM processes, extracting simultaneously the total unpolarised cross sections, the relevant left-right asymmetries, the beam polarisations and the charged triple gauge couplings, see Sec. 9.1 and Ref. [109]. An illustrative example for the second category, though not directly connected to Higgs physics, is the WIMP search in the mono-photon channel, see Sec. 12.2 and Ref. [106].

Studies of this type lead us to the following estimates of the dominant systematic uncertainties. These sources of systematic uncertainty are also applied to the measurements of triple gauge boson couplings described in Sec. 9.1.

- The luminosity at the ILC will be measured from low-angle Bhabha scattering with the help of a dedicated forward calorimeters, the LumiCals (see Sec. 6.2.5 and Ref. [205]). This measurement is extremely sensitive to the exact alignment of the LumiCals on the two sides of the detector, as well as to beam backgrounds and has been studied in detailed simulations both for the ILC and for CLIC [206, 207]. Based on these studies, the resulting systematic uncertainty on all Higgs cross section and cross-section-times-braching-ratio measurements is assumed to be 0.1%
- Another 0.1% is assumed for the net systematic effect of the finite knowledge of luminosity-weighted long-term average values of the beam polarisations at the  $e^+e^-$  interaction point. Compton polarimeters in the Beam Delivery System will provide timestable measurements of the beam polarisations at their locations at the level of 0.25% [95, 208]. To obtain the polarisations relevant for the experiments, one must also consider also the effects of spin transport, misalignment of beam line magnets as well as depolarisation during the beambeam interaction [209]. The absolute scale of the luminosity-weighted average polarisation at the IP is finally calibrated from collision data, *e.g.*, from a



FIG. 56: 68% and 95% C.L. contour plots for fitted parameter a versus b at 250 GeV (left) and 500 GeV (right) [204].

global fit to SM processes with strong polarisation dependence [109].

- Theoretical uncertainties are also assumed to have reached the level of 0.1% by the time of ILC operation. This requires the computation of all relevant processes to 2 loops in the electroweak interactions, a task feasible within the current state of the art [210]. Another question is the availability of high-precision values for the most important input parameters— $m_b$ ,  $m_c$ ,  $\alpha_s$ , and  $m_h$ . We expect to obtain the first three of these to sufficient accuracy from lattice QCD [118]. For  $m_h$ , the ILC recoil measurement described in Sec. 8.2.1 will provide the high precision needed.
- For flavor tagging, systematic errors of 1% have already been reached at LEP. With the advances in detector technology and the larger integrated luminosity, we assume that for each data set at the ILC this can be reduced and also improved as a function of integrated luminosity by probe-andtag measurements. We expect an uncertainty of  $0.3\%\sqrt{0.250/L}$ , where L is the integrated luminosity in iab. This is an error of 0.1% for the ILC250.

# 8.3.2. Control of systematic uncertainties using beam polarisation

In the remainder of this section we will highlight the impact of the beam polarisation on the control of systematic uncertainties using these two studies as examples. We have already pointed out that beam polarisation provides subsets of the data that can be used as cross-checks of systematic errors on efficiencies for signal identification and background suppression. However, the studies in Refs. [106] and [109] go beyond this to illustrate the use of beam polarisation to actually reduce systematic errors beyond what is possible at an unpolarised collider. Both of these studies were carried out for measurements at the 500 GeV ILC, but the same principles apply to the 250 GeV data.

Several principles combine to produce this result. The first is that different polarization settings produce event samples with different mixtures of signal and background processes. The differences in these mixtures arise from order-1 polarization asymmetries that vary from process to process, to first approximation, in the manner predicted by the SM. In the SM, for example, lepton pair production has a small polarization asymmetry while the polarization asymmetry for  $b\bar{b}$  production is large and that for W pair production is almost maximal. For certain modes, for example, lepton pair production and dijet production, the detection efficiency is naturally very high and therefore has a small uncertainty, while for other processes, for example, bb production, this efficiency is smaller and also more complicated to estimate. If we introduce nuisance factors for the more uncertain efficiencies and determine these from data, the correlation of the relative compositions with polarization allows us to determine these parameters in terms of the efficiencies that are better known.

The second principle is that systematic uncertainties that are correlated with polarization can be cancelled locally in the data set using fast reversal of the beam helicities. This principle was essential to the excellent measurement of  $\sin^2 \theta_w$  by the SLD experiment from a very small data sets; almost all systematic errors were cancelled by flipping the  $e^-$  beam polarization in a pseudorandom fashion [211]. The principle of rapid helicity reversal is built into the ILC design, which gives the capability to flip the sign of polarisation for each of the two beams independently on a train-by-train basis (see



FIG. 57: Uncertainties on the unpolarised cross sections of various 2-fermion and 4-fermion processes as obtained from

the global fit introduced in the text [109], assuming a systematic uncertainty of 1% on the selection efficiencies and purities, each. In the case of polarised beams, it is estimated that only 10% of the uncertainty is uncorrelated between data sets. Applying that estimate to the analysis of data sets

taken "quasi-concurrently", the impact of the systematic uncertainties is minimal. Without the redundancies provided

by data sets with correlated systematic uncertainties, the total uncertainties increase by a factor 2 for WW and single-W processes and a factor of 5 for 2-fermion processes.

Sec. 2.3.1. This helicity reversal is fast compared to typical time-scales of changes in the configuration, calibration, and alignment of the detector and the accelerator. It implies that data sets with the same beam energy but different beam helicities can be considered as being collected essentially concurrently.

The improvement in the measurement of the absolute normalization of cross sections can be very significant. The study of Ref. [109] considered the full set of 2-fermion production processes and 4-fermion production processes (including  $e^+e^- \rightarrow WW/ZZ \rightarrow 4$  fermions and well as single-W production) at 250 GeV. Each channel was assigned a 1% systematic uncertainty in its selection efficiency and signal purity. Based on the correlations of experimental effects between "quasi-concurrently" taken data sets, discussed in section 8.3.2, it was estimated that only 10% of this uncertainty is uncorrelated between data sets with different beam polarisation configurations. Thus, a global fit using all four polarization settings allows one to determine the relative efficiencies and remove most of the systematic uncertainty. The result for the final normalization uncertainties are shown in Fig. 57. For each of several 2- and 4-fermion channels, the black bars show the statistical uncertainties, the red bars show the full uncertainties for unpolarised data, and the blue bars show the uncertainties for polarised data samples. The final uncertainties are larger in unpolarized case by a factor of 2 for WW and single-W processes and by a factor of 5 for lepton pair production.

The same principles can be applied to the measurement of polarisation asymmetries  $A_{LR}$ , which, as we have



FIG. 58: Uncertainties  $\Delta\beta$  on  $A_{\rm LR}$  of various 2-fermion and 4-fermion processes as obtained from the global fit introduced in the text [109] with both beams polarised (with the standard 45%/45%/5%/5% sharing between the four helicity configurations) and in the absence of positron polarisation (with a 50%/50% sharing between the two remaining helicity configurations). In the absence of positron polarisation, the uncertainties on  $A_{\rm LR}$  increase by a factor 2 for WW and by about a factor of 10 for 2-fermion processes. Alone the single-W processes remain unaffected.

seen, play a large role in the ILC program. Though many systematic errors automatically cancel in  $A_{LR}$ , there are new sources of systematic uncertainty, for example, the possibility of a correlation between the helicity orientation and the luminosity delivered per bunch train. This is effectively controlled if both the electron and positron bunches can be polarised. Roughly, the polarization asymmetry in W pair production is almost maximal, and the small uncertainty in this quantity can be transferred to the value of  $A_{LR}$  for other processes. The point is illustrated in Fig. 58, again from Ref. [109], which shows a comparison of the final uncertainty on  $A_{LR}$  in a global fit between a collider with  $e^-$  and  $e^+$  polarization (black bars) and a collider with only  $e^-$  polarization (red bars). The improvement is a factor of 10 for fermion pair production. (In this illustrative study, the systematic errors from detector efficiency and theory are set equal to zero.)

Similar large effects from polarisation are seen in cases in which the signal is detected in the shape of a distribution. An illustration here is given by a study of the search for dark matter particles  $\chi$  using the monophoton signature [106], already discussed in Sec. 4.10. In our earlier discussion, we pointed out that the signal from  $e^+e^- \rightarrow \gamma\chi\chi$  sits on top of a large irreducible background from  $e^+e^- \rightarrow \gamma\nu\bar{\nu}$ . The study includes a careful evaluation of the systematic uncertainties, including those on selection efficiencies, luminosity, beam energy (spectrum) and polarization as well as on the theoretical modelling of the background. The limit calculation uses fractional event counting based on the observed energy spectrum of the selected photon candidates and considers normalisation and shape-dependent uncertainties as well as the



FIG. 59: Comparison of the reach of the search for WIMP production in the mono-photon channel for different assumptions on luminosity and polarization, *including* systematic uncertainties (see Sec. 12 for a description of the analysis) [106].

correlations between these. If the mass of the  $\chi$  is relatively high, only low-energy photons can appear in the signal process. Then the high-energy part of the photon spectrum can be used to determine nuisance parameters assigned to the polarization and efficiencies. The results for the lower limit on the mediator scale, including systematic errors, are shown in Fig. 59. This figure should be compared to Fig. 25, in which systematic errors are set to zero. Note that, in this case, the strongest limits are set using a mixture of beam polarizations (the dashed red curve in both cases) since this allows the systematic errors from beam polarisation to be better controlled.

## 8.4. Estimation of future improvements

As elaborated in the previous section, all the estimates for Higgs measurements shown in Tab. XI are based on available full simulation studies, which are performed using the analysis techniques known at present. These estimates are clearly too conservative in the sense that we have not been able to analyse all useful signal channels. In addition, analysts working closely with the data are always able to invent algorithms to that are more cleverly optimized to the data that is actually collected. The projected uncertainties quoted here and in Sec. 11.1 do not take advantage of these likely improvements.

Since the formal estimates of the performance of HL-LHC given in the HL-LHC Yellow Report [126] do take into account improvements in systematic uncertainties that are anticipated but not yet realised, it seems to us reasonable to define also for ILC an optimistic scenario with improved performance. We use this scenario to compare to the results of Ref. [126] in the manner explained in Sec. 11.3. This scenario, which we refer to as "S2" in that discussion, includes the following improvements in the analysis just described. In all cases, these improvements are under study using our full simulation tools and are suggested, if not yet validated, by our current results:

- 10% improvement in signal efficiency of the jet clustering algorithm.
- 20% improvement in the performance of the flavor tagging algorithm.
- 20% improvement in statistics by including more signal channels in  $\sigma_{Zh} \cdot BR(h \to WW^*)$ .
- a factor of 10 improvement in the precision electroweak input  $A_{\ell}$  thorugh the measurment of  $e^+e^- \rightarrow \gamma Z$  with polarized beams at 250 GeV.
- 30% improvement in the precision of Higgs selfcoupling and top-Yukawa coupling at 500 GeV, which is a consequence of the improvements in jet clustering algorithm, flavor tagging algorithms and statistics by including more signal channels.

## 8.5. Measurement of the Higgs boson selfcoupling

The trilinear Higgs coupling can be measured at colliders in two different ways. First, the coupling can be measured directly, using processes with Higgs pair production that diagrams involve the triple Higgs coupling at the tree level. Second, the coupling can be measured indirectly, since radiative corrections to single-Higgs processes can include effects due to the tripple Higgs coupling.

The important Higgs pair production reactions at  $e^+e^-$  colliders are  $e^+e^- \rightarrow ZHH$  and  $e^+e^- \rightarrow \nu\overline{\nu}HH$ , shown in Fig. 60. Note in both reactions there are diagrams that do not involve trilinear Higgs coupling. The first of these processes can be studied already at 500 GeV; the second, which is a 4-body process, requires somewhat higher energy. The cross sections of these two processes as a function of  $\sqrt{s}$  are shown in Fig. 61. Full simulation studies at a  $\sqrt{s} = 500$  GeV show that a discovery of the double Higgs-strahlung process is possible within the H20 program, using  $Z \to l^+ l^- / \nu \overline{\nu} / q \overline{q}$  and  $hh \to b \overline{b} b \overline{b} / b \overline{b} W W^*$  channels. With 4 ab<sup>-1</sup> at 500 GeV, a combination of those decay channels would yield a precision of 16.8%on the total cross section for  $e^+e^- \rightarrow ZHH$  [212–214]. Assuming the SM with only the trilinear Higgs coupling free, this corresponds to an uncertainty of 27% on that coupling.

At still higher energy vector boson fusion becomes the dominant production channel. Making use of this channel, with 8  $ab^{-1}$  at 1 TeV, the studies of Refs. [213–215] show that, in the same context of varying the trilinear Higgs coupling only, this coupling can be determined to 10%.

The impact of the center-of-mass energies on the trilinear Higgs coupling measurement is studied by extrapolating the full simulation results done at 500 GeV and 1 TeV to other energies. Due to the existence of diagrams that do not involve the trilinear Higgs coupling in



FIG. 60: Diagrams contributing to (a)  $e^+e^- \rightarrow Zhh$  and (b)  $e^+e^- \rightarrow \nu \overline{\nu}hh$ .



FIG. 61: Cross sections for the double Higgs production processes,  $e^+e^- \rightarrow Zhh$  and  $e^+e^- \rightarrow \nu\overline{\nu}hh$ , as a function of  $\sqrt{s}$  for  $m_h = 125 \text{ GeV}.$ 

both reactions, to get the correct extrapolation a careful analysis taking into account the dependence on  $\sqrt{s}$  for both the total cross sections and interference contributions was performed in Ref. [216]. The results are shown in Fig. 62 as the blue lines for the two reactions. In addition to the results from realistic full simulations, the expectations for the ideal case, assuming no background and 100% signal efficiency, are shown as the red lines in the figure. The differences between the blue and the read lines, is as large as a factor of 4-5. This suggests that there is much room for improvement in the clustering algorithm used to identify 2-jet systems with the Higgs boson mass, which lead to improvements in the final results. Improvements could also come from better flavor-tagging algorithms and inclusion of additional signal channels such as  $Z \to \tau^+ \tau^-$ . The figure does imply that  $\sqrt{s} = 500-600$  GeV is optimal for  $e^+e^- \rightarrow Zhh$  but that CM energies of 1 TeV or above would be needed for  $e^+e^- \rightarrow \nu \overline{\nu} hh.$ 

Since large deviations of the trilinear Higgs coupling are expected in some new physics models, in particular in models of electroweak baryogenesis, it is interesting to see how the expected precisions would change in that case. Figure 63(left) gives the cross sections of the two reactions as a function of the actual triple Higgs coupling  $\lambda$ , and Figure 63(right) shows the expected precisions of the ILC measurements. The natures of interference between the triple Higgs coupling and the SM production amplitude is very different for the two reactions, constructive for  $e^+e^- \rightarrow Zhh$  but destructive for  $e^+e^- \rightarrow \nu \overline{\nu}hh$ . Therefore, the two reactions, useful at 500 GeV and 1 TeV respectively, are complementary in determining the trilinear Higgs coupling. If the trilinear Higgs coupling is indeed a factor of 2 larger, as expected in some models, the double Higgsstrahlung process at 500 GeV becomes very useful and would already provide a measurement of around 15% precision for the trilinear Higgs coupling.

The indirect determination of the trilinear Higgs coupling is based on the observation of McCullough [217] that the cross section for  $e^+e^- \rightarrow ZH$  contains a radiative correction involving the trilinear coupling that lower the cross section by about 1.5% from 250 GeV to 500 GeV, with most of the decrease taking place below 350 GeV. Taken a face value in the simple context with only the trilinear coupling free, the ILC cross section measurements would determine the trilinear coupling to about 40%.

It is important to note, however, that the determination of the trilinear coupling involves two separate questions. First, is the SM violated? The accuracies with which this question can be answered are those given above. Second, can the violation of the SM be attributed to a change in the trilinear coupling or the Higgs potential rather than being due to other possible new physics effects? A precise way to ask this question is: Can the shift of the trilinear coupling be measured independently



FIG. 62: The expected precisions of  $\lambda$  as a function of  $\sqrt{s}$  for  $e^+e^- \rightarrow Zhh$  (left) and for  $e^+e^- \rightarrow \nu\overline{\nu}hh$  (right). The two lines in each plot correspond to ideal situation (red) and realistic situation (blue) as described in the text. Same integrated luminosities of 4 ab<sup>-1</sup> is assumed at all  $\sqrt{s}$ .



