

**MATH 341**  
**MIDTERM 2 REVIEW**

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The format and length of the second midterm will be similar to the first, except there will be some true / false questions on it. Here is a list of textbook problems similar in scope and difficulty to the second midterm, to use as review. (This list is longer than the midterm itself.)

- §2.2: Find the inverse of  $\begin{bmatrix} -1 & -1 & 1 & -3 \\ -1 & -2 & 2 & -2 \\ 0 & 3 & -2 & 2 \\ 0 & -4 & 3 & 0 \end{bmatrix}$ .
- §2.5: 11, 18
- §2.8: 23, 29
- §2.9: 6, 9
- Supplementary exercises p. 162: 6, 8, 9
- §3.1: 9
- §3.2: 8, 39
- Indicate whether each statement is true or false. If true, give a one sentence explanation of why. If false, give an example to show it is false (i.e., a counterexample).
  - (a) If  $AB = AC$  and  $\det(A) = 7$  then  $B = C$ .
  - (b) If  $A$  is a  $4 \times 4$  matrix and the row-reduced echelon form of  $A$  has 3 pivots then  $\det(A)$  is non-zero.
  - (c) If a linear transformation  $T$  is onto then the standard matrix for  $T$  has at least as many rows as columns.
  - (d) If a linear transformation  $T$  is one-to-one then the standard matrix for  $T$  has at least as many rows as columns.
  - (e) If  $A$  is a  $3 \times 3$  matrix and the equation  $A\vec{x} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$  has infinitely many solutions then  $\det(A) \neq 0$ .
  - (f) If  $A$  is a  $3 \times 3$  matrix and the equation  $A\vec{x} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$  has exactly one solution then  $A$  is invertible.
  - (g) If  $A$  is a  $4 \times 4$  matrix and the null space of  $A$  is 3-dimensional then the column space of  $A$  is 2-dimensional.
  - (h) If  $A$  is a  $4 \times 4$  matrix and the row space of  $A$  is 3-dimensional then the column space of  $A$  is 3-dimensional.

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