## WORKSHEET: DERIVATIVES AND LOCAL EXTREMUMS

Names and student IDs:

Recall that a differentiable function f is increasing on (a, b) exactly when  $f'(x) \ge 0$  on (a, b), and that f is decreasing on (a, b) exactly when  $f'(x) \le 0$  on (a, b).

Also recall that f'(a) is the slope of the tangent line to the graph of y = f(x) at x = a (the point (a, f(a)) on the graph).

1. Draw the graph of a differentiable (in particular, continuous) function f which is decreasing on the open interval (0,2) and increasing on the open interval (2,6). What kind of feature does this function have at x = 2?

2. Draw the graph of a differentiable (in particular, continuous) function f such that f'(x) < 0 on the open interval (0, 2) and f'(x) > 0 on the open interval (2, 6). What kind of feature does this function have at x = 2?

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3. Draw the graph of a differentiable (in particular, continuous) function f such that f'(3) = 0and f'(x) is increasing on the interval [3,6). In particular, as you move right through [3,6), the slopes of the tangent lines are positive and the tangent lines are getting steeper.

4. Draw the graph of a differentiable (in particular, continuous) function f such that f'(3) = 0and f'(x) is increasing on the interval (0,3]. In particular, as you move right through (0,3], the slopes of the tangent lines are negative and the tangent lines are getting less steep (since, for example, -2 < -1 < 0).

5. Draw the graph of a differentiable (in particular, continuous) function f such that f'(2) = 0and f'(x) is increasing on the open interval (0,6). In particular, as you move right through (0,6), the slopes of the tangent lines are increasing and switch from negative to positive at x = 2. What kind of feature does this function have at x = 2?

6. From the reminder at the top of the page, but applied with f = g': if g' is differentiable, then g' is decreasing on (a, b) exactly when  $g''(x) \leq 0$  on (a, b).

Draw the graph of a twice differentiable (in particular, continuous) function g such that g'(4) = 0and g''(x) < 0 on the open interval (0,6). What kind of feature does this function have at x = 2?