FIG. 63: Left: the cross section as a function of  $\lambda$  for  $e^+e^- \rightarrow Zhh$  (red line) and for  $e^+e^- \rightarrow \nu\bar{\nu}hh$  (blue line), where values of both  $\lambda$  and  $\sigma$  are scaled to their SM values. Right: expected precisions of  $\lambda$  when  $\lambda$  is deviated from its SM value.

of possible effects of all other dimension-6 EFT operators? To our knowledge, this latter question has only been addressed for determinations of the trilinear coupling at lepton colliders. In Ref. [218] it is shown that, after the ILC H20 program of single-Higgs measurements is complete, the uncertainty in the measurement of the total cross section for  $e^+e^- \rightarrow ZHH$  receives a negligible 2.5% uncertainty due to variation of the other relevant dimension-6 EFT perturbations. In Ref. [219], it is shown that, when the cross section for  $e^+e^- \rightarrow ZH$  is fit together with other relevant observables at 250 GeV and 500 GeV, the uncertainty in the coupling is not substantially changed from the value of 40%. This conclusion, however, might be sensitive to the precision of the inputs from precision electroweak observables. A study of those effects is in progress.

## 9. PHYSICS SIMULATIONS: ELEC-TROWEAK PRODUCTION OF 2- AND 4-FERMION FINAL STATES

The precision studies of the Higgs boson described in the previous section receive important and complementary support from analyses of 2- and 4-fermion final states which do not directly involve Higgs bosons, but our wellknown SM gauge bosons — or potentially their yet to be discovered siblings. In this section, some of the key examples introduced in Sec. 4.7 will be discussed in more detail, highlighting the level of realism on which the projections are based.

## 9.1. Analyses of $e^+e^- \rightarrow W^+W^-$

The analysis of four-fermion processes, e.g. from Wpair production, but also Z-boson pairs and single-boson processes, plays a key role in the ILC physics program. As discussed in Sec. 4.7, constraints on triple gauge couplings (TGCs) are an important input to the dim-6 EFTbased interpretation of Higgs precision measurements introduced in Sec. 4.6. Prospects for this type of analysis have been intensely studied in full detector simulation (c.f. Sec. 7), however only at center-of-mass energies of at least 500 GeV. In this section, we will start out by summarizing these detailed studies, and then proceed to their recent extrapolations to a center-of-mass energy of 250 GeV.

## 9.1.1. Full simulation analyses of TGCs

The prospects for probing charged TGCs at the ILC have been studied in full, GEANT4-based simulation of the ILD detector concept at  $\sqrt{s} = 500 \,\text{GeV}$  [220] in the context of the ILD Letter of Intent [155] and at  $\sqrt{s} = 1 \text{ TeV}$  [221] as a benchmark for the ILD Detailed Baseline Design (Vol 4 ILC TDR [5]). Both analyses focused on the channel  $e^+e^- \rightarrow W^+W^- \rightarrow qql\nu$ ,  $l = e, \mu$  and followed a similar, cut-based selection approach. Thereby they exploit the known initial state for a full kinematic reconstruction of both W bosons, under consideration of optional photon radiation collinear to the beam direction. Neither the case  $l = \tau$ , nor the fully hadronic mode, nor contributions from single-W production were included at the time. Especially the fully hadronic mode will profit substantially from the recent advances in reconstructing the jet charge with the ILD detector, c.f. Sec. 9.2, in order to determine the charges of the W boson candidates.

Figure 64 shows one of the final observables sensitive to anomalous TGCs, namely the cosine of the polar angle of the  $W^-$  boson,  $\cos \theta_W$ , which is reconstructed from the hadronically decaying W boson. The left part of the figure illustrates the high purity of the selection which ranges between 85% and 95%, depending on whether  $WW \rightarrow qq\tau\nu$  is considered as background or not. The right panel shows relative deviation of the reconstructed  $\cos \theta_W$  from MC truth, indicating a resolution of better than 0.5%.

In the 500 GeV analysis, no pile-up from  $\gamma \gamma \rightarrow \log p_t$ hadrons was considered, which has, at  $\sqrt{s} =500$  GeV, an expectation value of 1.2 events per bunch crossing, c.f. Sec. 7. This type of background was considered, however, in the TGC study at 1 TeV, where its expectation value increases to 4.1 pile-up events per bunch crossing. Figure 65 shows the impact of these pile-up events on the reconstructed hadronic W-boson mass without ("Durham") and with ("Kt") application of suitable suppression algorithms (see Sec 8.1 for a detailed description of the algorithm). It can be seen that the residual effect is small even at 1 TeV, where the number of pile-up events is expected to be nearly four times higher than at 500 GeV.

Both full-simulation studies used only three out of five possible angular distributions which could provide sensitivity to TGCs: besides the production angle of the  $W^-$ , the two angles describing the direction of the decay lepton in the restframe of its mother W were considered in a five-parameter fit based on MC templates. The free parameters of the fit were the three TGCs  $g_1^Z$ ,  $\kappa_{\gamma}$ and  $\lambda_{\gamma}$  as well as the absolute values of the electron and positron beam polarisations. With this approach, statistical uncertainties of about  $6 \cdot 7 \cdot 10^{-4}$  were obtained for all three couplings for an integrated luminosity of 500 fb<sup>-1</sup> at  $\sqrt{s} = 500$  GeV, shared equally between all four beam polarisation configurations. In the context of the 500 GeV analysis a thorough evaluation of the systematic errors was performed. It was found at the time that uncertainties on the selection efficiencies of signal and background of 0.2% and 1%, respectively, would lead to systematic effects in the same order of magnitude as the statistical uncertainty for 500 fb<sup>-1</sup>.

A recent study dedicated to a global fit of total and differential cross sections of various SM processes sensitive to TGCs and/or beam polarisation has shown, however, that a much better control of systematic effects can be achieved — provided that *both* beams are polarised [109, 110].

The full simulation study at  $\sqrt{s} = 1$  TeV, following the same fitting approach, found statistical uncertainties of about  $2 \cdot 3 \cdot 10^{-4}$  for all three TGCs for an integrated luminosity of 1000 fb<sup>-1</sup>. The effect of different sharings of the luminosity between the four polarisation sign combinations on the TGC precisions were found to be minor.

## 9.1.2. Extrapolation of TGC prospects to 250 GeV

While extensive studies of WW production exist at higher center-of-mass energies, no complete analysis based on full detector simulation is available yet for  $\sqrt{s} = 250 \text{ GeV}$ . Nevertheless substantial progress has been made in various important aspects which have been incorporated in an extrapolation [4] based on a) the previously discussed full-simulation studies at 500 GeV [220] and 1 TeV [221] and b) the actual LEP results at ~ 200 GeV [222]:

- As discussed in Sec. 4.7, the sensitivity of measured cross sections to the TGCs depends on the center-of-mass energy as  $s/m_W^2$ .
- Naively, the statistical uncertainties on measured cross sections scale as  $1/\sqrt{\sigma \mathcal{L}}$ . However at higher center-of-mass energies, the W bosons are more and more boosted into the forward direction due to increasing amount of ISR and beamstrahlung. Therefore the experimental acceptance decreases for higher  $\sqrt{s}$ . A correction factor for this effect has been derived [223] from a comparison of the full detector simulation studies at 500 GeV and 1 TeV.
- The dependence on the sharing of luminosity between the four different polarisation configurations was found minor [221] and therefore no corrections for differences in the assumptions of the full simuation studies w.r.t. the H20 running scenario (c.f. Sec. 3.2) were applied.



FIG. 64: Left: Reconstructed polar angle distribution  $\cos \theta_W$  of the  $W^-$  boson candidates for signal and SM background events before the application of the final selection cut  $\cos \theta_W > -0.95$ . Right: relative deviation of the reconstructed  $\cos \theta_W$ from the MC truth value  $\cos \theta_W^T$ . Both from [220].



FIG. 65: Reconstructed mass of the hadronically decaying W boson at  $\sqrt{s} = 1$  TeV without pile-up compared to the situation with pile-up in absence ("Durham") or presence ("Kt") of a mitigation strategy in the analysis. From [221].

- The improved treatment of systematic uncertainties based on a nuisance parameter technique in a global fit to many observables and datasets explored in [109] was assumed, which leads to a constant ratio between systematic and statistical uncertainties up to luminosities of at least 2 ab<sup>-1</sup>.
- The full simulation studies were found to be limited their MC-based, binned fit of 3D-template histograms. The relative improvement expected when including the fully hadronic channel and when exploiting all five sensitive angles (production angle of one of the W bosons plus decay angles of both W bosons, see e.g. Fig. 5.16 in [220] for an ilustration) in an unbinned fit [224], or, equivalently, when applying an optimal observable technique [225, 226], was estimated in a parton-level study to be a factor 2.4 in the case of  $g_1^Z$ , and a factor of 1.9 for the

other two couplings.

• Since none of the ILC full-simulation studies evaluated the precisions for single-coupling fits, i.e. when fixing the other two anomalous couplings to 0 as done in hadron collider studies, the corresponding LEP2 results [222] were extrapolated up in center-of-mass energy, and then the minimum of this extrapolation and of the 3-coupling extrapolation from ILC studies was taken.

The results of this procedure are displayed in Tab. XV and Figs 66 and 67 in comparison with the LEP2 and LHC results as well as HL-LHC projections, where applicable. In case of the single-parameter fits, the 250 GeV stage of the ILC will improve the precision on  $g_1^{\mathbb{Z}}$  and  $\kappa_{\gamma}$  by factors of 5 and 30 w.r.t to HL-LHC, while the projections for  $\lambda_{\gamma}$  are comparable. The loss in precision when fitting all three couplings simultaneously to ILC data is minor, and the resulting precisions are used as input for the EFT-based Higgs coupling fit discussed in Sec. 11.1. Actually, it has been shown it is possible even to determine simultaneously the 14 complex couplings in the most general parametrisation of triple gauge boson vertices, including e.g. CP violating contributions, at  $e^+e^-$  linear colliders when both beams are polarised and all polarisation configurations, including transverse polarisation, are exploited [226].

## 9.1.3. W mass measurement at 250 GeV

The analysis of  $W^+W^- \rightarrow qql\nu$  discussed in the previous sections, as well as the study of single-W events also offer an excellent setting for the measurement of the W mass. As discussed in Sec. 4.8, the available statistics at the 250 GeV ILC will be about a factor of 2000 larger than at LEP2, which makes it obvious that a pure consideration of statistical uncertainties is meaningless. While

		total error $(\times 10^{-4})$			correlation		
Exp	$N_{par}$	$g_1^Z$	$\kappa_{\gamma}$	$\lambda_{\gamma}$	$g_1^Z \kappa_\gamma$	$g_1^Z \ \lambda_\gamma$	$\kappa_{\gamma} \lambda_{\gamma}$
LEP 2	3	516	618	376	-0.17	-0.62	-0.15
ILC 250	3	4.4	5.7	4.2	0.63	0.48	0.35
LEP 2	1	300	626	292	_	_	_
LHC	1	319	1077	198	—	_	_
HL-LHC	1	19	160	4	—	-	-
ILC 250	1	3.7	5.7	3.7	-	-	-

TABLE XV: TGC precisions for LEP 2, Run1 at LHC, HL-LHC and the ILC at  $\sqrt{s} = 250$  GeV with 2000 fb<sup>-1</sup>

luminosity (ILC 250). The LEP 2 result is from ALEPH [222] at  $\sqrt{s} \approx 200$  GeV with 0.68 fb<sup>-1</sup>. The LHC result is from ATLAS[227] at  $\sqrt{s} = 7$  TeV with 4.6 fb<sup>-1</sup>. The HL-LHC estimate is from a 2013 overview of HL-LHC physics [228]. From [4].



FIG. 66: Comparison of the reachable TGC precision from single parameter fits: ILC [229], final results from LEP combined from ALEPH, L3 and OPAL results [230] and the LHC TGC limits for  $\sqrt{s} = 8$  TeV data and an integrated

luminosity of  $\mathcal{L} = 20.3 \text{ fb}^{-1}$  and  $\mathcal{L} = 19.4 \text{ fb}^{-1}$  for ATLAS and CMS, respectively [231].



FIG. 67: Comparison of the reachable TGC precision from a simultaneous fit of all three parameters: ILC [229] and final results from LEP combined from ALEPH, L3 and OPAL results [230]. No comparable hadron collider results are available.

the studies discussed in Sec. 9.1.1 showed that this kind of events can be selected with high efficiency and purity, a careful extrapolation of the systematic uncertainties of previous measurements is therefore much more instructive than the evaluation of the statistical uncertainty from full detector simulation. Apart from a scan of the production threshold, kinematic reconstruction of Wpair events and calorimetric comparison of hadronic Wand Z decays in single-boson events are the most promising techniques, which are described in detail in [232, 233]. With a combination of methods and considering advances in theory as well as in the performance of the detectors the systematic limit has been estimated as  $2.4\,{\rm MeV}.$  This is expected to be reached already at the 250 GeV stage of the ILC. Additional datasets at higher center-of-mass energies could then provide independent information in order to cross-check and constrain systematic effects.

## 9.2. Analyses of $e^+e^- \rightarrow f\overline{f}$

Another important class of processes at  $e^+e^-$  colliders is fermion-antifermion production, which is highly sensitive to various new physics models, as discussed in Sec. 4.8. Thereby, the important observables are the polarised total cross sections, in particular in form of the left-right asymmetry  $A_{\rm LR}$ , as well as the differential cross section as a function of the polar angle,  $d\sigma/d\cos\theta$ , which contains even more information than the forward-backward asymmetry  $A_{\rm FB}$ .

## 9.2.1. General experimental aspects

At center-of-mass energies above the Z pole, di-fermion production will be accompanied frequently by a significant amounts of ISR. For example, at  $\sqrt{s} = 250 \text{ GeV}$ , about half of the di-fermion events return to the Z pole. The ISR photons may escape undetected through the beam pipe, or they can be produced at a sufficiently large angle to be measured in the detector. The forward acceptance of the ILC detectors is assisted by dedicated forward calorimeters described in Sec. 6.2.5.

In the latter case, energy and momentum constraints can be employed to reconstruct the full event kinematics from the angles of the fermions and the photon, without relying on their calorimetrically measured energies or momenta. This technique offers an excellent opportunity to cross calibrate the energy scales of various subsystems, e.g., to calibrate the photon energy scale against the momentum scale of the tracking systems in  $e^+e^- \rightarrow \mu^+\mu^-\gamma$ events. While in principle also the beam energy spectrum can be obtained from this method, it suffers from large event-by-event statistical fluctuations due to the relatively large width of the Z resonance [234].

But also in the case that there is no photon detected, the amount of collinear beamstrahlung or ISR energy can be reconstructed from kinematic constraints on an eventby-event basis. In this case, however, the measured momenta of the fermions have to be used. The previously mentioned case of  $e^+e^- \rightarrow \mu^+\mu^-\gamma$ , then provides an excellent method for an in-situ determination of the beam energy spectrum, since the muon momentum scale can be calibrated to 10 ppm from  $J/\psi \rightarrow \mu^+\mu^-$  decays [234].

In presence of beam polarisation, another important observable becomes accessible, namely the left-right asymmetry of 2-fermion processes:

$$A_{\rm LR} = \frac{\sigma_{\rm LR} - \sigma_{\rm RL}}{\sigma_{\rm LR} + \sigma_{\rm RL}} \tag{22}$$

The parameters  $\sigma_{\text{LR}}$ , etc., are the chiral cross sections for fully polarised beams, defined in Sec. 4.10. Their relation to the cross section for partial polarisation is described in that section. Here, we will focus on the measurement of the polarised cross sections and of angular distributions for the various 2-fermion processes.

## 9.2.2. Inclusive $e^+e^- \to f\overline{f}$ analyses

Di-fermion production at a center-of-mass energy of 250 GeV has recently been studied both by ILD and SiD, albeit with complementary goals. ILD has performed a study of all di-lepton channels in full detector simulation, including all leptonic 2-fermion and 4fermion backgrounds and focussing on events with  $\sqrt{s'}$ 230 GeV [236, 237]. After a simple cut-based event selection, purities of 97-99% can be obtained, while retaining a signal of 26 million events in the  $e^+e^-$  case and of about 0.75 million events in the  $\mu^+\mu^-$  case and 0.6 million events in the  $\tau^+\tau^-$  case. The polar angle distributions of the selected events are then compared to the predictions of various BSM models, which fall into two classes: tree-level exchange of additional, E6-insprired Z' bosons and loop-effects from dark matter candidates on the  $\gamma/Z$  propagator. In the case of the Z' models, the reach for a  $3\sigma$  observation ranges between 1.6 and 4.8 TeV, depending on the exact model, while it is between 165 and  $460 \,\mathrm{GeV}$  in case of the dark matter models, again depending on the exact type of model. These numbers so far combine only the electron and muon channels, therefore further improvement is expected once the  $\tau$ -channel has been included in the combination.

SiD on the other hand has performed a study focussing on the measurement of  $A_{LR}$  from radiative returns to the Z pole. They studied inclusively all di-lepton and di-jet channels in fast detector simulation [238]. Thereby they make use of the method mentioned above in order to obtain the boost between the Z rest frame and the lab frame from the angles of the two leptons or jets. After a simple cut-based event selection, about 4.5 million hadronic Z events and about 0.5 million leptonic Z events remain over a background of 1.2 million events for  $250 \text{ fb}^{-1}$  with  $P(e^{-}, e^{+}) = (-80\%, +30\%)$ . Exploiting the modified Blondel scheme [239, 240] in order to extract  $A_{\rm LR}$  directly from the polarised cross sections measured in the four different beam helicity configuraions, the estimated uncertainty on  $A_{\rm LR}$  for the full 2 ab<sup>-1</sup> is  $\Delta A_{\rm LR} = 0.00039$ . This number is strictly speaking a statistical uncertainty

only. However, due to the redundancy offered by the presence of positron polarisation in combination with the "quasi-concurrent" collection of the four data sets with different beam helicity configurations, the impact of systematic uncertainties is expected to be very small, especially if  $A_{\rm LR}$  is extracted from a global fit to several physics processes, which is, in contrast to the modified Bondel scheme, fully robust against unequal absolute polarisation values when flipping the sign of the polarisation. For more details on the discussion of the impact of polarisation on the control of systematic uncertainties see Sec. 8.3.

9.2.3. 
$$e^+e^- \to \tau^+\tau^-$$

In the special case of  $e^+e^- \rightarrow \tau^+\tau^-$ , the decays of the  $\tau$  lepton can be used to determine their polarisation, which adds extra information about the  $Z\tau\tau$  vertex. For the polarisation measurement, the individual  $\tau$  decay modes have to be identified and treated separately. It has been shown in full simulation of the ILD detector at  $\sqrt{s} = 500 \,\text{GeV} \,[5, 241]$  that the leptonic decay modes can be identified with efficiencies and purities of about 99%. For the  $\pi$  and  $\rho$  decay modes as well as for the threeprong  $\tau \to a_1 \nu_{\tau}$  decay, the same study reached purities of 90% at efficiencies between 96% and 91%, while for the one-prong  $\tau \to a_1 \nu_{\tau}$  decay efficiencies and purities of about 70% were achieved. In a more recent study [242], covering only the separation of the hadronic decay modes, efficiencies and purities of about 90% were demonstrated also for the three-prong decay.

After a polarisation analysis of the leptonic channels and the  $\pi$  and  $\rho$  channels via an optimal observable technique, the polarisation of the  $\tau$  leptons can be measured with a relative uncertainty of about 1% already with an integrated luminosity of 500 fb<sup>-1</sup>.

9.2.4. 
$$e^+e^- \rightarrow b\bar{b}$$

The couplings of the *b*-quark are of particular interest because as a lighter sister of the top-quark, it could be partially composite in extensions of the SM. Also, a rather large discrepancy in the  $\sin^2 \theta_{eff}$  values extracted from the measurement of the foward-backward asymmetry of  $b\bar{b}$  production at LEP and the  $A_{\rm LR}$  measurement at SLD still persists today and could be easily confirmed or rejected by remeasuring  $b\bar{b}$  production at the ILC 250. The prospects for this measurement have recently been evaluated in full, GEANT4-based simulation of the ILD detector [235, 243].

Thereby the special difficulty is to distinguish the *b*quark from the  $\bar{b}$ -quark. This can either be achieved by reconstructing the charge sum of the tracks from the  $b/\bar{b}$ decay vertices, which requires highest efficiency and precision for the reconstruction of tracks, also at small momenta and in the forward region — or via the charge of Kaons identified via their specific energy loss in the Time Projection Chamber of ILD, see Sec. 6.3.1.



FIG. 68: Polar angle distribution  $\cos \theta_b$  of generated *b*-quarks and final reconstructed *b*-jets including any SM background remaining after event selection. Left:  $P(e^+, e^-) = (+100\%, -100\%)$  with a zoom of the region with negative  $\cos \theta_b$ . Right:  $P(e^+, e^-) = (-100\%, +100\%)$ . From [235].

Figure 68 compares the  $\cos \theta$  distribution of the bquark at the generator-level, at reconstruction-level and after all corrections applied, for both opposite-sign polarisation configurations. Both techniques for identifying the *b*-direction, vertex charge and Kaon ID, have been combined here and contribute about equally to the final event sample. These distributions are then used to extract the left- and right-handed couplings of the *b*-quark to the Z-boson and the photon — or alternatively form factors  $F_{1A/V}^{\gamma/Z}$ . The expected precisions on a subset of couplings and form factors is compared to the corresponding LEP results in Fig. 69. The ILC projections in this plot are based on only 500  $\text{fb}^{-1}$  at 250 GeV, corresponding to the data collected in the first couple of years before the luminosity upgrade. For the full data set, further improvement by about a factor of 2 is expected.

## 10. PHYSICS SIMULATIONS: TOP QUARK

In this section, we will review the highlights of the top quark program of linear colliders. Since the top quark has not yet been studied in  $e^+e^-$  reactions, its study at a linear collider gives the opportunity to dramatically improve the precision with which we know its properties. As we have explained above, such precision measurement can reveal clues to the origin of the large mass of the top quark and possibly, through this, to the nature of the Higgs interactions that give mass to all fermions. The potential of linear  $e^+e^-$  colliders for top quark physics is discussed in more detail in the ILC design reports [5, 138] and in Refs. [244–246].



FIG. 69: Comparison of the LEP measurements to the expected precision at the ILC. The results of the ILC correspond to the integrated luminosity of  $\mathcal{L}_I = 500 \text{ fb}^{-1}$  to be collected at  $\sqrt{s} = 250 \text{ GeV}$  before the luminosity upgrade. Final results for the full 250 GeV dataset would improve the precision further by about a factor of 2. From [235].

## 10.1. Selection and reconstruction of topquark pairs

The  $e^+e^- \rightarrow t\bar{t}$  production process has a sizeable cross section above the top quark pair production threshold. With a left-handed electron beam and right-handed positron beam the cross section reaches approximately 1 pb at  $\sqrt{s} = 500$  GeV. Top quark pair production, with the top quarks decaying to a W-boson and a bottom
quark, is the leading six-fermion process. Most recent simulation studies [246-248] have focused on the the lepton+jets final state, where one of the W-bosons decays to a charged lepton and a neutrino and the other W-boson to jets. Compared to the fully hadronic final state [249], the lepton + jets final state offers the advantage of the presence of an energetic charged lepton, that helps to tag top and anti-top quarks and is an efficient polarimeter.

The selection of top quark pair events at the ILC is straightforward. For lepton+jets events the requirement of a charged lepton and two b-tagged jets is sufficient to reduce the Standard Model background. The efficiency of the selection can be very high, between 50 and 80% depending on the purity requirement.

The complete reconstruction of the  $t\bar{t}$  system is more challenging. The assignment of the six fermions to top and anti-top quark candidates suffers from combinatorics that can lead to significant migrations in differential measurements. Their effect on observables such as the forward-backward asymmetry are kept under control by a rigorous selection on the reconstruction quality. The size of potential systematic effects due to the selection and reconstruction of the complex six-fermion final state is then expected to be sub-dominant [247]. Later studies have extended this conclusion to a broader set of observables [246, 248, 250].

To take full advantage of the large integrated luminosity envisaged in the ILC operating scenario, a rigorous control of experimental and theoretical uncertainties is required. Ultimately, we expect that the data-driven techniques developed for the bottom-quark analysis of Ref. [235, 243] will supply an in-situ measurement of the rate of wrong combinations. This will allow one to correct differential measurements using the statistical power of the entire data set.

A complete and quantitative analysis of systematic limitations is currently ongoing. The results presented in this section are based on the prospects of Ref. [246–248]. Where needed, results are extrapolated to the full integrated luminosity of 4  $ab^{-1}$ .

## 10.2. Measurement of the top quark mass

The top quark mass is a fundamental parameter of the Standard Model that must be determined experimentally. Precise measurements are essential for precise tests of the internal consistency of the Standard Model, through the electro-weak fit [251] or the extrapolation of the Higgs potential to very high energy scales [252]. The precise value of the top quark is also needed as input to the theory of flavor-changing weak decays [253] and models of the grand unification of the fundamental interactions [254].

The top quark pair production threshold was identified long ago [255] as an ideal laboratory to measure the top quark mass, and other properties such as the top quark width and the Yukawa coupling and the strong coupling constant [256]. The large natural width of the top quark acts as an infrared cut-off, rendering the threshold cross section insensitive to the non-perturbative confining part of the QCD potential and allowing a well-defined cross section calculation within perturbative QCD. This calculation has now been carried out the N<sup>3</sup>LO order [257] with NNLL resummation [258]. Fully differential results are available in WHIZARD [259].

Given this precise theoretical understanding of the shape of the  $t\bar{t}$  threshold cross section as a function of center of mass energy, it is possible to extract the value of the top quark mass by scanning the values of this cross section near threshold. We emphasize that the top quark mass determined in this way is, directly, a short-distance quantity that is not subject to significant non-perturbative corrections. It is also closely related to the  $\overline{MS}$  top quark mass, the input to the theory calculations listed above. The uncertainty in the conversion is less than 10 MeV [260]. This contrasts with the situation at hadron colliders, where the conversion uncertainties, the nonperturbative corrections, and the experimental systematics in the measured top quark mass contribute independent uncertainties, each of which is about 200 MeV.

A simulation of the threshold scan is presented in Fig. 70. The scan of the  $t\bar{t}$  threshold measures the top quark pair production cross section at ten  $e^+e^-$  centerof-mass energy points. The error bars on the pseudo-data point represent the statistical uncertainty of the measurement, the uncertainty band indicates the theory (scale) uncertainty of the calculation. A fit of the line shape will give a precise extraction of the top quark mass [261–263]. The statistical uncertainty on the threshold mass is reduced to below 20 MeV with a scan of ten times 20 fb<sup>-1</sup>. The total uncertainty on the  $\overline{MS}$  mass can be controlled to the level of 50 MeV. These systematic uncertainties include a rigorous evaluation of theory uncertainties in the threshold calculation and in the conversion to the  $\overline{MS}$  scheme [264].

The top quark mass can also be measured precisely in operation above the  $t\bar{t}$  threshold. The top quark mass can be extracted from the differential cross section of  $t\bar{t}\gamma$  events as a function of the center of mass energy of the  $t\bar{t}$  system  $\sqrt{s'} = \sqrt{s}(1 - E_{\gamma}/\sqrt{s})$ , as shown in Fig. 70. A fit with a calculation that matches the NNLL prediction for the threshold region with an  $\mathcal{O}(\alpha_s^3)$  calculation for the continuum yields a statistical uncertainty with 100 MeV for 4 ab<sup>-1</sup> at 500 GeV [246]. Including the theory uncertainty due to scale variations and experimental systematic uncertainties the total uncertainty is estimated to be below 200 MeV .

A direct mass measurement can reach a statistical precision below 100 MeV [263] and will be helpful to clarify the interpretation of such measurements.

A linear  $e^+e^-$  collider can thus achieve a precision that goes well beyond even the most optimistic scenarios for the evolution of the top quark mass measurement at the LHC.



FIG. 70: Two methods to extract the top quark mass: (upper panel) a scan of the center of mass energy through the top quark pair production threshold, and (lower panel) a reconstruction of the differential  $t\bar{t}\gamma$  cross section as a function of s' during operation at  $\sqrt{s}=500~{\rm GeV}$ .

## 10.3. Searches for flavour changing neutral current interactions of the top quark

Among the direct searches for physics beyond the Standard Model with top quarks in the final state, the searches for flavour changing neutral current interactions of the top quark have been studied in most detail. Thanks to the excellent charm tagging performance and the clean experimental environment such searches at the ILC can compete with the sensitivity of the LHC to anomalous tZc, tHc and  $t\gamma c$  couplings.

Searches for  $e^+e^- \rightarrow tc$  production can already be performed during the 250 GeV stage [265]. Greater sensitivity can be achieved in searches for  $t \rightarrow Hc$  and  $t \rightarrow \gamma c$  decays above the  $t\bar{t}$  production threshold. Based on full-simulation studies [246, 266] scaled to an integrated luminosity of 4 ab<sup>-1</sup> at a center of mass energy of 500 GeV, the 95% C.L. limits on FCNC branching ratios are expected to reach  $BR(t \rightarrow Hc) \sim 3 \times 10^{-5}$  and  $BR(t \rightarrow \gamma c) \sim 10^{-5}$ , well in excess of the limits expected after 3  $ab^{-1}$  at the HL-LHC.

## 10.4. Measurement of the top quark electroweak couplings

Composite Higgs models and models with extra dimensions naturally predict large corrections to the top quark couplings to the Z and W bosons [267–269]. The study of top quark pair production at an  $e^+e$  collider therefore provide a stringent test of such extensions of the SM.

The potential of the 500 GeV ILC for the measurement of the cross section and forward-backward asymmetry in  $t\bar{t}$  is characterized in detail in Ref. [247]. It is important to note that these measurements search for deviations from the SM in the main production mechanism of the  $t\bar{t}$  system through s-channel  $\gamma$  and Z exchange. With two configurations of the beam polarization, measurement of the angular distribution, and measurement variables sensitive to the t and  $\bar{t}$  polarizations, all 6 possible *CP*-conserving form factors can be disentangled and constrained at the 1% level. Especially designed *CP*-odd observables can also provide precise and specific constraints on the CP-violating form factors [248]. The expected 68% C.L. limits on the form factors with 500 fb<sup>-1</sup> at a center of mass energy of 500 GeV are compared to the HL-LHC expectation of Ref. [270, 271] in Fig. 71.

The corrections to the top quark electroweak couplings can be parametrized by set of dimension-6 operators of the SM EFT that contain the top quark as a field. There is a large number of such operators, although the restriction to  $e^+e^-$  reactions allows us to concentrate on a limited set of operators that appear at the tree level in electroweak pair production. Because the top quark is massive, helicity conserving operators such as chiral 4-fermion operators and helicity violating operators that give corrections to the top quark magnetic moments must be considered on an equal footing.

In Ref. [250], the authors consider the perturbation of the reaction  $e^+e^- \rightarrow t\bar{t}$  by the 10 dimension-6 operators that contribute to the cross section at the tree level. They show that a combination of the 500 GeV run, with excellent sensitivity to two-fermion operators, with 1 TeV data, with increased sensitivity to four-fermion operators, yields tight constraints independently on all operator coefficients. This study demonstrates the feasibility of a global EFT analysis of the top sector at the ILC. It also gives an expected sensitivity of the ILC to top electroweak couplings that exceeds that of the HL-LHC programme by one to two orders of magnitude. Translated into discovery potential for concrete BSM scenarios, a linear collider operated above the top quark pair production threshold can probe for compositeness of the Higgs sector to very high scales, up to 10 TeV and beyond [269].

Figure 72 presents the results of a combined fit of the Wilson coefficients dimension-six operators that affect the electroweak interactions of bottom and top quarks. For each operator, limits are extracted from existing LEP I and LHC run 2 data and from prospects for the high-luminosity stage of the LHC and for ILC runs at  $\sqrt{s} =$ 



FIG. 71: The ILC prospects for the measurement of the electroweak couplings of the top quark, expressed as 68% C.L. bounds on the form factors in a general expression for the Lagrangian that describes the  $t\bar{t}Z$  and  $t\bar{t}\gamma$  vertices: (upper panel) CP-conserving form factors from Ref. [272], and (right) CP-violating form factors, from Ref. [248].

### $250~{\rm GeV}$ and $500~{\rm GeV}$ .

The LHC measurements in the top quark sector are extrapolated to the complete program, including the highluminosity phase of the LHC. The detailed analyses presented in Ref. [273] predict that significant progress can be made, especially in the measurements on rare associated processes. The HL-LHC scenarios S1 and S2 are The ILC250 scenario includes measurements of the cross section and forward-backward asymmetry of bottom quark pair production, with a total integrated luminosity of 2 ab<sup>-1</sup> divided between the left-right and right-left beam polarizations, following Ref. [235]. The ILC500 prospects includes in addition the projections at  $\sqrt{s} = 500$  GeV of Ref. [250] for top-quark pair production, scaled to an integrated luminosity of 4 ab<sup>-1</sup> at  $\sqrt{s} = 500$  GeV.

The Z-pole data yield tight constraints on coefficients of operators that are specific to the bottom quark  $C_{\omega b}$ and  $C_{dW}$ . The current LHC constraints on the top quark operators, from single top production, top quark decay and associated  $t\bar{t}X$  production are relatively weak. The operator coefficients  $C_{\varphi}^{1/3}$ , that affect both bottom-quark and top-quark interactions have tight individual limits from LEP, but are poorly constrained in a global fit. The S2 scenario for the HL-LHC foresees a significant increase of the precision of the measurements. The 250 GeV run at the ILC considerably sharpens the limits on the operators that affect the bottom-quark interactions with Z-bosons and photons. Finally, with the 500 GeV data, the operators specific to the top quark, the dipole operators  $C_{tB}$  and  $C_{tW}$  and the operator that  $C_{\varphi t}$  that modifies the right-handed coupling of the top quark. With respect to the current precision the constraints on all operator coefficients are expected to improve by one to two orders of magnitude. The increase in precision is very significant even with respect to the most aggressive scenario for the HL-LHC.

Similar analyses, now requiring only 4 relevant dimension-6 operator coefficients, can improve the constraints on four-fermion operators involving b, c, and light-fermion sectors beyond the results projected in Sec. 9.2.

## 10.5. Measurement of the top quark Yukawa coupling

As with the trilinear Higgs coupling, the top quark Yukawa coupling can be measured either directly or indirectly. In the literature, most estimates of the accuracy of determination of the top quark Yukawa coupling are done within the simple context of the SM with only this one parameter varied. We will first quote uncertainties within this model in this section and then explore the implications of a general EFT analysis.

Consider first the indirect determination of the top quark Yukawa coupling. For the Higgs boson decays  $H \rightarrow gg, H \rightarrow \gamma\gamma$ , and  $H \rightarrow Z\gamma$ , there are no SM

 $\Delta C_i [TeV^{-2}]$  $10^{2}$ EP1 + LHC Run 2 + HL-LHC S1 HL-LHC S2 ILC250 + ILC500 10 1  $10^{-1}$  $10^{-2}$  $10^{-3}$  $C_{\phi t}$  $\boldsymbol{C}_{\boldsymbol{\phi}\boldsymbol{b}}$  $C^3_{\phi Q}$  $C^{1}_{\phi Q}$  $C_{bW}^{R}$  $C_{tW}^{R}$  $C_{tB}^{R}$ 

FIG. 72: The 68% C.L. limits on the Wilson coefficients of the dimension-six operators that affect the electroweak interactions of the top and bottom quark. The filled bars indicate *individual* limits, from a single-parameter fit, while the dashed bars present the *marginalized* limits of a seven-parameter fit. The first bar indicates the current limits, obtained in a fit to LEP I and LHC run 2 measurements. These results are compared with prospects for the HL-LHC, with 3 ab<sup>-1</sup> at  $\sqrt{s} = 14$  TeV. The S1 and S2 scenarios are defined in analogy with the Higgs scenarios of Ref. [126]: S1 envisages no improvement of the systematic uncertainties, while S2 foresees that theory uncertainties can be reduced by a factor 2 and experimental systematic uncertainties are expected to scale with  $1\sqrt{s}$ . The green bars indicate the 250 GeV and 500 GeV runs of the ILC, with 2 ab<sup>-1</sup>.

tree diagrams and so diagrams with top quark loops give leading contributions. For  $h \to gg$ , the top quark loop diagram gives the single largest contribution. In Tab. XX, it is shown that the ILC program up to 500 GeV will determine the effective coupling in this process to bettter than 1%. Even higher precision can be obtained in a joint fit including also the top quark radiative corrections to the cross sections for  $e^+e^- \to ZH$ ,  $e^+e^- \to \nu \overline{\nu}H$ , and  $e^+e^- \to \gamma H$  [274]. However, one should be uncomfortable that, for this determination, the simple model is too simple, since new heavy colored particles can also contribute to these processes at the 1-loop level.

An indirect determination that calls out the top quark more specifically is the measurement of the influence of the top quark Yukawa coupling on the shape of the ttpair production cross section very close to the  $t\bar{t}$  threshold, due to the Higgs boson-exchange contribution to the  $t\bar{t}$  potential. In principle, this effect could give a 4% determination of the Yukawa coupling if the QCD theory of the top quark threshold region were precisely known. However, the Higgs-exchange effect is of the same size as the  $N^3LO$  QCD corrections. At this time, the threshold shape is calculated only to this N<sup>3</sup>LO order, by the use of a very sophisticated NRQCD framework [257], combined with NNLL resummation of large logarithms [258]. Propagating the QCD uncertainties gives an uncertainty of 20% on the top quark Yukawa coupling [245], and there is no clear path at this time to improve the accuracy of

the QCD result.

A more direct – and more robust – extraction of the top quark Yukawa coupling is possible from measurements of the cross section of the associated production process of a Higgs boson with a top quark pair. In the SM the  $pp \rightarrow t\bar{t}h$  and  $e^+e^- \rightarrow t\bar{t}h$  production rates are simply proportional to the square of the Yukawa coupling. The first measurements of the  $t\bar{t}h$  rate at the LHC [275, 276] have an uncertainty of approximately 30% and are expected to improve considerably during the remainder of the LHC program [126].

At an electron-positron collider, the cross section for  $t\bar{t}h$  production increases rapidly above  $\sqrt{s} \sim 500$  GeV, reaching several fb for  $\sqrt{s} = 550$  GeV. Detailed studies of selection and reconstruction of these complex multi-jet events have been performed by the ILC at 500 GeV [277] and 1 TeV [5, 278] and by CLIC at 1.5 TeV [246]. The direct measurement of the top quark Yukawa coupling at the ILC reaches 2.8% precision [129], with 4 ab<sup>-1</sup> at 550 GeV. With a sample of 2.5 ab<sup>-1</sup> at 1 TeV, this precision would improve to 2% [108]. From the energy-dependence of the cross section and the top polarizations, this reaction can also be used to probe for non-standard forms of the *tth* coupling [279].

In principle, the corrections to the top quark electroweak couplings and to the top quark Yukawa coupling should be parametrized by dimension-6 operators of the SM EFT. The studies of Refs. [280, 281] show that the indirect extraction of the Yukawa coupling from the hgg or  $h\gamma\gamma$  vertices do not provide robust measurements of the top quark Yukawa coupling in a general multi-parameter fit. The indirect determination is certainly very sensitive to new physics in the Higgs sector, but in case a deviation from the Standard Model predictions is observed, further measurements are needed to unambiguously identify the operator that gave rise to the effect.

The direct determination from the  $t\bar{t}h$  rate, be it at the LHC or at the ILC, is more robust. However, even in this case vertices arising from dimension-6 operators that do not directly involve the Higgs boson can affect the cross section for  $e^+e^- \rightarrow t\bar{t}h$  and thus create ambiguity in the extraction of the top quark Yukawa coupling. In  $e^+e^- \rightarrow t\bar{t}h$ , the EFT corrections arise from 4-fermion *eett* operators and from operators that correct the  $\gamma$  and Z anomalous moments of the t quark. Similarly, in hadron-hadron collisions, the cross section for  $qq \rightarrow t\bar{t}H$  is corrected by dimension-6 operator that alter the top quark vector coupling to gluons and those which create a possible axial vector coupling to gluons and a gluonic magnetic moment. The 34-parameter fit on current LHC data of Ref. [282] indeed finds that the marginalized limits on the operator  $C_{t\varphi}$  that shifts the top quark Yukawa coupling are considerably weaker than the individual constraints and the results of fits with fewer parameters.

The LHC and a linear  $e^+e^-$  collider offer excellent opportunities to probe the interaction between the top quark and the Higgs boson, both directly and indirectly. In a global EFT fit the coefficients of all operators affecting the Higgs branching ratios and  $t\bar{t}h$  production rate must be constrained to sufficient precision, such that the coefficient of the operator that shifts the Yukawa coupling can be extracted unambiguously. Precise measurements at a linear collider operating above the  $t\bar{t}$  threshold provides powerful constraints to such a fit.

## 11. GLOBAL FIT TO HIGGS BOSON COUPLINGS, AND COMPARISONS OF ILC TO OTHER COLLIDERS

In this section, we make use of the simulation results presented in Secs. 8 and 9 to present projections for the uncertainties in Higgs boson couplings that will be obtained from the ILC. We will present projections both for the 250 GeV stage and for the stage that includes at 500 GeV in the centre of mass, following the plan presented in Sec. 3.

## 11.1. Elements of the fit to Higgs couplings from Effective Field Theory

To extract Higgs boson couplings from measurements, we will use the method of Effective Field Theory (EFT) sketched in Sec. 4.6. This method has been explained in full technical detail in [3, 218]. Here we will present an overview of the EFT analysis, supplying those technical details that are relevant to the evaluation of our fitting procedure.

In the EFT method, we represent the effects of new physics on the Higgs boson and other SM observables by the most general linear combination of dimension-6 operators invariant under  $SU(2) \times U(1)$ . In the most general setting, this formalism contains a very large number of parameters. However, in the special case of  $e^+e^-$  collisions, there are some simplifications. First, for the purpose of computing deviations from the SM due to dimension-6 operators, it suffices to work at the electroweak tree level. (The basic SM predictions must of course be computed as accurately as possible, typically to 2-loop order in electroweak couplings.) Second, it suffices to consider only CP-even observables, since the contributions of *CP*-odd operators can be bounded by independent measurements. With these simplifications, a total of 16 operator coefficients appear in the analysis. One additional parameter  $c_6$  appears in double Higgs production, and 10 additional parameters appear in analyses of top quark production, but these do not enter the extraction of the Higgs couplings we will discuss here.

To determine these operator coefficients, we can use precision electroweak measurements and data on  $e^+e^- \rightarrow W^+W^-$  in addition to data from Higgs processs. The analysis also makes use of specific constraints from the LHC that should be available when the ILC runs and have a clear model-independent interpretation. These are the ratios of branching ratios of the Higgs boson to the final states  $\gamma\gamma$ ,  $ZZ^*$ ,  $Z\gamma$ ,  $\mu^+\mu^-$ . The measurements of these four channels are all based on Higgs bosons produced centrally through the dominant gluon fusion process. The ratios of rates should be extracted from LHC data in a way that most systematic errors are common and cancel in the ratios. It is shown in [3, 218] that this data suffices to determine these coefficients independently and without important degeneracies.<sup>6</sup>

The way that we make use of LHC inputs illustrates the complementarity of LHC and ILC results on the Higgs boson. The LHC has special strength in gathering statistics on rare modes of Higgs decay, especially those with leptons in the final state. On the other hand, results from the ILC are needed to determined the Higgs total width and the absolute normalization of branching ratios and partial widths with minimal model assumptions. In a similar way, the HL-LHC will probe deeply for specific exotic decays of the Higgs boson, especially those involving muons, while ILC is needed to survey the most general possibilities for exotic decays.

Here is an outline of the analysis. We need to fit 16 operator coefficients plus 4 SM parameters which are shifted by dimension-6 effects. The 16 EFT coefficients arise in

<sup>&</sup>lt;sup>6</sup> An 17th operator contributes to  $G_F$  but is controlled by constraints from the measurement of  $e^+e^- \rightarrow \mu^+\mu^-$  at high energy. The bound from LEP 2 is already very strong.

the following way: 2 from Higgs boson operators  $(c_H, c_T)$ , 4 from operators involving the squares or cubes of SM gauge field strengths  $(c_{WW}, c_{WB}, c_{BB}, \text{ and } c_{3W})$ , 3 from Higgs current couplings to leptons  $(c_{HL}, c'_{HL}, c_{HE})$ , 5 from the operators that shift the Higgs coupling to b,  $c, g, \tau, \mu$ , and two more from Higgs current couplings to quarks  $(c_W \text{ and } c_Z)$ .

The parameters are constrained rather specifically, in a way that we can outline. Measurements of  $\alpha$  and  $G_F$ and the W, Z and H masses constrain the SM parameters plus one additional parameter  $(c_T)$ . Purely leptonic precision electroweak measurements ( $\Gamma(Z \to \ell^+ \ell^-)$ ) and  $A_\ell$ ) constrain two of the three  $c_{H\ell}$  parameters, and measurements of the W and Z total widths fix  $c_W$  and  $c_Z$ . Measurements on  $e^+e^- \rightarrow W^+W^-$  constrain the third  $c_{H\ell}$ parameter, plus  $c_{WB}$  and  $c_{3W}$ . The LHC measurement of the ratio of branching ratios  $\Gamma(h \to \gamma \gamma) / \Gamma(h \to ZZ^*)$ will put a strong constraint on  $c_{BB}$ . The Higgs branching ratios to fermion and gluon states constrain those 5 parameters. At this point, only the parameters  $c_H$ and  $c_{WW}$  remain. These are constrained, respectively, by the normalized cross section for  $e^+e^- \rightarrow ZH$  and the polarization asymmetry or angular distribution in this reaction.

To account for the possibility of non-standard Higgs boson decays, we add two more parameters to our global fit. The first is the Higgs branching ratio to invisible decay products. This is independently measurable at an  $e^+e^-$  collider using the Z tag in  $e^+e^- \rightarrow ZH$ . The second is the branching ratio to exotic modes that somehow do not correspond to any category that has been previously defined. Though it might be argued that any Higgs decay mode above the  $10^{-3}$  level of branching ratio should be directly observed, we add this parameter as insurance against modes not yet thought of. It is determined by the constraint that the Higgs branching ratios, including this one, sum to 1.

The ratio of the Higgs couplings to W and Z plays an important role in the extraction of Higgs boson couplings and the Higgs boson total width. In the  $\kappa$  formalism, one parameter is assigned for each of these couplings, and these parameters are determined independently from Higgs production cross sections. This typically leads to very small errors on the Z coupling and large errors on the W coupling. In the EFT formalism, as we have shown in Eq. 8, two parameters are needed to describe each of these couplings, making the  $\kappa$  description oversimplified. The corresponding W and Z parameters are linked by not-so-simple formulae involving other EFT parameters. However, these formula can be evaluated with the help of data from precision electroweak and WW reactions, leading to constraints that are at the same time tight and highly model-independent [218]. This is one illustration of the synergies between different measurements that the EFT method brings into play.

It is remarkable that, though the EFT analysis introduces a large number of free parameters, each one has a direct counterpart in a physical observable that can be

FIG. 73: Feynman diagrams contributing to the process  $e^+e^- \rightarrow Zh$  when contributing dimension-6 operators are included.



FIG. 74: Projected Higgs boson coupling uncertainties when including the charged triple gauge coupling precisions as expected from ILC250, compared to the case of using the corresponding LEP results instead.

measured in the  $e^+e^-$  environment. In particular, beam polarisation is very powerful in providing needed information. For example, in the EFT framework, the process  $e^+e^- \rightarrow ZH$  involves three diagrams, shown in Fig. 73. Only the first diagram appears in the SM. The third diagram is required to be small by precision electroweak constraints. The second diagram, with s-channel  $\gamma$  exchange, is generated by the operator corresponding to the coefficient  $c_{WW}$ . Under a spin reversal  $e_L^- \leftrightarrow e_R^-$ , the Z diagram flips sign while the  $\gamma$  diagram keeps the same sign. Thus, measurement of the polarisation asymmetry in the total cross section for  $e^+e^- \rightarrow ZH$  directly measures the  $c_{WW}$  parameter. Beam polarisation plays another important role. With beam polarisation, the branching ratios of the Higgs boson are measured for two different polarisation settings. The statement that the same branching ratio must appear in each pair of measurements helps to sharpen the global fit. At the same time, this comparison provides a check of assigned systematic errors. In Sec. 11.2, we will assess the importance of polarisation quantitatively and present results on the trade-off between polarisation and increased luminosity.

The precise measurement of the triple gauge bosons

couplings expected at the ILC also plays an important role in global fit. We have described the measurement of these couplings through analysis of  $e^+e^- \rightarrow W^+W^-$  in Sec. 9.1. The ILC is expected to improve the precision of our knowledge of these couplings by a factor of 10 over results from LEP and by a similar large factor over results from LHC. Figure 74 shows the significance of this set of inputs. In the figure, the results of our global fit, in green, are compared to the same fit using as inputs the LEP constraints on the triple gauge boson couplings.

From this analysis, we derive the projected uncertainties on Higgs couplings shown in Tab. XVI. Here and in the rest of this section, the uncertainty presented in the tables for each  $HA\overline{A}$  coupling is defined to be half of the fractional uncertainty in the corresponding partial width. In cases such as HZZ in which multiple EFT coefficients contribute to a given partial width (see Eq. 8), the quoted uncertainty includes the uncertainties in these EFT parameters and their correlation.

Table XVI is the main result of this report in relation to the ILC capabilities for Higgs boson coupling measurements. This table gives the current state of our understanding of the ILC capabilities. We emphasise that the analysis leading to these projections is completely modelindependent, in the sense that all models of new physics describable either by the addition of local operators to the SM EFT (for heavy new particles) or by the addition of invisible and exotic Higgs decays (for light new particles) are included. Given the run plan and detector designs described above, we have a high degree of confidence that these estimated uncertainties will be achieved – and, probably, surpassed – in the realisation of the ILC program. The projections in the table are summarised in Fig. 75.

# 11.2. Comparison of $e^+e^-$ Higgs factory proposals

In this section, we will present a comparison of the capabilities of the ILC for precision Higgs measurement with those of other proposed linear and circular colliders, including CLIC, CEPC, and FCC-ee. We will present three sets of quantitative comparisons.

To begin, each collider proposal has presented its own set of projections in its documentation for the European strategy study. We have copied the relevant numbers for projected Higgs boson coupling uncertainties into Tab. XVII. For colliders other than the ILC, those estimates have been made using the more model-dependent  $\kappa$ fit. The small values of the ZZ coupling uncertainty relative to the WW coupling uncertainty reflects the modeldependence of the  $\kappa$  formalism as discussed in Sec. 11.1.

It is interesting to ask how the proposals would compare if a common fitting technique is used. In almost all cases, the measurement errors are dominated by statistics and the efficiencies used in the analyses are similar. A direct way to make the comparison is to use the results of our ILC analyses to estimate efficiencies and statistical errors for all of the colliders. That is, we assume

coupling $2$	$ab^{-1}$ at 250	$0 + 4 \text{ ab}^{-1} \text{ at } 500$
HZZ	0.56	0.38
HWW	0.55	0.37
Hbb	1.0	0.60
$H\tau\tau$	1.2	0.77
Hgg	1.6	0.96
Hcc	1.8	1.2
$H\gamma\gamma$	1.1	1.0
$H\gamma Z$	7.5	4.0
$H\mu\mu$	4.0	3.8
Htt	-	6.3
HHH	-	27
$\Gamma_{tot}$	2.4	1.6
$\Gamma_{inv}$	0.36	0.32

TABLE XVI: Projected uncertainties in the Higgs boson couplings for the ILC at 250 GeV and 500 GeV, with precision LHC input, assuming the integrated luminosities in the H20 program. All values are given in percent (%). The definition of a Higgs coupling uncertainty, for the purpose of

this table, is half the fractional uncertainty in the corresponding Higgs boson partial width. (See the text for further explanation.) The ILC at 250 GeV only does not have direct sensitivity to the Htt and HHH couplings; thus no model-independent values are given in these lines. The bottom lines give, for reference, the projected uncertainties in the Higgs boson total width and the 95% confidence limits on the Higgs boson invisible width. The analysis, which applies Effective Field Theory as described in the text, is highly model-independent

the luminosity samples in the collider proposals, assume the same measurement errors per unit of luminosity used to generate Tab. XVI, take account of differences in the cross sections resulting from the use (or not) of polarized beams, and rerun our fitting program for those conditions. This is the method used to generate Tab. 3 of Ref. [3]. As a proxy for CEPC, we assume a sample of 5  $ab^{-1}$  at 250 GeV without polarisation. As a proxy for FCC-ee, we use a sample of 5  $ab^{-1}$  at 250 GeV plus 1.5  $ab^{-1}$  at 350 GeV, without polarisation. The run plan for CLIC includes only 1  $ab^{-1}$  at 380 GeV before the energy upgrade to 1 TeV. Since we are uncomfortable using the EFT formalism with dimension-6 operators only at 1 TeV and above, we represent CLIC by a sample of 2  $ab^{-1}$ , similar to ILC, with 80%  $e^{-1}$  polarisation only, at 350 GeV. The results are presented in Tab. XVIII and visualised in Fig. 76.

Though not all differences among the various proposals are included in this table, the table does usefully show how increased luminosity trades off against beam polarisation. We see that beam polarisation is a very powerful tool, essentially compensating the advantage of larger event samples claimed by the circular machines. Note that the advantage is not uniform; increased luminosity is a generally greater benefit for smaller couplings such as Hcc, while polarisation has special benefit for specific couplings such as  $H\gamma Z$ . The comparison of 2 ab<sup>-1</sup> data samples at 250 and 350 GeV is also interesting, since



FIG. 75: Projected Higgs boson coupling uncertainties for the ILC program at 250 GeV and an energy upgrade to 500 GeV, using the highly model-independent analysis presented in [4]. This analysis makes use of data on  $e^+e^- \rightarrow W^+W^-$  in addition to Higgs boson observables and also incorporates projected LHC results, as described in the text. The darker bands correspond to the values given in Tab. XVI. The lighter bands correspond to the scenario S2\* in Table XX, which is defined

correspond to the values given in Tab. XVI. The lighter bands correspond to the scenario S2<sup>\*</sup> in Table XX, which is defined in the discussion of Sec. 11.3. The column  $\lambda$  refers to the *HHH* coupling. In the last four columns, all bars are rescaled by the indicated factor.

coupling	EFT fit	EFT fit	$\kappa$ fit				
HZZ	0.56	0.38	0.25	0.17	0.6	0.6	0.6
HWW	0.55	0.37	1.4	0.43	1.0	0.6	0.6
Hbb	1.0	0.60	1.3	0.61	2.1	0.7	0.7
$H\tau\tau$	1.2	0.77	1.5	0.74	3.1	1.4	1.0
Hgg	1.6	0.96	1.5	1.01	2.6	1.4	1.0
Hcc	1.8	1.2	2.2	1.21	4.4	1.9	1.4
$H\gamma\gamma$	1.1	1.0	1.6	1.3	-	4.8	2.3
$H\mu\mu$	4.0	3.8	5.0	3.8	-	12.1	5.7
Htt	-	6.3	-	-	-	3.0	3.0
HHH	-	27	-	-	-	35	9
$\Gamma_{tot}$	2.4	1.6	2.8	1.3	4.7	2.6	2.5
$\Gamma_{inv}$	0.36	0.32	< 0.3	-	-	-	-

ILC250 ILC500 CEPC FCC-ee CLIC350 CLIC1.4 CLIC3

TABLE XVII: Projected uncertainties in the Higgs boson couplings quoted in the CDRs presented to the European Strategy Study. The methodology of the fit is indicated. The precise definition of a Higgs coupling uncertainty for the ILC EFT analysis is given at the end of Sec. 11.1 and in the caption of Tab. XVI. For the ILC, the values are taken from Tab. XVI. For the CEPC, the values are taken from Ref. [283], Tab. 11.4. For the FCC-ee, the values are taken from Ref. [284], Tab. 1.2. As discussed later, the capability for  $\Gamma_{inv}$  is similar to that for CEPC. For CLIC, the values are taken from Ref. [285], Tab. 2, with *HHH* values from Ref. [215]. All values are given in percent (%). The bottom lines give, for reference, the projected uncertainties in the Higgs boson total width and the 95% confidence limits on the Higgs boson invisible width. For ILC, CEPC, and FCC-ee, the values given for the  $\gamma\gamma$  and  $\mu\mu$  modes are takes combined with expected LHC results.

the two energy settings bring different advantages to the Higgs physics study.

To make the comparison in Tab. XVIII more realistic, we should indicate how the improved precision electroweak measurements that can be achieved at circular colliders affect these numbers. The answer to this question is given in Tab. XIX, which is compared with Tab. XVIII in Fig. 77. For the ILC columns, we have

	2/ab-250	+4/ab-500	5/ab-250	+ 1.5/ab-350	2/ab-350
coupling	pol.	pol.	unpol.	unpol	$e^{-}$ pol.
HZZ	0.56	0.38	0.80	0.42	0.51
HWW	0.55	0.37	0.80	0.42	0.50
Hbb	1.0	0.60	0.98	0.66	1.0
$H\tau\tau$	1.2	0.77	1.0	0.75	1.3
Hgg	1.6	0.96	1.3	0.99	1.6
Hcc	1.8	1.2	1.4	1.2	2.2
$H\gamma\gamma$	1.1	1.0	1.2	1.0	1.1
$H\gamma Z$	7.5	4.0	8.5	6.8	6.6
$H\mu\mu$	4.0	3.8	3.8	3.7	4.0
Htt	-	6.3	-	-	-
HHH	-	27	-	-	-
$\Gamma_{tot}$	2.4	1.6	2.1	1.5	2.4
$\Gamma_{inv}$	0.36	0.32	0.34	0.30	0.58

050

1 5 / 1 250 0 / 1

TABLE XVIII: Projected uncertainties in the Higgs boson couplings computed using the EFT method, with ILC uncertainties per unit of luminosity and assuming a run with the quoted integrated luminosity and energy. The notation is that of Tab. XVI. The first two columns are identical to the ILC values from Tab. XVI. In the last column, we assume 80% electron polarisation and zero positron polarisation.



FIG. 76: Projected Higgs boson coupling uncertainties for selected scenarios from Table XVIII. In particular it shows that at  $\sqrt{s} = 250 \text{ GeV}, 2 \text{ ab}^{-1}$  with polarised beams yield comparable results to a much larger data set of 5  $\text{ ab}^{-1}$  with unpolarised beams.

assumed that the input measurement of  $A_{\ell}$ , the polarisation asymmetry of the lepton-Z coupling, will be improved by a factor 10 by measurement of the polarisation asymmetry in  $e^+e^- \rightarrow Z\gamma$  at 250 GeV. This is one of the improvements to our Higgs analysis currently under study listed in Sec. 8.4. The improvement in  $A_{\ell}$ by a dedicated "Giga-Z" run at the Z pole would be comparable [138]. For the third and fourth columns, we assume the improvements in measurements of precision electroweak observables described in the FCC-ee CDR [284].

The ILC results with polarised beams are somewhat improved in the most precisely determined couplings by the improvement in the input  $A_{\ell}$ . The changes for circular colliders, which make use of the large improvements from Z pole running, are more significant for the results at 250 GeV. More surprisingly, though, the improvement in precision electroweak inputs turns out to make only a

	2/ab-250	+4/ab-500	5/ab-250	+ 1.5/ab-350
coupling	pol.	pol.	unpol.	unpol
HZZ	0.50	0.36	0.64	0.40
HWW	0.50	0.36	0.65	0.41
Hbb	1.0	0.59	0.87	0.66
$H\tau\tau$	1.1	0.75	0.95	0.75
Hgg	1.6	0.96	1.2	0.98
Hcc	1.8	1.2	1.4	1.1
$H\gamma\gamma$	1.1	1.0	1.1	1.0
$H\gamma Z$	7.0	3.7	8.3	5.1
$H\mu\mu$	4.0	3.8	3.8	3.7
Htt	-	6.3	-	-
HHH	-	27	-	-
$\Gamma_{tot}$	2.3	1.6	1.9	1.5
$\Gamma_{inv}$	0.36	0.32	0.34	0.30

TABLE XIX: Projected uncertainties in the Higgs boson couplings computed using the same methodology as in Tab. XVIII but including projected improvements in precision electroweak measurements. In the first two columns, the polarised collider projections from Tab. XVIII are modified to include an improvement by a factor 10 in  $A_{\ell}$ , as discussed in Sec. 8.4. In the second two columns, the unpolarised collider projections from Tab. XVIII are modified to include the improvement of the uncertainties on precision electroweak observables described in the FCC-ee CDR [284].

small difference when the dataset at 350 GeV is added. One reason for this, pointed out in Ref. [218], is that the EFT coefficients responsible for precision electroweak corrections also contribute terms of order  $s/m_Z^2$  to the  $e^+e^- \rightarrow ZH$  cross section. Then these coefficients are powerfully constrained by comparing measurements of this cross section at different centre-of-mass energies.

## 11.3. Comparison of the ILC and the HL-LHC Higgs capabilities

Finally, we compare the capabilities of the ILC for precision Higgs measurement to those of the HL-LHC.

In Sec. 4, we have presented qualitative comparisons of the approach to Higgs physics that is possible at the ILC to the approach that must be taken at the LHC. Here we will compare the quantitative projections given in Sec. 11.1 to the projections presented in the HL-LHC Yellow Report [126]. The comparison is not so straightforward because of the different frameworks used in the analyses. In Tab. XX, we quote projected uncertainties in Higgs boson couplings for HL-LHC given in Ref. [126] and present results from the ILC global fit in a number of scenarios.

The projections in Ref. [126] are based on operational experience with detectors that have successfully made measurements on the Higgs boson, have exceeded their expectations from the proposal stage, and, based on that experience, expect further improvements beyond the level of their current methodologies. These estimates are based on extrapolation of current results. They do depend on the assumption that the improvement of the ATLAS and CMS detectors by the Phase-II upgrades will fully compensate for the effects of the high-pileup environment expected at the HL-LHC. With this understanding, these estimates give the expectations for the performance of the ATLAS and CMS experiments in the HL-LHC program.

In addition to the formal HL-LHC projections, which are ATLAS/CMS combinations, the individual LHC experiments have actually produced two sets of projections, a final one (S2) described above and a maximally conservative one (S1) that includes the increase in statistics from HL-LHC but uses only current methodologies and current estimates of systematic errors. It is interesting to us to compare the S1 and S2 projections, since this comparison gives an idea of the improvements expected by the LHC experiments beyond the current state of the art to the end of the HL-LHC program. In Tab. XX we have quoted both the S1 numbers from CMS (those from ATLAS are similar) and the final (S2) projections from Ref. [126]. At the S2 level, the systematic errors are estimated to be small enough that the projections benefit by about 20% from making an ATLAS/CMS combination.

We call to the reader's attention the fact that the improvements projected for HL-LHC from the current AT-LAS and CMS uncertainties on the HZZ and HWW couplings are very significant already in the S1 analysis. This is because the high statistics of the HL-LHC allows one to make use of the vector boson fusion production mode, which has a low cross section but relatively small theoretical and modelling uncertainties. On the other hand, the projected improvement in the Hbb couplings is based mainly on a higher-precision understanding of analyses such as that shown in the upper plot of Fig. 45.

The ILC estimates have a very different basis. It is always risky to estimate errors for experiments that have not yet been constructed or taken data. We have designed the ILC detectors to have the superb performance characteristics detailed in Secs. 6 and 7. As far as is possible today, these projected performances are justified by R&D and test beam measurements. However, from this point, we wished to be quite conservative. We



FIG. 77: Impact of improved electroweak precision observables on the projected precisions for various Higgs couplings for the combinations of luminosity, energy and polarisation from Tab. XIX. For the unpolarised cases, EWPO projections from the FCC-ee CDR [284] have been assumed, while for the polarised case only an improved precision for  $A_{\ell}$  is assumed. Couplings for which there is no improvement due to improved EWPO have been omitted from the figure. The notation of the figure is the same as that in Fig. 75.

then take the expected precision of our measurements to be those of our current analyses of fully simulated, digitised events. This conservative choice is the basis of the estimates quoted in Sec. 11.1. Experience at all other colliders has shown that final precision with real data exceeds such *a priori* estimates.

To compare these projections with those for HL-LHC, we have defined four scenarios, called S1\*, S1, S2\*, S2. The projections in Tab. XX labeled  $S1^*$  are those from Tab. XVI in Sec. 11.1. While, as we have stressed, the ILC analysis is highly model-independent, the LHC analvsis relies on certain model assumptions that are difficult to remove with only the constraints available at a hadron collider. The LHC results in Tab. XX assume that the Higgs boson has no decay modes beyond those predicted in the SM, and they assume that the Higgs boson couplings to WW and ZZ are modified only by a rescaling. In the ILC EFT analysis, each of these these couplings depends on two additional independent constants  $\zeta_W$  and  $\zeta_Z$  defined in Eq. 8. For a sharper comparison, then, we have then recast the ILC EFT analysis adding these two assumptions, that is, assuming no Beyond-Standard-Model decays and assuming  $\zeta_W = \zeta_Z = 0$ . This gives the set of values labelled S1. We do foresee some improvements in our analyses, as described in Sec. 8.4. These reflect improvements to our methods that are under study and seem promising but are not vet completely

validated. Making these improvements gives the uncertainties S2\* and S2 (for model-independent and modeldependent EFT fits) quoted in Tab. XX. These estimates are intended give an indication that the ILC capabilites are not fixed but rather are improvable with further experimental effort. We remind the reader that all estimates quoted for ILC require certain specific inputs from HL-LHC, as explained in Sec. 11.1. Our use of HL-LHC results nicely illustrates the complementarity of the two machines, as is discussed in that section.

It is subtle to directly compare the projections for HL-LHC and ILC taking into account their two different philosophies. On the ILC side, since we have no experience with the actual operation of the detectors and the accelerator, we have been very cautious in making extrapolations beyond our current full-simulation results to the actual performance that we might eventually achieve. We therefore regard our scenario S1, and even our scenario S2, to be more conservative than the final (S2) HL-LHC projections. In any event, we hope that we have described the various estimates given in Tab. XX clearly enough that the reader can make his or her own judgement as to the most appropriate comparison of the ILC to the HL-LHC.

In all cases, however, it is only the ILC results that cross a boundary into the region in which we can robustly claim discovery of deviations from the SM of the size



FIG. 78: Projected Higgs boson coupling uncertainties for the LHC and ILC using the model-dependent assumptions appropriate to the LHC Higgs coupling fit. The dark and light red bars represent the projections in the scenarios S1 and S2 presented in Ref. [126]. The dark and light green bars represent the projections in the ILC scenarios S1 and S2 described in the text. The dark and light blue bars show the projections for scenarios S1 and S2 when data from the 500 GeV run of the ILC is included. The notation of the figure is the same as that in Fig. 75.

generally expected in new physics models.

In summary, Figs. 75 and 78 illustrate the capabilities of the ILC and the comparison of the ILC and LHC projections. Figure 75 shows the uncertainty projections for the 250 GeV stage of the ILC, in the highly modelindependent framework S1<sup>\*</sup>. These results are compared to results obtained in the same framework with the addition of data from an energy upgrade to 500 GeV. This justifies the statement made earlier that deviations from the SM seen at the 250 GeV stage of the ILC can be confirmed with an independent data set after the upgrade to higher energy. Figure 78 shows the comparison of the ILC projections in the S1 and S2 scenarios to the projections given for the S1 and final (S2) HL-LHC projections given in Ref. [126]. Note that, while the improvement from the S1 to S2 scenarios for ILC is a matter of conjecture, the improvement from the 250 GeV to the 500 GeV values is based on completed full-simulation studies.

## 12. PHYSICS SIMULATIONS: DI-RECT SEARCHES FOR NEW PARTI-CLES

In this section, we will discuss the prospects at the ILC for the direct discovery of new particles. Our discussion will of course be given in the context in which the LHC experiments have carried out a large number of new particle searches, some reaching deeply into the mass region above 1 TeV. Still, we will explain, experiments at  $e^+e^-$  colliders can bring a new approach to new particle searches and still have very interesting windows for discovery.

In general, the new particle searches done at the LHC have focused on scenarios within each theory of new physics that give the *best* possible experimental prospects to observe new physics. However, a negative result will only make it possible to claim that new physics is absent in a specific region of the full theoretical parameter space. There is no guarantee that new physics would be discovered even if it is within the kinematic reach of the experiment. The actual parameters of the theory might be far from the ones giving the searched-for signature.

It is a rather different perspective to concentrate on the *worst* possible points in the theoretical parameter space. This clearly cannot reach as far out as in the previous case, but now a negative result would make it possible to claim that the new physics theory is ruled out at *all* possible parameter values below the kinematic reach of the experiment. It would also make discovery of the new physics *guaranteed* if it is indeed energetically reachable.

These two avenues in the search for new physics are in fact the main difference between searches at hadron colliders and lepton colliders. Hadron colliders are well

coupling	current	$S1^*$	S1	$S2^*$	S2
HZZ - LHC	11.		2.4		1.5
- ILC 250		0.56	0.46	0.47	0.37
- ILC 500		0.38	0.20	0.33	0.18
HWW - LHC	15.		2.6		1.7
- ILC 250		0.55	0.44	0.47	0.36
- ILC 500		0.37	0.19	0.33	0.18
Hbb - LHC	29.		6.0		3.7
- ILC 250		1.0	0.83	0.81	0.69
- ILC 500		0.60	0.43	0.49	0.37
$H\tau\tau$ - LHC	17.		2.8		2.0
- ILC 250		1.2	0.98	0.98	0.86
- ILC 500		0.77	0.63	0.68	0.59
Hgg - LHC	15.		4.0		2.5
- ILC 250		1.6	1.6	1.2	1.2
- ILC 500		0.96	0.91	0.75	0.70
<i>Hcc</i> - LHC	-		-		-
- ILC 250		1.8	1.8	1.4	1.3
- ILC 500		1.2	1.1	0.9	0.85
$H\gamma\gamma$ - LHC	15.		2.9		1.8
- ILC 250		1.1	1.1	1.1	1.0
- ILC 500		1.0	0.97	1.0	0.96
$H\gamma Z$ - LHC	15.				9.8
- ILC 250		7.5		7.0	
- ILC 500		4.0		3.5	
$H\mu\mu$ - LHC	70.		6.7		4.3
- ILC 250		4.0	4.0	4.0	4.0
- ILC 500		3.8	3.7	3.8	3.7
Htt - LHC	14.		5.5		3.4
- ILC 500		6.3	4.1	4.5	2.8
HHH - LHC			80		50
- ILC 500		27	27	20	20
$\Gamma_{tot}$ - LHC	28		5		4
- ILC 250	-	2.4	1.4	1.9	1.1
- ILC 500		1.6	0.70	1.3	0.60
$\overline{\Gamma_{inv}}$ - LHC	26	-		-	3.8
- ILC 250	-	0.36	-	0.36	_
- ILC 500		0.32	-	0.32	-

TABLE XX: Projected uncertainties in the Higgs boson couplings for HL-LHC and for ILC with the specific LHC inputs described in the text, in various scenarios. All values are given in percent (%). The precise definition of a Higgs coupling uncertainty for the ILC EFT analysis is given at the end of Sec. 11.1. The values labelled "current" are taken mainly from Table 8 of the CMS publication Ref. [286]; the values for  $\Gamma_{tot}$  and  $\Gamma_{inv}$  are found in the text of Sec. 8.2 and Sec 3.9, respectively. The LHC S1 values are those from the  $\kappa$  fit to CMS projections, given in Tab. 36 of Ref. [126]; the ATLAS projections are similar. The S2 values are those

from the ATLAS/CMS combination given in Fig. 30 of Ref. [126]. Values for the HHH coupling are found in the text of Sec. 3.2 of Ref. [126]. Values for  $\Gamma_{tot}$  and  $\Gamma_{inv}$  are found in the text of Sec. 2.7.1 and Sec 6.1, respectively, in

Ref. [126]; these are CMS results only. For ILC, the S1<sup>\*</sup> results are those presented in Sec. 11.1 for ILC programs at 250 GeV and 500 GeV. The scenario S1 includes the same values for ILC measurement uncertainties but also includes additional model-dependent assumptions that are used in the LHC S1 analysis. These are described in the text. The scenarios S2<sup>\*</sup> and S2 assume the improved performance in

ILC measurements presented in Sec. 8.4.

suited for the first approach, with their large reach into unknown territory in energy, but are less well suited for the second one due to huge background levels and to the initial state being unknown. Lepton colliders have a lower reach in energy, but excel in fully exploiting all possible manifestations of new physics within reach. When comparing exiting limits on new physics from LHC or LEP, commonly presented in the mass-plane of a pair of new states, one must note that the former are incomplete ones showing models than *might* be excluded (for some - but not all - other model parameters), while the latter shows complete ones, i.e. models that *must* be excluded (for any value of other parameters).

ILC—like LEP—will explore all corners of the parameter spaces of theoretical models. It offers a guaranteed discovery within the kinematic reach of the machine and, in the case of no discovery, sets immutable limits that can be the final word the models it considers. In this section, we will concentrate on this aspect, explaining how ILC will expand the region of fully-explored theory space beyond that of LEP.

It is clear that an ILC operating at 500 GeV, or even at 1 TeV, will vastly extend the fully explored region. But, already at 250 GeV, ILC will significantly extend this region: While it is true that 250 GeV is not much more than the maximum energy of 208 GeV that LEP reached, there are other features that are ameliorated by orders of magnitude: The luminosity is 1000 times higher, and both beams are polarised. The beam-spot is sub-microscopic in size, allowing to find displaced vertices at much smaller distances, also in channels (like  $\tilde{\tau}$  pair production), where there is no reconstructable primary vertex. Furthermore, many aspects of the detectors are better than the LEP ones by a factor ten or more. Since computing power has been increased by orders of magnitude, all interactions can be recorded and analysed, i.e. no trigger will be needed for experiments at the ILC, unlike the conditions at LEP. Taken together, this means that much more subtle effects can be probed for at energies that in principle were reachable at LEP.

Many of these features also are relevant in exploiting LHC's blind-spots: namely any signal stemming from processes without QCD interactions, or with only soft final states. Here, trigger-less operation of almost fully hermetic detectors is a great advantage. Processes where only kinematic reconstruction of the full event would reveal BSM physics, can be studied at a lepton collider. In contrast, at a pp collider, only partial reconstruction in the transverse plane is possible. In addition, ILC detectors will be more precise than their LHC counter-parts, since the low background-rates means that it is not necessary to compromise between performance and radiation-hardness.

We will discuss a few particular classes of signatures, which have been studied in depth:

• Pair-production of new short-lived states decaying to visible SM particles and another lighter new state, the lighter state being invisible, the so-called *antler* signatures. R-parity conserving SUSY is an example.

- Production of new invisible final states, where only the presence of initial state radiation could reveal new phenomena, the *mono-photon* signature. A prominent example is dark matter production.
- Production of new scalars, similar to the SM Higgs boson, but with smaller coupling to the Z, and possibly very different decay branching ratios, the *new*-scalar signature. Here nMSSM and 2HDM models are typical examples.

In addition to these cases discussed in detail, other extensions to the SM can be searched for at the ILC. Compared to a hadron collider, a lepton collider is much less dependent on missing energy signature to find new physics. For example, in R-parity violating SUSY or models with visible signs of a dark sector, or in composite models, new physics does not necessarily manifest itself with a missing energy signature, but rather by the presence of new states. New physics could also manifest itself as new couplings, rather than new particles, e.g., in unexpected flavour signatures. ILC-250 would be able to probe such signatures, in some cases with a sensitivity equal to that of dedicated flavour experiments, like BELLE II or LHCB. In general, due to the low background levels, the ILC can be used to search for any new particle in nature with electromagnetic, hyper-charge or electroweak quantum numbers and thus provides discovery potential complementary to that of the LHC. A comprehensive overview of the potential of the full ILC program to discover new particles and phenomena can be found in [136].

#### 12.1. Pair-production signatures

A event-signature that often occurs in BSM theories is the "antler" topology. In such processes, a pair of (not necessarily identical) new states are produced. These particles then decay into SM particles and a lighter new state. The lighter state might further decay to other SM particles, and an even lighter new state. At the end of such a cascade of decays, a detector-stable new state,  $\chi$ , is produced, which is not directly detectable. The properties of the visible decay-products not only reveals the presence of physics beyond the standard model, but also contain a large amount of information about the properties of the new states.

In the case of direct decays of a pair of new state(s) (denoted by X and Y) produced in an  $e^+e^-$  collision at  $E_{lab} = E_{cms} = M_o$ , the endpoints of the energies of the standard model particles x and y in the process

 $e^+e^- \rightarrow XY \rightarrow xy\chi\chi$  can be found to be

$$E_{i_{(min)}^{max}} = \frac{M_0}{4} \left( \sqrt{\frac{\lambda_{0,X,Y} + 4M_0^2 M_{i'}^2}{M_0^4}} \frac{\sqrt{\lambda_{i',i,\chi} + 4M_{i'}^2 M_i^2}}{M_{i'}^2} \right)^+ \left( \sqrt{\frac{\lambda_{0,X,Y}}{M_0^4}} \frac{\sqrt{\lambda_{i',i,\chi}}}{M_{i'}^2} \right)$$
(23)

where the shorthand  $\lambda_{k,l,m} = \lambda(M_k^2, M_l^2, M_m^2)$  is used<sup>7</sup>, and *i'* is either X or Y (and similarly, *i* is the corresponding SM particle, either x or y)[287]. By determining these endpoints of the energy-spectra of the two SM particles (x and y), and using the knowledge of  $E_{\text{cms}}, M_x$  and  $M_y$ , both  $M_{\chi}, M_X$  and  $M_Y$  can be determined. If the two initially produced new particles have the same mass, so that  $M_X = M_Y = M_{i'}$ , then  $\lambda_{0,X,Y} = M_0^4 - 4M_o^2 M_{i'}^2$ . If, in addition, the masses of the produced SM particles can be neglected,  $\lambda_{i',i,\chi} = (M_{i'}^2 - M_{\chi}^2)^2$ . Hence, in the important case of pair production,  $e^+e^- \rightarrow Y\overline{Y} \rightarrow y\overline{y}\chi\chi$ with  $M_y \approx 0$ , one finds the simpler relation

$$E_{y_{(min)}^{max}} = \frac{E_{\rm cms}}{4} \left( 1 - \left(\frac{M_{\chi}}{M_Y}\right)^2 \right) \\ \left( 1 {}_{(-)}^+ \sqrt{1 - 4 \left(\frac{M_Y}{E_{\rm cms}}\right)^2} \right)$$
(24)

from which  $M_{\chi}$  and  $M_Y$  can be determined from the end-points.

R-parity conserving SUSY is a model that predicts a variety of antler-type signatures, in sfermion or bosino production. The lightest SUSY particle (the LSP) would be the final, undetectable, new state, and would usually be the lightest neutralino,  $\widetilde{\chi}_1^0$ , even though other candidates also would be possible. Both pair-production and associated production can occur, and the decays might be direct or in cascades. The produced pair might be fermions (bosinos), or scalars (sfermions), and can carry a variety of different quantum-numbers. Hence, an extensive study of SUSY covers a wide range of possible antler topologies. The essential difference between SUSY and the general case, is that SUSY predicts the couplings, by the fundamental principle of SUSY: spaticles couples as particles. From the experimental point of view, the implication of this is rather in the interpretation in terms of exclusion- or discovery-reach, than in the actual analysismethods required. In the SUSY case, regions in the massplane can be fully exploited, since the production crosssection is predicted. In the general case, the conclusion would be that discovery or exclusion is possible down to some minimal cross-section, determined by the data. Therefore, the extensive study of SUSY at past and future lepton colliders serves as a boiler-plate for any search

 $<sup>^7~</sup>$  The Källén function  $\lambda$  is defined as  $\lambda(a,b,c)=a^2+b^2+c^2-2ab-2ac-2bc$ 

for new physics with antler signatures. In the following we will concentrate on the SUSY case.

### 12.1.1. Loop-hole free searches

In [288], it is shown how experiments an  $e^+e^-$  collider can systematically and exhaustively search for *any* Nextto-lightest SUSY Particle (NLSP), and thereby guarantee discovery, or set immutable limits for SUSY within the kinematic reach of the accelerator.

LHC has set no limits on processes giving the weakest limits, such as sleptons in general, and staus in particular. In Refs. [289–291], it is shown that limits on selectrons and smuons can be set in the best possible case - either requiring that not only that both selectrons and smuons have the same mass, but also that the left- and righthanded states are degenerate, or that the mass difference to the LSP is very large. No limits at all could be set for stau production. One the other hand, LHC does give stringent limits on a gluino or first- or second-generation squarks [292]. Also for a stop, the LHC coverage is increasing, and excludes a stop with a mass of 1 TeV, if the LSP mass is below 250 GeV [292, 293]. However, both theoretically, and given these limits, it is quite unlikely that a coloured sparticle would be the NLSP.

Instead, the most stringent absolute limits on the NLSP comes from LEP. There limits on all SUSY particles has been set. In [177, 294–296], searches for sleptons are reported, in [177, 295, 297, 298], the results of the searches for squarks can be found, and in [177, 299–301], the results for charginos and neutralinos are given. In addition, combined results can be found in [302].

A summary of the LEP results is that a chargino NLSP below between 92 and 103 GeV (depending on the mass-difference) is excluded, whatever the nature of the chargino is. For the second neutralino, a general exclusion in the mass-plane is not possible, due to the complicated structure of the neutralino mass-matrix, which allows for situations where the cross-sections both for  $e^+e^- \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_2^0$  and  $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0$  can be small at the same time. For any given SUSY model, however, the combination of the searches for  $e^+e^- \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_2^0$ ,  $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0$  and  $e^+e^- \rightarrow \tilde{\chi}_e^1 \tilde{\chi}_1^+$ , as well as the searches for  $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0$  and  $e^+e^- \rightarrow \tilde{\nu}_e \tilde{\nu}_e$  (since the  $\tilde{e}$  and the  $\tilde{\nu}_e$  contribute to t-channel production of  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^\pm$ , respectively) will be likely to yield constraints on  $M_{\tilde{\chi}_2^0}$ .

In the slepton sector, smuons and selectrons are excluded below 95 to 100 GeV, if the mass difference to the LSP is above 4 GeV. Staus are excluded below 87 to 93 GeV, if the difference is above 8 GeV. Selectrons and smuons are completely excluded below  $M_Z/2$  (from the width of the Z), while staus are excluded below 28 GeV for any mass-difference and mixing. The weaker limit for the staus is due to the fact that it is possible that the stau mixing is such that it does not couple at all to the Z, only to the photon, and hence that the constraint from the width of the Z cannot be applied. In fact, the limit from the stau at minimal cross-section is the weakest limit on any NLSP candidate, and therefore represents the current absolute exclusion for any MSSM model.

In addition, LEP excludes third generation squarks below 94 to 98 GeV at mass differences to the  $\tilde{\chi}_1^0$  larger than 8 GeV and the mixing angle giving the minimal crosssection are excluded. For any mixing, mass-difference and dominant decay mode, a stop with mass below 63 GeV is excluded. However, these coloured sector limits are essentially superseded by the LHC ones.

It can be noted that, except for the chargino, the LEP limits fall short of the kinematic limit by 10 to 20 % even for large mass-differences, and for small differences by 50 % or more. This is due to the fact that the size of the data-sets at the highest energies were tiny - 500  $pb^{-1}$ at 206 GeV, and only 33  $pb^{-1}$  at 208 GeV. This low luminosity is particularly unfavorable for the sfermions, because of the slow  $(\beta^3)$  rise of the cross-section close to threshold. Also, the LEP detectors all were triggered, meaning that in the low mass-difference cases, either some auxiliary activity was needed to provide a trigger, or only a small fraction of the events - those where the detectable SM decay-products happened to be almost aligned with the direction of the decaying sparticle would be registered. This resulted in a quite low selection efficiency in these cases. Furthermore, due to the large size of the beam-spot at LEP, using impact-parameters as a tool to separate signal and background was not very effective. Finally, the beams at LEP were unpolarised, which is a particular draw-back when searching for signs of a chiral theory such as SUSY.

In contrast, the ILC has none of these problems, as already mentioned, which means that the ILC will largely extend the territory explored by LEP. The same features of the ILC allows to probe for signals in the LHC blind areas for un-coloured states at lower mass differences.

In [288], the prospects at the ILC at 500 are evaluated. Two cases were studied in more detail, the least and the most challenging ones, namely the cases where the NLSP is either the  $\tilde{\mu}_{\rm R}$  or the  $\tilde{\tau}_1$ . The first case profits from a very clean and well measured signal, with no other parameters than the two masses involved, while the second one has the most difficult signal (due to the partly invisible SM system), and in addition has a further theory parameter, namely the  $\tilde{\tau}$  mixing angle. For both these cases, the full mass-plane was scanned over a 1-by-1 GeV grid, using the detailed fast simulation SGV, described in 7.7. In the  $\tilde{\tau}_1$  case, the mixing-angle was chosen such that the production cross-section was as small as possible. The resulting exclusion/discovery reaches are shown in Fig. 79. One can note that the exclusion limit, even for the rather modest luminosity used in the study is only 0.8 (4) % from the kinematic limit for the  $\tilde{\mu}_{\rm R}(\tilde{\tau}_1)$ . Hence, the area of assured discovery-potential or power of model-independent exclusion will increase by a factor of 6 to 7 with respect to current (LEP) results.

Even for an ILC operating at 250 GeV, a substantial increase in reach is expected. The area of the excluded



FIG. 79: ILC discovery reach for a  $\tilde{\mu}_{\rm R}$  (top)  $\tilde{\tau}_1$  (bottom) NLSP for  $\int \mathcal{L} dt = 500 \text{ fb}^{-1}$  at  $\sqrt{s} = 500 \text{ GeV}$ . For the  $\tilde{\tau}_1$ , the mixing angle was chosen to give the lowest possible production cross-section. (a,c) full scale, (b,d) zoom to last few GeV before the kinematic limit [288].

mass plane will increase much more than the modest increase in energy might suggest at first glance. Reasonably assuming that also at 250 GeV, reach will fall only a few percent short of the kinematic limit, the area covered by ILC-250 will increase by 70 % to 80 % at large mass-differences compared to the LEP results. At the smallest mass-differences, even larger improvements might be expected, once dedicated analyses have been performed in this region. Also at 250 GeV, the reach into LHC's blind areas will be important.

### 12.1.2. Sleptons

In [287] and [303] more in-depth analyses of specific models are presented. The emphasis in these works is to estimate the precision with which various parameters can be extracted. The analyses were done with the full SM background simulated with full detector simulation at  $E_{\rm cms}$ = 500 GeV. In [303], also the signal was simulated with full simulation, while the detailed fast simulation SGV was used in [287]<sup>8</sup>. In Fig. 80, the energy-spectra of the visible decay-products of  $\tilde{e}_{\rm R}$ ,  $\tilde{\mu}$  and  $\tilde{\tau}_1$  are shown. A number of novel techniques were utilised to extract the relevant edges from the distributions (the truncated sub-sample method [287], and finite impulse response method [304]), both giving precisions a factor two or more better than traditional methods. Once the edges were determined, applying Eq. 23, the masses of  $\tilde{e}_{\rm R}$  and  $\tilde{\mu}_{\rm R}$  could be estimated with an error of 2 ‰ and 4 ‰, respectively. Fitting for a single value of  $M_{\tilde{\chi}_1^0}$  in these two spectra, an error of 1.5 ‰ was obtained. Using the value of  $M_{\tilde{\chi}_1^0}$ , and

 $<sup>^8</sup>$  The models studied allows for  $\widetilde{\rm e}_{\rm R},\,\widetilde{\mu}_{\rm R}.$  and  $\widetilde{\tau}_1$  production also at  $E_{\rm cms}{=}~250~{\rm GeV}$ 



FIG. 80: Property determination of SUSY (a) selectron. (b) muon and (c)  $\tau$ -jet energies in selected di-leptons events after collecting 500 fb<sup>-1</sup> of data for beam-polarisation  $\mathcal{P}_{-80,+30}$  [287].

fitting spectrum in Fig. 80c for  $M_{\widetilde{\tau}_1}$ , the  $\widetilde{\tau}_1$  mass could be determined to 2 ‰.

Furthermore, as can also be seen from Eq. 23, close to the threshold, the decay-products become monoenergetic which means that an almost background-free threshold-scan can be done at a collider – such as ILC – where  $E_{\rm cms}$  can be freely chosen. The result of such a scan is shown in Fig. 81. The precision of the masses are comparable to those obtained from the fit to the spectra, but are independent of  $M_{\tilde{\chi}_1^0}$ . In addition, the fit to the shape of the threshold makes it possible to exclude the hypothesis that the new states discovered are fermions, as can be see by the fits of either  $\sigma \propto \beta^3$  (expected for scalars) or  $\sigma \propto \beta$  (expected for fermions).

A further measurement possible in these models is the determination of the polarisation of the  $\tau$ -lepton from the  $\tilde{\tau}_1$  decay. This is achieved by studying the spectrum of the  $\pi$ :s in the  $\tau \to \pi \nu_{\tau}$  mode, or the ratio of  $E_{\pi}^{\pm}$  to  $E_{\pi}^{0} + E_{\pi}^{\pm}$  in the  $\tau \to \rho \nu_{\tau} \to \pi^{\pm} \pi^{0} \nu_{\tau}$  mode. In [303] it was found that the degree of polarisation could be determined to  $\sim 8$  %. Also in [303], it was found that the cross-section for  $\tilde{\tau}_1$  pair-production could be determined to 4 %. The difference in the cross-section when the beam-polarisations are reversed can be used to determine the  $\tilde{\tau}$  mixing angle<sup>9</sup>, which together with the determine the size of the chirality-conserving gauagino fraction of the  $\tilde{\chi}_1^0$  relative to it's chirality-flipping higgsino fraction.

#### 12.1.3. Bosinos

In [287, 305–307] detailed studies of specific points where a bosino is the NLSP are presented. Many different topologies are covered by the analyses, depending on the mass-difference. The bosinos might decay to on-shell Zor W bosons, undergo three-body decays (mediated by virtual Z or W bosons), or decay radiatively. In addition, mixing in the bosino-sector will yield relations between the masses of  $\tilde{\chi}_2^0$ ,  $\tilde{\chi}_1^{\pm}$  and the LSP, relations that are different for different models. The same is true for the production cross-sections, in particular the relation between  $\tilde{\chi}_2^0 \tilde{\chi}_2^0$  pair-production and  $\tilde{\chi}_1^0 \tilde{\chi}_2^0$  associated production. Also assumed relations at the high scale have implications on the phenomenology at the EW-scale, in particular on how large the LSP-NLSP mass difference can be. For bosino production it is therefore needed to study various cases in detail, and avoid assumptions on other related processes. The LEP experiments all carried out a comprehensive search for a  $\tilde{\chi}_1^{\pm}$  NLSP which were combined in [302]. For the  $\tilde{\chi}_2^0$  NLSP case, as mentioned is section 12.1.1, only cross-section limits can be given, if no assumptions on the model is done. Such limits were given by the experiments [177, 299, 301].

At LHC, the reach of the search for the non-coloured bosinos can be quite large, but always with strong model assumptions. Even so, the limits tend to disappear for low mass-differences, and are largely absent in the region allowed if GUT-scale unification of the bino and wino mass-parameters ( $M_1$  and  $M_2$ ) is assumed [289, 308, 309].

Once again, the conditions at the ILC will allow to extend the model-independent LEP limits to higher masses. Because the  $\tilde{\chi}_1^{\pm}$  cross-section is quite large, and has a sharp ( $\propto \beta$ ) threshold dependence, the increase in reach at ILC-250 with respect to LEP is not as large as it is for the sfermions: already LEP could exclude an  $\tilde{\chi}_1^{\pm}$ NLSP to only a few GeV below the kinematic limit and at all mass-differences. However, the ILC potential be-

<sup>&</sup>lt;sup>9</sup> The other possibility to determine the mixing-angle, namely the  $\tilde{\tau}_1 \tilde{\tau}_2$  associated production have not yet been studied in detail



FIG. 81: : Scans over the threshold for slepton production (a) scan of the  $e^+e^- \rightarrow \tilde{e}_R \tilde{e}_R$  threshold (b) scan of the  $e^+e^- \rightarrow \tilde{\mu}_R \tilde{\mu}_R$  [287].

comes very important at a 500 GeV, and even more so after a future energy-upgrade to 1 TeV. Nevertheless, the limit/discovery potential of ILC-250 is still sizeable compared to current and future LHC limits, in particular as the LHC limits for bosinos suffer more from modeldependence than the sfermion ones.

This is illustrated by a specific example in figure 82, which shows the current limits in the  $M_{\tilde{\chi}_1^0} - M_{\tilde{\chi}_1^{\pm}}$  plane from ATLAS [290], together with the projected discovery reach at 14 TeV with  $\int \mathcal{L} dt = 3000 \text{ fb}^{-1}$  [310] Here it is assumed that  $M_{\tilde{\chi}_2^0} = M_{\tilde{\chi}_1^{\pm}}$ , that  $\tilde{\chi}_1^{\pm}$  and  $\tilde{\chi}_2^0$  are pure Winos, and that  $\text{Br}(\tilde{\chi} \to W^{(*)}/Z^{(*)}\tilde{\chi}_1^0) = 1^{-10}$ . The brown-shaded area indicates the corresponding limit from LEP [177, 300, 311], which assumes only  $\tilde{\chi}_1^{\pm}$  pair production, with no assumption on the decay mode, nor the nature of the  $\tilde{\chi}_1^{\pm}$ . The expected limits for the ILC at  $\sqrt{s} = 500$  or 1000 GeV are also shown with the same assumptions as for the LEP exclusion. As can be seen from the (loophole) region not covered by the LHC, there is a large discovery potential for the ILC, even after the high luminosity LHC data has been fully exploited.

#### 12.1.4. Small mass differences

The case with antler topologies with small massdifferences is particularly interesting for ILC, already at 250 GeV. Partly because the experimental limits from LEP are much weaker then for high mass differences, and largely absent at LHC, but also for theoretical reasons.

One reason to particularly search for SUSY with small mass-differences is the possibility that the LSP is the (full) explanation for Dark Matter: Over a large region of SUSY parameter space, co-annihilation with the

<sup>10</sup> Note that the more difficult case  $\tilde{\chi} \to h^{(*)} \tilde{\chi}_1^0$  is not considered.

NLSP is an attractive mechanism which acts to reduce the relic density of the LSP to its cosmologically observed value [312]. An example of such a model is the one presented in [287] and discussed in the previous section. In this model, the NLSP is the  $\tilde{\tau}_1$ , with a mass 10 GeV above the LSP. Co-annihilation requires a small mass difference between the NLSP and the LSP in order to be effective, and thus the expected value of the relic density depends strongly on the exact masses and mixings of the involved particles, requiring measurements at the permille and percent-level, respectively. This is discussed in [313], where also a detailed analysis of the relicdensity determination that the measurements presented in [287] would imply. Figure 83a shows the precision of the fitted relic density relative to the model value. In the figure, the model value was chosen to be the central value determined from cosmology using the observations of PLANCK [314]. It was also verified the other modelvalues were faithfully reproduced by the fit, see Fig. 83b.

A second reason to search for such low mass-difference processes, applying to SUSY is that they tend to occur in many possible SUSY scenarios, as shown in Fig. 84, because of the mass-relations between different bosinos in the Wino- and Higgsino-sectors, the second lightest bosino will be close in mass to the LSP, if the latter is dominantly Wino or Higgsino. Only in the case of a large admixture of Bino in the LSP can the mass-difference be arbitrarily large. Furthermore, *if* GUT-scale unification of the Bino and Wino mass parameters  $M_1$  and  $M_2$  holds, the next-to-lightest bosino *cannot* be heavier the twice the LSP mass[315].

In fact, light higgsinos are a fundamental requirement of natural SUSY models. The generic formula relating



FIG. 82: Discovery or exclusion regions in the  $M_{NLSP} - M_{LSP}$  plane for a  $\tilde{\chi}_1^{\pm}$  or  $\tilde{\chi}_2^0$  NLSP. Solid brown area: LEP exclusion; Solid red and dashed grey/blue lines: ATLAS exclusion (observed and expected), for the 8 TeV data (thinner lines) and the 13 TeV data (thicker lines). Dashed green line: ATLAS 14 TeV discovery projections for  $\int \mathcal{L} dt = 3000 \text{ fb}^{-1}$ ; Dashed magenta (orange) lines: ILC discovery expectation for  $E_{CMS} = 500$  (1000) GeV; Solid black line: below line, no GUT scale gaugino mass unification. The symbols indicate the positions in the mass-plane of the analyses mentioned in the text. The magenta solid area is the ATLAS low  $\Delta(M)$  search at 13 TeV, which however is within a different model.



FIG. 83: (a) Comparison of relic density fitted to the measurements of the SUSY model to the model value, with or without using input from ILC higgs-measurements and with, in addition, using measured cross-sections. (b) Comparison between fitted and model value, when the model value was by hand modified as indicated. From [313].

 $M_Z$  to SUSY parameters reads [316]:

$$\frac{m_Z^2}{2} = \frac{(m_{H_d}^2 + \Sigma_d^d) - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{(\tan^2 \beta - 1)} - \mu^2$$
$$\simeq -m_{H_u}^2 - \mu^2 \tag{25}$$

To avoid unnatural fine-tuning between the terms on the right-hand side in this expression, each term should individually be of the order of the left-hand side, *i.e.*,  $M_Z^2$ , and in particular  $\mu$  should be as close as possible to  $M_Z$ . This leads to a dominantly higgsino LSP and that also  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^{\pm}$  are mainly higgsino. Mass differences within the higgsino sector are small, typically below 20 GeV, depending on the values of the other SUSY parameters, in particular on  $M_1$  and  $M_2$ . The other SUSY particles can be more heavy: top squarks may range up to ~ 3 TeV and gluinos up to ~ 4 TeV with little cost to naturalness [316]. Such heavy top squarks and gluinos may well lie beyond the reach of even HL-LHC.

In the clean environment of the ILC, the soft visible decay products of  $\tilde{\chi}_2^0$  and  $\tilde{\chi}_1^{\pm}$  can be easily detected — without any need to rely on large-mass-gap decays of heavier particles. The ILC capabilities have been studied in detector simulations performed for different benchmark points with mass differences ranging from 770 MeV [305] to 20 GeV [306]. Two examples of the striking signals



FIG. 84:  $M_{\tilde{\chi}_1^0}$  vs  $M_{\tilde{\chi}_1^\pm}$  when scanning over the bosino parameters  $M_1, M_2, \tan \beta$  and  $\mu$ . (a) Higgsino-like LSP ( $\mu < M_1, M_2$ ), (b) Wino-like LSP ( $M_2 < \mu, M_1$ ), (c) Bino-like LSP ( $M_1 < \mu, M_2$ ).

and the extraction of kinematic endpoints are given in Fig. 85. The resulting precisions on masses and polarised cross sections reach the percent level even in the experimentally most difficult cases and allow to determine other SUSY parameters. They will also play an important role in unveiling the nature of dark matter: in this case with the result that the LSP only contributes a small fraction of the total abundance. Such a situation might call for additional, non-WIMP constituents of dark matter such as axions. In [317], it is shown that an ILC operating at 1 TeV would have guaranteed discovery/exclusion reach over the entire class of natural SUSY models, which is illustrated in Fig. 86 for the example of the NUMH2 model [318]. Only highly fine-tuned, un-natural, models would still be allowed if ILC at 1 TeV failed to discover SUSY. No such statement can be expected to come out of HL-LHC: even though discovery would be possible at HL-LHC, no guarantee is possible.

### 12.2. Mono-photon signature

The primary probe at the ILC for the direct production of WIMP dark matter are photons emitted as initialstate radiation in association with the pair production of dark matter. Such a Mono-photon search is analogous to Mono-X searches at the LHC. The main backgrounds to this search are the radiative neutrino production, which is irreducible, and the radiative Bhabha scattering process, in which the outgoing electron and positron escape undetected in the beam pipe. At LEP, searches for photon events with missing energy were performed [320], and were later re-analysed within the effective operator framework [321]<sup>11</sup>.

The prospects to detect WIMPs with such methods at the ILC and to determine their properties have been studied for a centre-of-mass energy of 500 GeV in detailed detector simulation [106, 322]. Also at the ILC, the experimental sensitivity have been interpreted in the framework of effective operators. Figure 87a shows the exclusion reach found, and Fig. 87b shows the extrapolation of these results to a wide range of integrated luminosities and centre-of-mass energies [106]. For the full 500 GeVprogram of the ILC, scales of new physics ( $\Lambda$ ) of up to 3 TeV can be probed, while the 1 TeV-energy-upgrade of the ILC would extend this even to 4.5 TeV or more, depending on the integrated luminosity. At 250 GeV, the full reach will be attained already at a modest integrated luminosity.

If a WIMP would be discovered, its properties could be determined precisely due to the known initial state of a lepton collider [322]. In particular, its mass could be determined with a precision of about 1%, and the type of operator (or the angular momentum of dominant partial wave) of the WIMP pair production process can be determined. By such detailed measurements of WIMP properties as offered at the ILC, it is often possible to constrain WIMP production rates in the early universe along with WIMP scattering or annihilation rates and the local WIMP abundance [323]. Such checks could verify or falsify the simple assumptions associated with thermal DM production within the WIMP miracle scenario, thus giving important insights into the nature of dark matter.

Searches for WIMP dark matter at the ILC are highly complementary to those at hadron colliders and at direct detection experiments: as an electron-positron collider, ILC is sensitive to WIMP couplings to electrons, whereas hadron colliders and direct detection experiments are sensitive to WIMP couplings to quarks. Depending on the type of particle mediating the WIMP-SM interaction, there is a priori no reason for these couplings to be of similar strength. Thus, if the LHC does not discover a deviation from the SM expectation in its Mono-X searches, it is essential to complement the picture by probing the WIMP-lepton couplings at an electronpositron collider. Moreover, while LHC can probe larger

<sup>&</sup>lt;sup>11</sup> Note that under LEP or ILC conditions the effective field theory approximation is accurate, while it is questionable in similar analyses at hadron colliders.



FIG. 85: Higgsino mass determination for (a) the charged higgsino from the recoil against an ISR photon in a scenario with a mass splitting of 770 MeV [305], using the SGV detector simulation. (b) the neutral higgsino from the energy of its visible decay products in a scenario with a mass splitting of 10 GeV [306], using full detector simulation.



FIG. 86: The  $m_{1/2}$  vs.  $\mu$  plane in the NUHM2 model for tan  $\beta = 15$ ,  $m_0 = 5$  TeV,  $A_0 = -8$  TeV and  $m_A = 1$  TeV. We show contours of the naturalness measure  $\Delta_{EW}$  [319] along with current limits from LHC13 and future reach of HL-LHC and ILC. Location of benchmark points is indicated in green.

WIMP masses due to its higher centre-of-mass energy, ILC can probe smaller couplings, thus higher energy scales for the WIMP-electron interaction due to its higher precision.

## 12.3. New-scalar signatures

In many models with extended Higgs sectors, *e.g.*, Two Higgs Doublet Models, The Next-to-Minimal Supersymmetric Standard Model and Randall Sundrum models, there exists a light scalar  $S^0$ , lighter than the Standard



FIG. 87: Left: Observational reach ( $3\sigma$ ) of the ILC for a Spin-1 WIMP in terms of WIMP mass and  $\kappa_e$  for three different chiralities of the WIMP-fermion couplings Right: Expected sensitivity for a vector operator in an EFT-based interpretation as a function of integrated luminosity and centre-of-mass energy [106].

Model Higgs. The coupling of the  $S^0$  to the Z can be very small, compared to the coupling a standard model Higgs with the same mass would have to the Z. Such a light scalar with suppressed couplings to the Z boson would have escaped detection at LEP. With a factor of 1000 higher luminosity and polarised beams, the ILC is expected to have substantial discovery potential for this kind of states. Furthermore, searches for additional scalars at LEP and LHC are usually dependent on the model details, in particular on the decay branching ratios of the new scalar. Thus, to be able to search for such new states, it is paramount to have a more general analysis without model-dependent assumptions. The recoil-mass technique, in particular with the Z boson decaying into a pair of leptons, offers the possibility to achieve this.

The OPAL collaboration at LEP searched for light scalars with this method, but the results were limited due to the low luminosity [324]. The large luminosity offered by the ILC makes the recoil mass technique correspondingly more powerful [108] Therefore a search for a light scalar with a very weak interaction with the Z boson using the model-independent analysis would become viable at the ILC-250.

A study was performed using the full GEANT4-based simulation of the ILD concept. As a preliminary result [325], exclusion cross-section limits for masses of the new scalar between 10 and 120 GeV are given in terms of a scale factor k with respect to the cross-section of the Standard Model Higgsstrahlung process would have had, would the Higgs-mass have been the one assumed for the new scalar.

Background events are rejected by considering kinematic variables only relied on muons and the reconstructed Z: The invariant mass, transverse momentum and polar angle of the muon pair, as well as the polar angle of the missing momentum, and the polar angle of each muon, and the angle between them. Thus, no information on the decay of  $S^0$  is used, and the results will indeed be model-independent. The recoil mass distributions obtained after applying the cuts are shown in Fig. 88a, for a number of hypotheses on the mass of  $S^0$ , and k = 1.

The main backgrounds depend on the scalar mass. In the small mass region, the two fermions background  $e^+e^- \rightarrow \mu^+\mu^-$  with an energetic ISR photon is the overwhelming background; while in the Z-pole region,  $e^+e^- \rightarrow ZZ \rightarrow \mu^+\mu^- + X$  is an irreducible background, as is - obviously -  $e^+e^- \rightarrow Z^* \rightarrow ZH \rightarrow \mu^+\mu^-H$  at  $M_{S^0} \sim M_H$ . The two fermion background can be further rejected by taking into account ISR photon return effects. The ISR photon veto cuts are applied to the ISR photons in the centre region and forward region, separately.

The obtained  $2\sigma$  expected exclusion limits for the cross section scale factor  $k_{95}$  are shown for scalar mass from 10 GeV to 120 GeV in Fig. 88b. It is one to two orders of magnitude more sensitive than LEP, and covering substantial new phase space. In particular, at all studied points, a new scalar with a coupling to the Z greater than 1% of that of a SM-higgs at the same mass would be excluded or discovered at ILC-250. Preliminary studies indicate that an ILC operating at 500 GeV could discover or exclude such a scalar with a mass up to 350 GeV, even if the coupling is only one tenth of the coupling of a would-be SM Higgs at the same mass [326]

## 13. CONCLUSION

In this report, we have reviewed the full panorama of the International Linear Collider project.

This machine addresses compelling physics questions. In our quest to discover new interactions beyond the Standard Model, the couplings of the Higgs boson are



FIG. 88: (a) The recoil mass distributions for various signals and all backgrounds after the cuts From [325]. (b) The 2  $\sigma$  exclusion limits for the cross section scale factor k comparing the LEP and ILC-250 results. From [325]. (b) The 2  $\sigma$  exclusion limits for the cross section scale factor k comparing for ILC 250 and ILC-500. From [326].

the most obvious place to look, and the one place where today we are not looking with sufficient power. The ILC will supply the capabilities that we need to study the Higgs boson and other particles with the degree of precision that is actually required to learn their secrets.

The ILC provides a fully formed project proposal with a total cost estimate similar to that of the LHC, a moderate time scale for its construction, and well-tested technologies for its accelerator and detector designs. The ILC is designed as a staged machine with its first stage at 250 GeV. Its design includes straightforward upgrade paths to extend this initial configuration. The full ILC machine will be capable of running at center-of-mass energies from the Z pole to 1 TeV, covering the production thresholds of: Z, WW, Z-Higgs, top-quark, top-Higgs and Higgs pair production. The choice of energy can respond flexibly to new discoveries in particle physics, at the LHC, at the ILC, or at other facilities.

The ILC detectors are designed to meet the challenges of high precision. Taking advantage of the more benign environment of  $e^+e^-$  colliders, they are designed for performance on charged-particle tracking, heavy-flavor identification, and calorimetry that improve on existing detectors by large factors. These are essential capabilities to confidently obtain the high-quality measurements that we seek.

For first time in a collider for particle physics, the detectors will operate without any trigger system. Physics analyses and data-acquisition architecture will considerably benefit from this fact and consequently simplify with respect to present and past experiments. The overall computing costs should be an order of magnitude smaller than those for the LHC. The software and computing tools so far developed provide physics simulations and detector studies that give solid predictions for the ILC performance toward its physics goals. We have presented the results of those studies in this document.

The ILC will use polarised electron and positron beams. Beam polarisation brings both quantitative and qualitative advantages with respect to unpolarized  $e^+e^-$  colliders. Polarisation enhances signal reactions and allows the measurement of helicity-dependent observables, multiplying the physics output per unit of luminosity. It also allows suppression of backgrounds and accurate control of systematic errors, improving the robustness of high-precision measurements.

The ILC machine is ready for construction. We have described the detailed design of the ILC, explaining how the performance of each component is supported by prototyping and, in most cases, by operational/industrial experience.

The physics program begins with a stage at 250 GeV in the center of mass. At this stage, each Higgs boson is produced together with a Z boson at 110 GeV lab energy that serves to tag the event. This allows unambiguous, model-independent measurements of the total cross section for Higgs boson production and the branching ratios for Higgs boson decays. It also gives a tool for searches for exotic Higgs boson decays, including decays to invisible or partially visible final states.

Measurements at the 250 GeV stage will improve current measurements of W boson couplings and SM quark and lepton couplings by large factors beyond what is possible at the HL-LHC.

The simplicity of  $e^+e^-$  pair production allows the full set of electroweak and Higgs processes at the ILC to be combined in a global fit based on an Effective Field Theory description of modifications of the Standard Model. This framework is essentially model-independent with respect to new physics. Within this framework, the 250 GeV stage of the ILC will measure the *Hbb* couplings to 1%, the *HWW* and *HZZ* to 0.7%, and all other important Higgs boson couplings to levels close to 1%. These are the levels of precision required to access new physics beyond the reach of direct searches at HL-LHC.

The first-stage ILC is intrinsically upgradable in energy and luminosity. The accelerator and detectors are designed for operation up to a center of mass energy of 1 TeV. The technology, detector performance, and physics for the 500 GeV stage has been described in detail. All of the measurements discussed in the previous paragraphs benefit, with the uncertainties in Higgs boson couplings decreasing by a factor of 2. The 500 GeV stage offers a program exploring the couplings of the top quark and thus a second, independent, opportunity to probe for new physics through precision measurement. It also offers the opportunity to search for pair-production of elusive particles produced in electroweak interactions that are challenging to discover at the LHC. Running at the Z pole (ILC-GigaZ) is also possible. Essential observables implying lepton or quark left-right asymmetries can be measured with extremely high accuracy when combined with other measurements above the Z.

The opportunities that the ILC gives to discover new physics are robust, and the ILC measurements are improvable as the accelerator moves from one energy stage to the next.

We have compared the projected ILC performance

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on Higgs boson couplings to those put forward for other colliders. The ILC will provide a significant and necessary—step in precision beyond the HL-LHC. A number of other proposals for  $e^+e^-$  Higgs factories are now under discussion. We have shown that none expects a performance significantly superior to the ILC even at its 250 GeV stage. Also, no other proposal has been designed and costed at the level of a formal proposal. Only ILC is on the table today.

Finally, the ILC laboratory will provide a base for future proposals of  $e^+e^-$  and  $\gamma\gamma$  colliders based on advanced high-gradient acceleration. The ILC laboratory thus can expect a long lifetime, beyond our current horizon, in which it will continue to explore the frontier of fundamental physics.

Come join us! It is time to make the International Linear Collider a reality.

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